Experiments

Effective Lagrangians

# Lecture 1: Introduction to Dark Matter Direct Detection

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Frontiers in Dark Matter, Neutrinos, and Particle Physics Theoretical Physics Summer School



MELBOURNE

Sun Yat-Sen University, Guangzhou July 27-28, 2017



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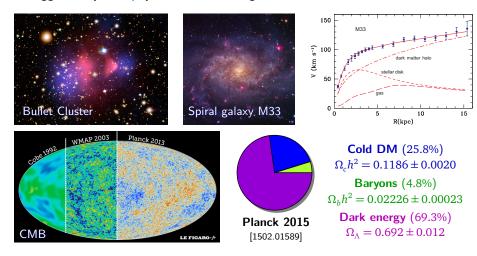
**Dark Matter Direct Detection** 

July 2017 1 / 37

Basics	Experiments	Effective Lagrangians	Homework
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#### Dark Matter in the Universe

**Dark matter (DM)** makes up most of the matter component in the Universe, as suggested by astrophysical and cosmological observations



Basics	
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Experiments

Effective Lagrangians

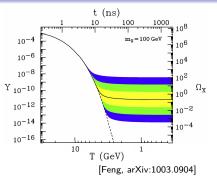
# **DM Relic Abundance**

If DM particles ( $\chi$ ) were thermally produced in the early Universe, their **relic abundance** would be determined by the annihilation cross section  $\langle \sigma_{ann} \nu \rangle$ :

$$\Omega_{\chi}h^2 \simeq \frac{3\times 10^{-27}~{\rm cm}^3{\rm s}^{-1}}{\langle\sigma_{\rm ann}\nu\rangle}$$

Observation value  $\Omega_{\chi} h^2 \simeq 0.1$ 

$$\Rightarrow \quad \langle \sigma_{\rm ann} \nu \rangle \simeq 3 \times 10^{-26} \ {\rm cm}^3 \, {\rm s}^{-1}$$



Assuming the annihilation process consists of two weak interaction vertices with the SU(2)<sub>L</sub> gauge coupling  $g \simeq 0.64$ , for  $m_{\chi} \sim O(\text{TeV})$  we have

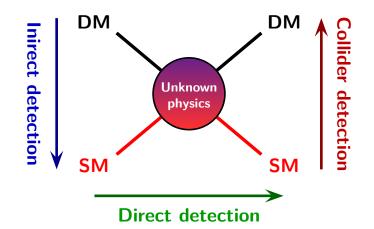
$$\langle \sigma_{\rm ann} \nu \rangle \sim \frac{g^4}{16\pi^2 m_{\chi}^2} \sim \mathcal{O}(10^{-26}) \ {\rm cm}^3 \, {\rm s}^{-1}$$

 $\Rightarrow$  A very attractive class of DM candidates:

#### Weakly interacting massive particles (WIMPs)

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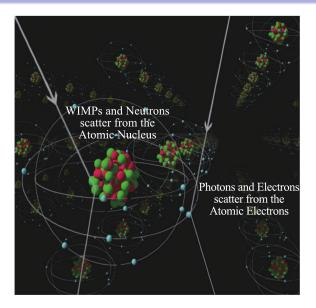




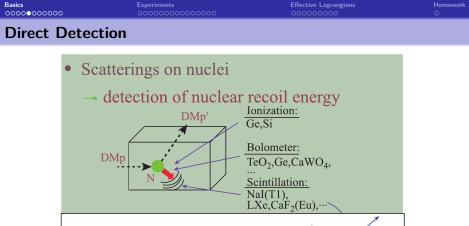
Experiments

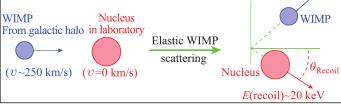
Effective Lagrangian

# WIMP Scattering off Atomic Nuclei



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[Bing-Lin Young, Front. Phys. 12, 121201 (2017)]

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July 2017 6 / 37

Basics	Experiments	Effective Lagrangians	Homework
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## WIMP Velocity Distribution

During the collapse process which formed the Galaxy, WIMP velocities were "thermalized" by fluctuations in the gravitational potential, and WIMPs have a **Maxwell-Boltzmann velocity distribution** in the **Galactic rest frame**:

$$\tilde{f}(\tilde{\mathbf{v}})d^{3}\tilde{v} = \left(\frac{m_{\chi}}{2\pi k_{\rm B}T}\right)^{3/2} \exp\left(-\frac{m_{\chi}\tilde{v}^{2}}{2k_{\rm B}T}\right) d^{3}\tilde{v} = \frac{e^{-\tilde{v}^{2}/v_{0}^{2}}}{\pi^{3/2}v_{0}^{3}}d^{3}\tilde{v}, \quad v_{0}^{2} \equiv \frac{2k_{\rm B}T}{m_{\chi}}$$
$$\langle \tilde{\mathbf{v}} \rangle = \int \tilde{\mathbf{v}}\tilde{f}(\tilde{\mathbf{v}})d^{3}\tilde{v} = \mathbf{0}, \quad \langle \tilde{v}^{2} \rangle = \int \tilde{v}^{2}\tilde{f}(\tilde{\mathbf{v}})d^{3}\tilde{v} = \frac{3}{2}v_{0}^{2}$$
Speed distribution:  $\tilde{f}(\tilde{v})d\tilde{v} = \frac{4\tilde{v}^{2}}{\sqrt{\pi}v_{0}^{3}}e^{-\tilde{v}^{2}/v_{0}^{2}}d\tilde{v}$ 

For an **isothermal** halo, the local value of  $v_0$ equals to the **rotational speed of the Sun**:  $v_0 = v_{\odot} \simeq 220 \text{km/s}$ 

[Binney & Tremaine, Galactic Dynamics, Chapter 4]



[Credit: ESO/L. Calçada]

**Velocity dispersion:** 
$$\sqrt{\langle \tilde{v}^2 \rangle} = \sqrt{3/2} v_0 \simeq 270 \text{km/s}$$

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July 2017 7 / 37

Basics 000000●0000	Experiments	Effective Lagrangians	
Earth Rest Frame	2		

The WIMP velocity distribution  $f(\mathbf{v})$  seen by an observer on the Earth can be derived via **Galilean transformation** 

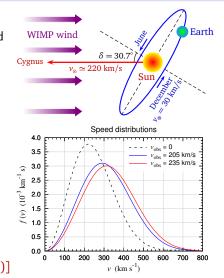
$$\tilde{\mathbf{v}} = \mathbf{v} + \mathbf{v}_{obs}, \quad \mathbf{v}_{obs} = \mathbf{v}_{\odot} + \mathbf{v}_{\oplus}$$

Velocity distribution:  $f(\mathbf{v}) = \tilde{f}(\mathbf{v} + \mathbf{v}_{obs})$ Speed distribution:

$$f(v)dv = \frac{4v^2}{\sqrt{\pi}v_0^3} \exp\left(-\frac{v^2 + v_{obs}^2}{v_0^2}\right)$$
$$\times \frac{v_0^2}{2vv_{obs}} \sinh\left(\frac{2vv_{obs}}{v_0^2}\right)dv$$

Since  $v_\oplus \ll v_\odot$ , we have ( $\omega = 2\pi/{
m year}$ )

$$v_{obs}(t) \simeq v_{\odot} + v_{\oplus} \sin \delta \cos[\omega(t - t_0)]$$
  
$$\simeq 220 \text{ km/s} + 15 \text{ km/s} \cdot \cos[\omega(t - t_0)]$$



⇒ Annual modulation signal peaked on June 2 [Freese et al., PRD 37, 3388 (1988)]

Basics 0000000●000	Experiments	Effective Lagrangians	Homework O
Nuclear F	Recoil		
$\frac{1}{2}m_{\chi}v^{2}$ Momentu	m conservation:	IMP Nucleus $\chi$ $\chi$ $\nu$ $A$ $\theta_{\chi}$	ν <sub>χ</sub>
$\int_{\chi}^{\chi} m_{\chi} v_{\chi}$	$\chi v_{\chi} \cos \theta_{\chi} + m_A v_R \cos \theta_R$ $\sin \theta_{\chi} = m_A v_R \sin \theta_R$ velocity $v_R = \frac{2m_{\chi} v \cos \theta_R}{m_{\chi} + m_A}$		$\theta_{\rm R}$ $\nu_{\rm R}$
$\Rightarrow$ Recoil	momentum (momentum tra	ansfer) $q_{\rm R} = m_A v_{\rm R} = 2\mu_{\chi A} v \cos \theta$	) <sub>R</sub>
Reduced	<b>mass</b> of the $\chi A$ system $\mu_{\chi A} \equiv$	$= \frac{m_{\chi}m_{A}}{m_{\chi} + m_{A}} = \begin{cases} m_{A}, & \text{for } m_{\chi} \gg \\ \frac{1}{2}m_{\chi}, & \text{for } m_{\chi} \approx \\ m_{\chi}, & \text{for } m_{\chi} \ll \end{cases}$	$m_A = m_A$

Forward scattering  $(\theta_R = 0) \Rightarrow$  maximal momentum transfer  $q_R^{max} = 2\mu_{\chi A} v$ 

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Basics 0000000●000	Experiments	Effective Lagrangians	Homework O	
Nuclear Re	ecoil			
Energy cons	servation:		ν	
$\frac{1}{2}m_{\chi}v^2 =$	$= \frac{1}{2}m_{\chi}v_{\chi}^{2} + \frac{1}{2}m_{A}v_{R}^{2}$	o Nucleus	X	
Momentum	conservation: $\chi^{\text{WIMH}}$	A		
$m_{\chi}v = m_{\chi}v$	$v_{\chi} \cos \theta_{\chi} + m_A v_R \cos \theta_R$	$\rightarrow$ $\rho_{\chi}$		
$m_{\chi}v_{\chi}$ si	$n \theta_{\chi} = m_A v_R \sin \theta_R$		$\theta_{\rm R}$	
$\Rightarrow$ Recoil ve	elocity $v_{\rm R} = \frac{2m_{\chi}v\cos\theta_{\rm R}}{m_{\chi}+m_A}$	A	$\nu_{\rm R}$	
$\Rightarrow$ Recoil n	nomentum (momentum transf	fer) $\mathbf{q}_{\mathrm{R}} = m_A v_{\mathrm{R}} = 2\mu_{\chi A} v \cos \theta$	$\theta_{ m R}$	
$\Rightarrow \text{ Kinetic energy of the recoiled nucleus } E_{\text{R}} = \frac{q_{\text{R}}^2}{2m_A} = \frac{2\mu_{\chi A}^2}{m_A} \nu^2 \cos^2 \theta_{\text{R}}$				
	As $\nu \sim 10^{-3}c$ , for $m_{\chi} = m_A c$	$\simeq 100~{ m GeV}$ and $ heta_{ m R}=$ 0,		
	$q_{\rm R} = m_\chi \nu \sim 100$ MeV, E	$_{\rm R} = \frac{1}{2} m_{\chi} v^2 \sim 50 \text{ keV}$		

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July 2017 9 / 37

Basics 00000000●00	Experiments	Effective Lagrangians	Homework O
Event Rate			

Event rate per unit time per unit energy interval:

$$\frac{dR}{dE_{\rm R}} = N_A \frac{\rho_{\oplus}}{m_{\chi}} \int_{\nu_{\rm min}}^{\nu_{\rm max}} d^3 \nu f(\mathbf{v}) \nu \frac{d\sigma_{\chi A}}{dE_{\rm R}}$$

Astrophysics factors Particle physics factors Detector factors

#### N<sub>A</sub>: target nucleus number

 $\rho_{\oplus} \simeq 0.4 \text{ GeV/cm}^3$ : DM mass density around the Earth  $(\rho_{\oplus}/m_{\chi} \text{ is the DM particle number density around the Earth})$  $\sigma_{\chi A}$ : DM-nucleus scattering cross section

Minimal velocity  $v_{\min} = \left(\frac{m_A E_R^{\text{th}}}{2\mu_{\chi A}^2}\right)^{1/2}$ : determined by the detector threshold of nuclear recoil energy,  $E_R^{\text{th}}$ 

Maximal velocity  $v_{max}$ : determined by the DM escape velocity  $v_{esc}$ 

 $\left(\nu_{esc}\simeq 544~\text{km/s}~\text{[Smith et al., MNRAS 379, 755]}\right)$ 

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# **Cross Section Dependence on Nucleus Spin**

There are two kinds of DM-nucleus scattering

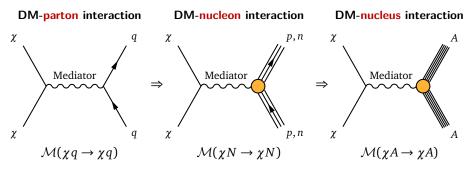
**Spin-independent (SI)** cross section:  $\sigma_{\chi A}^{SI} \propto \mu_{\chi A}^2 [ZG_p + (A-Z)G_n]^2$ **Spin-dependent (SD)** cross section:  $\sigma_{\chi A}^{SD} \propto \mu_{\chi A}^2 \frac{J_A + 1}{J_A} (S_p^A G'_p + S_n^A G'_n)^2$ 

Nucleus properties: mass number A, atomic number Z, spin  $J_A$ , expectation value of the proton (neutron) spin content in the nucleus  $S_p^A(S_n^A)$  $G_p^{(\prime)}$  and  $G_n^{(\prime)}$ : DM effective couplings to the proton and the neutron

- $Z \simeq A/2 \Rightarrow \sigma_{\chi A}^{SI} \propto A^2[(G_p + G_n)/2]^2$ Strong coherent enhancement for heavy nuclei
- Spins of nucleons tend to **cancel out** among themselves:
  - $S_N^A \simeq 1/2$  (N = p or n) for a nucleus with an odd number of N
  - $S_N^A \simeq 0$  for a nucleus with an even number of N

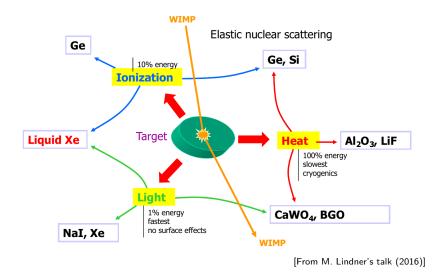


#### Three Levels of Interaction



- As a variety of target nuclei are used in direct detection experiments, results are usually compared with each other at the **DM-nucleon level**
- The DM-nucleon level is related to the DM-parton level via form factors. which describe the probabilities of finding partons inside nucleons
- Relevant partons involve not only valence quarks, but also sea quarks and gluons

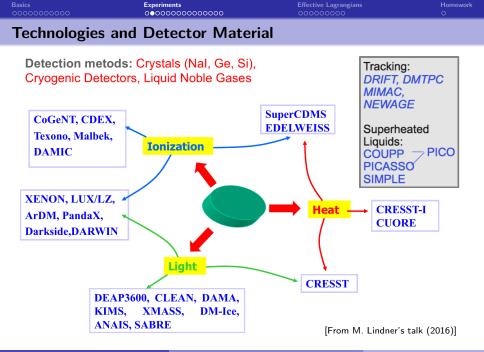




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July 2017 13 / 37



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Dark Matter Direct Detection

July 2017 14 / 37

Effective Lagrangians

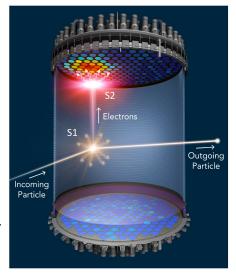
# Example: Dual-phase Xenon Time Projection Chamber

#### Upper: Xenon gas Lower: Liquid Xenon

UV scintillation photons recorded by photomultiplier tube (PMT) arrays on top and bottom

- **Primary scintillation (S1):** Scintillation light promptly emitted from the interaction vertex
- Secondary scintillation (S2): lonization electrons emitted from the interaction are drifted to the surface and into the gas, where they emit proportional scintillation light

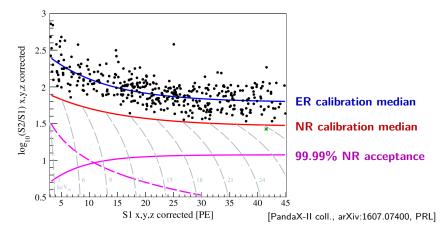
Experiments: XENON, LUX, PandaX



[From A. Cottle's talk (2017)]



- PandaX-II Real Data: S1 versus S2
  - S1 and S2: characterized by numbers of photoelectrons (PEs) in PMTs
  - The  $\gamma$  background, which produces electron recoil (ER) events, can be distinguished from nuclear recoil (NR) events using the S2-to-S1 ratio



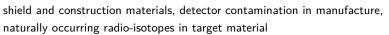
Basics Experiments	Effective Lagrangians	Homework
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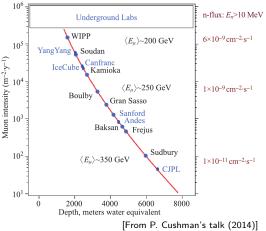
# Backgrounds

# Background suppression: Deep underground

Shielded environments

- Cosmogenic backgrounds:
  - Cosmic rays and secondary reactions
  - Activation products in shields and detectors
- Radiogenic backgrounds:
  - External natural radioactivity: walls, structures of site, radon
  - Internal radioactivity:









[Yue et al., arXiv:1602.02462]

#### Experiments: CDEX, PandaX

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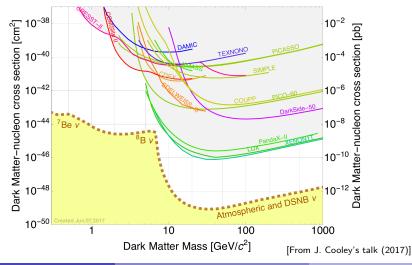
July 2017 18 / 37

 Basics
 Experiments
 Effective Lagrangians
 Homework

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# **Exclusion Limits for SI Scattering**

For **SI** scattering, the coherent enhancement allows us to treat protons and neutrons as the same species, "nucleons"



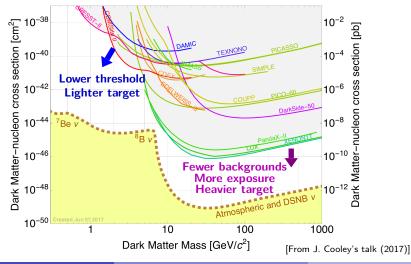
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 Basics
 Experiments
 Effective Lagrangians
 Homework

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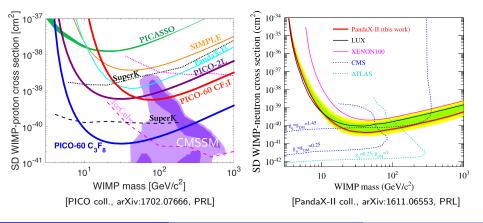


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# **Exclusion Limits for SD Scattering**

- For **SD** scattering, specific detection material usually has very different sensitivities to WIMP-proton and WIMP-neutron cross sections
- As there is no coherent enhancement for SD scattering, the sensitivity is **lower** than the SI case by **several orders of magnitude**

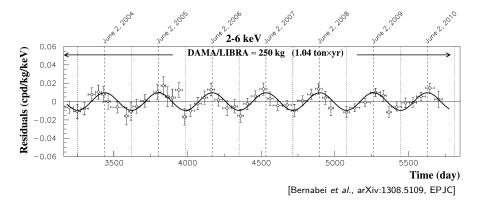


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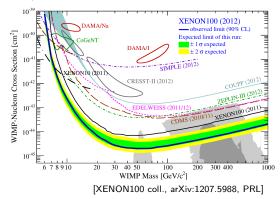
# DAMA/LIBRA Annual Modulation "Signal"

- Highly radio-pure scintillating Nal(TI) crystals at Gran Sasso, Italy
   Annual modulation signal observed over 14 cycles at 9.3σ significance
- No background/signal discrimination



#### DAMA/LIBRA Annual Modulation "Signal"

- Highly radio-pure scintillating Nal(TI) crystals at Gran Sasso, Italy
- <sup>(2)</sup> Annual modulation signal observed over 14 cycles at 9.3 $\sigma$  significance
- No background/signal discrimination



Favored regions excluded by other direct detection experiments

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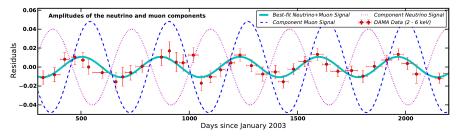
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July 2017 21 / 37

# Other Sources for DAMA/LIBRA Signal

The DAMA/LIBRA signal might be composed of neutrons liberated in the material surrounding the detector by two sources [Davis, arXiv:1407.1052, PRL]

- Atmospheric muons: flux depends on the temperature of the atmosphere, peaked on June 21st
- Solar neutrinos: flux depends on the distance between the Earth and the Sun, peaked on January 4th



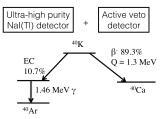
**Objection:** Klinger & Kudryavtsev, "muon-induced neutrons do not explain the DAMA data," arXiv:1503.07225, PRL

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Basics 0000000000	Experiments 000000000●0000	Effective Lagrangians	
Further Test:	SABRE Project		

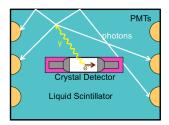
SABRE: Sodium iodide with Active Background REjection

- Complementary tests in **both hemispheres**: one part in Gran Sasso (Italy) and one part in Stawell (Australia)
- Developing **low background** scintillating NaI(TI) crystals that exceed the radio-purity of DAMA/LIBRA
- A well-shielded active veto to reduce internal and external backgrounds



 $^{40}$ K $\rightarrow$  $^{40}$ Ar, ~11% branch ratio

- 3 keV K shell X-ray, Auger e<sup>-</sup>
- Background at ~3 keV if γ escapes

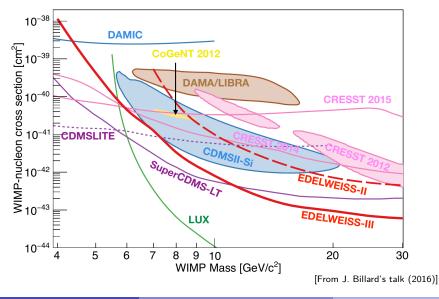


1.46MeV  $\gamma$  can be detected by a veto. <sup>40</sup>K background can be rejected.

[From E. Barberio's talk]

	Experiments	Effective Lagrangians	
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#### Low Mass Situation



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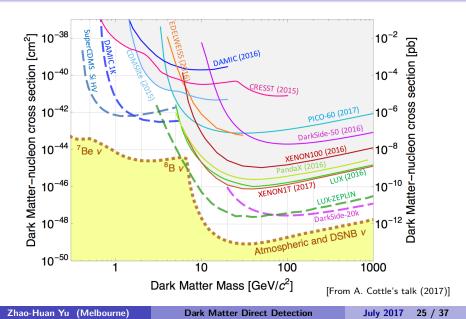
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July 2017 24 / 37

Experiments

Effective Lagrangian

# **Near Future Prospect**



# Neutrino Backgrounds

Direct detection experiments will be sensitive to coherent neutrino-nucleus scattering (CNS) due to astrophysical neutrinos [Billard et al., arXiv:1307.5458, PRD]

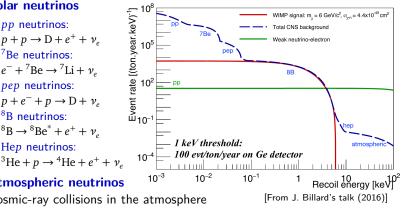
- Solar neutrinos
  - pp neutrinos:
  - <sup>7</sup>Be neutrinos:  $e^- + {}^7\text{Be} \rightarrow {}^7\text{Li} + \nu_a$
  - *pep* neutrinos:  $p + e^- + p \rightarrow D + \nu_e$
  - <sup>8</sup>B neutrinos:  $^{8}B \rightarrow ^{8}Be^{*} + e^{+} + \gamma$
  - Hep neutrinos:  $^{3}\text{He} + p \rightarrow ^{4}\text{He} + e^{+} + \nu_{e}$
- Atmospheric neutrinos

Cosmic-ray collisions in the atmosphere

# Diffuse supernova neutrino background (DSNB)

All supernova explosions in the past history of the Universe

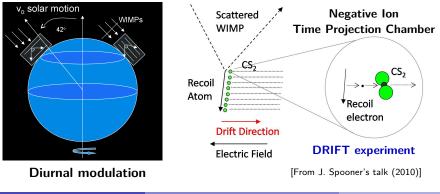
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Going beyond the	Neutrino Floor		
Basics 0000000000	Experiments	Effective Lagrangians	

Possible ways to reduce the impact of neutrino backgrounds:

- Reduction of systematic uncertainties on neutrino fluxes
- Utilization of different target nuclei [Ruppin et al., arXiv:1408.3581, PRD]
- Measurement of annual modulation [Davis, arXiv:1412.1475, JCAP]
- Measurement of nuclear recoil direction [O'Hare, et al., arXiv:1505.08061, PRD]

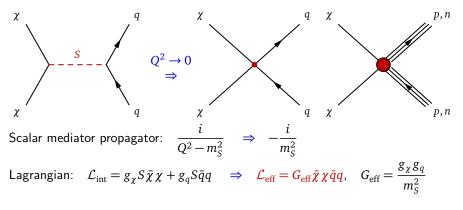


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#### Zero Momentum Transfer Limit

- As the momentum transfer (q<sub>R</sub> in the nucleus rest frame) is typically much smaller than the underlying energy scale (*e.g.*, mediator mass), the zero momentum transfer limit is a good approximation for calculation
- In this limit, the mediator field can be integrated out, and the interaction can be described by effective operators in effective field theory



 Basics
 Experiments
 Effective Lagrangians
 Homework

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#### **Effective Operators for DM-nucleon interactions**

Assuming the DM particle is a **Dirac fermion**  $\chi$  and using **Dirac fields** p and n to describe the proton and the neutron, the effective Lagrangian reads

 $\mathcal{L}_{\mathrm{eff},N} = \sum_{N=p,n} \sum_{ij} G_{N,ij} \bar{\chi} \Gamma^i \chi \bar{N} \Gamma_j N, \quad \Gamma^i, \Gamma^j \in \{1, i\gamma_5, \gamma^\mu, \gamma^\mu \gamma_5, \sigma^{\mu\nu}\}$ 

[Bélanger et al., arXiv:0803.2360, Comput.Phys.Commun.]

- Lorentz indices in  $\Gamma^i$  and  $\Gamma_i$  should be contracted in pair
- Effective couplings  $G_{N,ij}$  have a mass dimension of -2:  $[G_{N,ij}] = [Mass]^{-2}$
- $\bar{\chi}\chi\bar{N}N$  and  $\bar{\chi}\gamma^{\mu}\chi\bar{N}\gamma_{\mu}N$  lead to **SI** DM-nucleon scattering
- $\bar{\chi}\gamma^{\mu}\gamma_5\chi\bar{N}\gamma_{\mu}\gamma_5N$  and  $\bar{\chi}\sigma^{\mu\nu}\chi\bar{N}\sigma_{\mu\nu}N$  lead to **SD** DM-nucleon scattering
- The following operators lead to scattering cross sections  $\sigma_{\chi N} \propto |Q^2|$ :  $\bar{\chi} i \gamma_5 \chi \bar{N} i \gamma_5 N, \ \bar{\chi} \chi \bar{N} i \gamma_5 N, \ \bar{\chi} i \gamma_5 \chi \bar{N} N, \ \bar{\chi} \gamma^{\mu} \chi \bar{N} \gamma_{\mu} \gamma_5 N, \ \bar{\chi} \gamma^{\mu} \gamma_5 \chi \bar{N} \gamma_{\mu} N$
- For a Majorana fermion  $\chi$  instead, we have  $\bar{\chi}\gamma^{\mu}\chi = 0$  and  $\bar{\chi}\sigma^{\mu\nu}\chi = 0$ , and hence the related operators vanish

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### Higgs Portal for Majorana Fermionic DM

Interactions for a Majorana fermion  $\chi$ , the SM Higgs boson *h*, and quarks *q*:

$$\mathcal{L}_{\rm DM} \supset \frac{1}{2} g_{\chi} h \bar{\chi} \chi$$
$$\mathcal{L}_{\rm SM} \supset -\sum_{q} \frac{m_{q}}{v} h \bar{q} q, \quad q = d, u, s, c, b, t$$

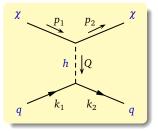
The amplitude for 
$$\chi(p_1) + q(k_1) \rightarrow \chi(p_2) + q(k_2)$$
:  
 $i\mathcal{M} = ig_{\chi}\bar{u}(p_2)u(p_1)\frac{i}{Q^2 - m_h^2} \left(-i\frac{m_q}{\nu}\right)\bar{u}(k_2)u(k_1)$ 

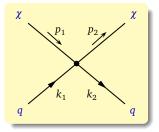
Zero momentum transfer  $~\Downarrow~ Q^2 = (k_2 - k_1)^2 \rightarrow 0$ 

$$i\mathcal{M} = -i\frac{g_{\chi}m_q}{\nu m_h^2}\bar{u}(p_2)u(p_1)\bar{u}(k_2)u(k_1)$$

$$\downarrow$$

$$\mathcal{L}_{\text{eff},q} = \sum_{q} G_{\text{S},q}\bar{\chi}\chi\bar{q}q, \quad G_{\text{S},q} = -\frac{g_{\chi}m_q}{2\nu m_h^2}$$





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#### Effective Lagrangian: Scalar Type

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Scalar-type effective Lagrangian for a spin-1/2 fermion  $\chi$ :

$$\mathcal{L}_{S,q} = \sum_{q} G_{S,q} \bar{\chi} \chi \bar{q} q \quad \Rightarrow \quad \mathcal{L}_{S,N} = \sum_{N=p,n} G_{S,N} \bar{\chi} \chi \bar{N} N$$
$$G_{S,N} = m_N \left( \sum_{q=u,d,s} \frac{G_{S,q}}{m_q} f_q^N + \sum_{q=c,b,t} \frac{G_{S,q}}{m_q} f_Q^N \right)$$

The second term accounts for DM interactions with gluons through loops of heavy quarks (c, b, and t):  $f_Q^N = \frac{2}{27} \left(1 - \sum_{q=u,d,s} f_q^N\right)$ 

Form factor  $f_q^N$  is the contribution of q to  $m_N$ :  $\langle N | m_q \bar{q} q | N \rangle = f_q^N m_N$  $f_u^P \simeq 0.020, \quad f_d^P \simeq 0.026, \quad f_u^n \simeq 0.014, \quad f_d^n \simeq 0.036, \quad f_s^P = f_s^n \simeq 0.118$ [Ellis *et al.*, arXiv:hep-ph/0001005, PLB]

The scalar type induces SI DM-nucleon scattering with a cross section of

$$\sigma_{\chi N}^{\rm SI} = \frac{n_{\chi}}{\pi} \mu_{\chi N}^2 G_{\rm S,N}^2, \quad \mu_{\chi N} \equiv \frac{m_{\chi} m_N}{m_{\chi} + m_N}, \quad n_{\chi} = \begin{cases} 1, & \text{for Dirac fermion } \chi \\ 4, & \text{for Majorana fermion } \chi \end{cases}$$

#### Z Portal for Majorana Fermionic DM

Interactions for a Majorana fermion  $\chi$ , the Z boson, and quarks q:

$$\mathcal{L}_{\rm DM} \supset \frac{1}{2} g_{\chi} Z_{\mu} \bar{\chi} \gamma^{\mu} \gamma_5 \chi, \quad \mathcal{L}_{\rm SM} \supset \frac{g}{2c_{\rm W}} Z_{\mu} \sum_{q} \bar{q} \gamma^{\mu} (g_{\rm V}^{q} - g_{\rm A}^{q} \gamma_5) q$$
$$g_{\rm V}^{u_i} = \frac{1}{2} - \frac{4}{3} s_{\rm W}^2, \quad g_{\rm V}^{d_i} = -\frac{1}{2} + \frac{2}{3} s_{\rm W}^2, \quad g_{\rm A}^{u_i} = \frac{1}{2} = -g_{\rm A}^{d_i}, \quad c_{\rm W} \equiv \cos \theta_{\rm W}, \quad s_{\rm W} \equiv \sin \theta_{\rm W}$$

Z boson propagator 
$$\frac{-i}{Q^2 - m_Z^2} \left( g_{\mu\nu} - \frac{Q_\mu Q_\nu}{m_Z^2} \right) \xrightarrow{Q^2 \to 0} \frac{i}{m_Z^2} g_{\mu\nu}$$

Effective Lagrangian in the zero momentum transfer limit:

$$\mathcal{L}_{\text{eff},q} = \sum_{q} \bar{\chi} \gamma^{\mu} \gamma_{5} \chi (G_{\text{A},q} \bar{q} \gamma_{\mu} \gamma_{5} q + G_{\text{AV},q} \bar{q} \gamma_{\mu} q), \quad G_{\text{A},q} = \frac{g_{\chi} g g_{\text{A}}^{q}}{4c_{\text{W}} m_{Z}^{2}}$$

 $G_{\rm AV,q} = -\frac{g_{\chi}gg_{\rm V}^q}{4c_{\rm W}m_Z^2}$  leads to  $\sigma_{\chi N} \propto |Q^2|$  and can be neglected for direct detection

#### Effective Lagrangian: Axial Vector Type

Axial-vector-type effective Lagrangian for a spin-1/2 fermion  $\chi$ :

$$\begin{aligned} \mathcal{L}_{\mathrm{A},q} &= \sum_{q} G_{\mathrm{A},q} \bar{\chi} \gamma^{\mu} \gamma_{5} \chi \bar{q} \gamma_{\mu} \gamma_{5} q \quad \Rightarrow \quad \mathcal{L}_{\mathrm{A},N} = \sum_{N=p,n} G_{\mathrm{A},N} \bar{\chi} \gamma^{\mu} \gamma_{5} \chi \bar{N} \gamma_{\mu} \gamma_{5} N \\ G_{\mathrm{A},N} &= \sum_{q=u,d,s} G_{\mathrm{A},q} \Delta_{q}^{N}, \quad 2 \Delta_{q}^{N} s_{\mu} \equiv \langle N | \bar{q} \gamma_{\mu} \gamma_{5} q | N \rangle \end{aligned}$$

**Form factors**  $\Delta_q^N$  account the contributions of quarks and anti-quarks to the nucleon spin vector  $s_{\mu}$ , and can be extracted from lepton-proton scattering data:

$$\begin{split} \Delta^p_u = \Delta^n_d \simeq 0.842, \quad \Delta^p_d = \Delta^n_u \simeq -0.427, \quad \Delta^p_s = \Delta^n_s \simeq -0.085 \\ \text{[HERMES coll., arXiv:hep-ex/0609039, PRD]} \end{split}$$

Neutron form factors are related to proton form factors by isospin symmetry

The axial vector type induces **SD** DM-nucleon scattering:

$$\sigma_{\chi N}^{\rm SD} = \frac{3n_{\chi}}{\pi} \mu_{\chi N}^2 G_{\rm A,N}^2, \quad n_{\chi} = \begin{cases} 1, & \text{for Dirac fermion } \chi \\ 4, & \text{for Majorana fermion } \chi \end{cases}$$

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Basics	Experiments	Effective Lagrangians	Homework

#### Z Portal for Complex Scalar DM

Interactions for a **complex scalar**  $\chi$ , the *Z* **boson**, and quarks *q*:

$$\mathcal{L}_{\rm DM} \supset g_{\chi} Z_{\mu} (\chi^* i \overleftrightarrow{\partial^{\mu}} \chi)$$

$$\mathcal{L}_{\rm SM} \supset \frac{g}{2c_{\rm W}} Z_{\mu} \sum_{q} \bar{q} \gamma^{\mu} (g_{\rm V}^{q} - g_{\rm A}^{q} \gamma_{5}) q$$

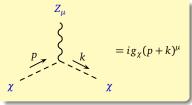
$$i\mathcal{M} = ig_{\chi} (p_{1} + p_{2})^{\mu} \frac{-i(g_{\mu\nu} - Q_{\mu}Q_{\nu}/m_{Z}^{2})}{Q^{2} - m_{Z}^{2}} \chi^{2}$$

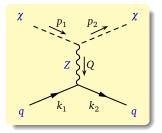
$$\times i \frac{g}{2c_{\rm W}} \bar{u}(k_{2}) \gamma^{\nu} (g_{\rm V}^{q} - g_{\rm A}^{q} \gamma_{5}) u(k_{1})$$

$$\frac{Q^{2} \rightarrow 0}{\longrightarrow} -i \frac{g_{\chi}g}{2c_{\rm W}m_{Z}^{2}} (p_{1} + p_{2})^{\mu} \bar{u}(k_{2}) \gamma_{\mu} (g_{\rm V}^{q} - g_{\rm A}^{q} \gamma_{5}) u(k_{1})$$

$$\mathcal{L}_{\rm eff,q} = \sum_{q} (\chi^* i \overleftrightarrow{\partial^{\mu}} \chi) (F_{{\rm V},q} \bar{q} \gamma_{\mu} q + F_{{\rm VA},q} \bar{q} \gamma_{\mu} \gamma_{5} q)$$

$$F_{\mathrm{V},q} = -\frac{g_{\chi}gg_{\mathrm{V}}^{q}}{2c_{\mathrm{W}}m_{Z}^{2}}, \quad F_{\mathrm{VA},q} = \frac{g_{\chi}gg_{\mathrm{A}}^{q}}{2c_{\mathrm{W}}m_{Z}^{2}} (\Rightarrow \sigma_{\chi N} \propto |Q^{2}|)$$





Basics	Experiments	Effective Lagrangians	
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Effective	Lagrangian: Vector Type		

The sector-type effective Lagrangian for a complex scalar  $\chi$ :

$$\mathcal{L}_{\mathrm{V},q} = \sum_{q} F_{\mathrm{V},q}(\chi^* i \overleftrightarrow{\partial^{\mu}} \chi) \bar{q} \gamma_{\mu} q \quad \Rightarrow \quad \mathcal{L}_{\mathrm{A},N} = \sum_{N=p,n} F_{\mathrm{V},N}(\chi^* i \overleftrightarrow{\partial^{\mu}} \chi) \bar{N} \gamma_{\mu} N$$

The relation between  $F_{V,N}$  and  $F_{V,q}$  reflects the valence quark numbers in N:

$$F_{V,p} = 2F_{V,u} + F_{V,d}, \quad F_{V,n} = F_{V,u} + 2F_{V,d}$$

The vector type induces **SI** DM-nucleon scattering:  $\sigma_{\chi N}^{SI} = \frac{1}{\pi} \mu_{\chi N}^2 F_{V,N}^2$ 

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$$\mathcal{L}_{\mathrm{V},q} = \sum_{q} G_{\mathrm{V},q} \bar{\chi} \gamma^{\mu} \chi \bar{q} \gamma_{\mu} q \quad \Rightarrow \quad \mathcal{L}_{\mathrm{A},N} = \sum_{N=p,n} G_{\mathrm{V},N} \bar{\chi} \gamma^{\mu} \chi \bar{N} \gamma_{\mu} N$$

It also induces **SI** DM-nucleon scattering:

$$\sigma_{\chi N}^{\rm SI} = \frac{1}{\pi} \mu_{\chi N}^2 G_{\rm V,N}^2, \quad G_{\rm V,p} = 2G_{\rm V,u} + G_{\rm V,d}, \quad G_{\rm V,n} = G_{\rm V,u} + 2G_{\rm V,d}$$

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Basics	Experiments	Effective Lagrangians	
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#### **Effective Operators for DM-quark Interactions**

	Spin-1/2 DM	Spin-0 DM
SI	$ar{\chi}\chiar{q}q,\ ar{\chi}\gamma^\mu\chiar{q}\gamma_\mu q$	$\chi^*\chi \bar{q}q, \ (\chi^*i\overleftrightarrow{\partial^\mu}\chi)\bar{q}\gamma_\mu q$
SD	$ar{\chi}\gamma^{\mu}\gamma_5\chiar{q}\gamma_{\mu}\gamma_5 q,\ ar{\chi}\sigma^{\mu u}\chiar{q}\sigma_{\mu u}q$	
$\sigma_{\chi N} \propto  Q^2 $	$ar{\chi}i\gamma_5\chiar{q}i\gamma_5q, \ ar{\chi}\chiar{q}i\gamma_5q \ ar{\chi}i\gamma_5\chiar{q}q, \ ar{\chi}\gamma^{\mu}\chiar{q}\gamma_{\mu}\gamma_5q \ ar{\chi}\gamma^{\mu}\gamma_5\chiar{q}\gamma_{\mu}q, \ ar{x}^{\mu\nu ho\sigma}ar{\chi}\sigma^{\mu\nu}\chiar{q}\sigma_{ ho\sigma}q$	$\chi^* \chi \bar{q} i \gamma_5 q$ $(\chi^* i \overleftrightarrow{\partial^\mu} \chi) \bar{q} \gamma_\mu \gamma_5 q$
	Spin-3/2 DM	Spin-1 DM
SI	$ar{\chi}^{\mu}\chi_{\mu}ar{q}q,\ \ ar{\chi}^{ u}\gamma^{\mu}\chi_{ u}ar{q}\gamma_{\mu}q$	$\chi^*_{\mu}\chi^{\mu}\bar{q}q, \ (\chi^*_{\nu}i\overleftrightarrow{\partial^{\mu}}\chi^{\nu})\bar{q}\gamma_{\mu}q$
SD	$ar{\chi}^{ u}\gamma^{\mu}\gamma_{5}\chi_{ u}ar{q}\gamma_{\mu}\gamma_{5}q, \ \ ar{\chi}^{ ho}\sigma^{\mu u}\chi_{ ho}ar{q}\sigma_{\mu u}q$ $i(ar{\chi}^{\mu}\chi^{ u}-ar{\chi}^{ u}\chi^{\mu})ar{q}\sigma_{\mu u}q$	$i(\chi_{\mu}^{*}\chi_{\nu} - \chi_{\nu}^{*}\chi_{\mu})\bar{q}\sigma^{\mu\nu}q$ $\varepsilon^{\mu\nu\rho\sigma}(\chi_{\mu}^{*}\overleftrightarrow{\partial_{\nu}}\chi_{\rho})\bar{q}\gamma_{\sigma}\gamma_{5}q$
$\sigma_{\chi N} \propto  Q^2 $	$\begin{split} \bar{\chi}^{\mu} i\gamma_{5} \chi_{\mu} \bar{q} i\gamma_{5} q,  \bar{\chi}^{\mu} \chi_{\mu} \bar{q} i\gamma_{5} q \\ \bar{\chi}^{\mu} i\gamma_{5} \chi_{\mu} \bar{q} q,  \bar{\chi}^{\nu} \gamma^{\mu} \chi_{\nu} \bar{q} \gamma_{\mu} \gamma_{5} q \\ \bar{\chi}^{\mu} \gamma^{\mu} \gamma_{5} \chi_{\nu} \bar{q} \gamma_{\mu} q,  \varepsilon^{\mu\nu\rho\sigma} i (\bar{\chi}_{\mu} \chi_{\nu} - \bar{\chi}_{\nu} \chi_{\mu}) \bar{q} \sigma_{\rho\sigma} q \\ \varepsilon^{\mu\nu\rho\sigma} \bar{\chi}^{\alpha} \sigma_{\mu\nu} \chi_{\alpha} \bar{q} \sigma_{\rho\sigma} q,  (\bar{\chi}^{\mu} \gamma_{5} \chi^{\nu} - \bar{\chi}^{\nu} \gamma_{5} \chi^{\mu}) \bar{q} \sigma_{\mu\nu} q \\ \varepsilon^{\mu\nu\rho\sigma} (\bar{\chi}_{\mu} \gamma_{5} \chi_{\nu} - \bar{\chi}_{\nu} \gamma_{5} \chi_{\mu}) \bar{q} \sigma_{\rho\sigma} q \end{split}$	$\begin{split} \chi^{*}_{\mu} \chi^{\mu} \bar{q} i \gamma_{5} q \\ (\chi^{*}_{\nu} i \overleftrightarrow{\partial^{\mu}} \chi^{\nu}) \bar{q} \gamma_{\mu} \gamma_{5} q \\ \varepsilon^{\mu\nu\rho\sigma} (\chi^{*}_{\mu} \overleftrightarrow{\partial_{\nu}} \chi_{\rho}) \bar{q} \gamma_{\sigma} q \\ \varepsilon^{\mu\nu\rho\sigma} i (\chi^{*}_{\mu} \chi_{\nu} - \chi^{*}_{\nu} \chi_{\mu}) \bar{q} \sigma_{\rho\sigma} q \end{split}$

[Zheng, ZHY, Shao, Bi, Li, Zhang, arXiv:1012.2022, NPB; ZHY, Zheng, Bi, Li, Yao, Zhang, arXiv:1112.6052, NPB; Ding & Liao, arXiv:1201.0506, JHEP]

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Basics 0000000000	Experiments	Effective Lagrangians	Homework •
Homework			

- **1** Derive the speed distribution f(v) in Page 8 from  $f(v) = \tilde{f}(v + v_{obs})$
- Calculate the normalization factor for the velocity distribution *f*(*v*) in Page 7 if the escape velocity v<sub>esc</sub> is taken into account
- Examine the conservation of electric charge, lepton number, and baryon number for the reactions producing solar neutrinos in Page 26
- Evaluate the values of DM-nucleon effective couplings  $G_{S,p}$  ( $G_{A,p}$ ) and  $G_{S,n}$  ( $G_{A,n}$ ) for the Higgs-portal (Z-portal) model in Page 30 (32) using the values of form factors listed in Page 31 (33)
- Proof the expressions for  $\sigma_{\chi N}^{\rm SI}$  and  $\sigma_{\chi N}^{\rm SD}$  shown in Pages 31, 33, and 35
- Section 20 Examine the hermiticity of the operators tabulated in Page 36