

DM Relic Abundance

If DM particles (χ) were thermally produced in the early Universe, their **relic abundance** would be determined by the annihilation cross section $\langle\sigma_{\text{ann}}v\rangle$:

$$\Omega_{\chi}h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle\sigma_{\text{ann}}v\rangle}$$

Observation value $\Omega_{\chi}h^2 \simeq 0.1$

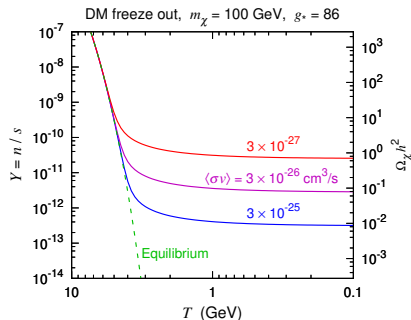
$$\Rightarrow \langle\sigma_{\text{ann}}v\rangle \simeq 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

Assuming the annihilation process consists of two weak interaction vertices with the $SU(2)_L$ gauge coupling $g \simeq 0.64$, for $m_{\chi} \sim \mathcal{O}(\text{TeV})$ we have

$$\langle\sigma_{\text{ann}}v\rangle \sim \frac{g^4}{16\pi^2 m_{\chi}^2} \sim \mathcal{O}(10^{-26}) \text{ cm}^3 \text{ s}^{-1}$$

\Rightarrow A very attractive class of DM candidates:

Weakly interacting massive particles (WIMPs)



Earth Rest Frame

The WIMP velocity distribution $f(\mathbf{v})$ seen by an observer on the Earth can be derived via **Galilean transformation**

$$\tilde{\mathbf{v}} = \mathbf{v} + \mathbf{v}_{\text{obs}}, \quad \mathbf{v}_{\text{obs}} = \mathbf{v}_{\odot} + \mathbf{v}_{\oplus}$$

Velocity distribution: $f(\mathbf{v}) = \tilde{f}(\mathbf{v} + \mathbf{v}_{\text{obs}})$

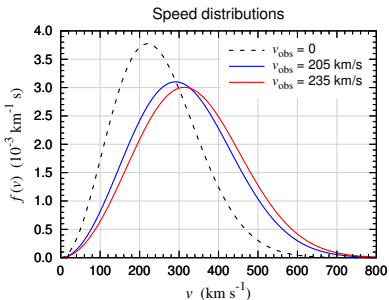
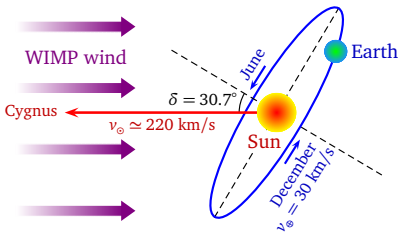
Speed distribution:

$$f(v)dv = \frac{4v^2}{\sqrt{\pi}v_0^3} \exp\left(-\frac{v^2 + v_{\text{obs}}^2}{v_0^2}\right) \times \frac{v_0^2}{2vv_{\text{obs}}} \sinh\left(\frac{2vv_{\text{obs}}}{v_0^2}\right) dv$$

Since $v_{\oplus} \ll v_{\odot}$, we have ($\omega = 2\pi/\text{year}$)

$$\begin{aligned} v_{\text{obs}}(t) &\simeq v_{\odot} + v_{\oplus} \sin \delta \cos[\omega(t - t_0)] \\ &\simeq 220 \text{ km/s} + 15 \text{ km/s} \cdot \cos[\omega(t - t_0)] \end{aligned}$$

⇒ **Annual modulation signal peaked on June 2** [Freese *et al.*, PRD 37, 3388 (1988)]



Nuclear Recoil

Energy conservation:

$$\frac{1}{2}m_\chi v^2 = \frac{1}{2}m_\chi v_\chi^2 + \frac{1}{2}m_A v_R^2$$

Momentum conservation:

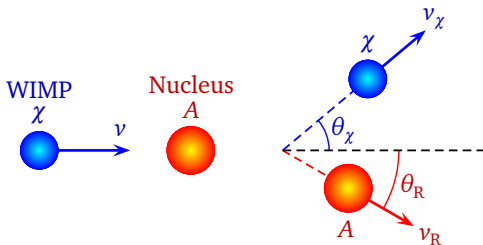
$$m_\chi v = m_\chi v_\chi \cos \theta_\chi + m_A v_R \cos \theta_R$$

$$m_\chi v_\chi \sin \theta_\chi = m_A v_R \sin \theta_R$$

$$\Rightarrow \text{Recoil velocity } v_R = \frac{2m_\chi v \cos \theta_\chi}{m_\chi + m_A}$$

$$\Rightarrow \text{Recoil momentum (momentum transfer) } q_R = m_A v_R = 2\mu_{\chi A} v \cos \theta_\chi$$

Reduced mass of the χA system $\mu_{\chi A} \equiv \frac{m_\chi m_A}{m_\chi + m_A} = \begin{cases} m_A, & \text{for } m_\chi \gg m_A \\ \frac{1}{2}m_\chi, & \text{for } m_\chi = m_A \\ m_\chi, & \text{for } m_\chi \ll m_A \end{cases}$



Forward scattering ($\theta_R = 0$) \Rightarrow maximal momentum transfer $q_R^{\max} = 2\mu_{\chi A} v$

Nuclear Recoil

Energy conservation:

$$\frac{1}{2} m_{\chi} v^2 = \frac{1}{2} m_{\chi} v_{\chi}^2 + \frac{1}{2} m_A v_R^2$$

Momentum conservation:

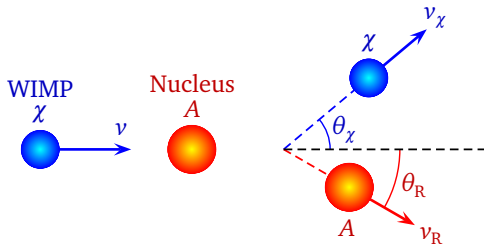
$$m_{\chi} v = m_{\chi} v_{\chi} \cos \theta_{\chi} + m_A v_R \cos \theta_R$$

$$m_{\chi} v_{\chi} \sin \theta_{\chi} = m_A v_R \sin \theta_R$$

$$\Rightarrow \text{Recoil velocity } v_R = \frac{2m_{\chi} v \cos \theta_R}{m_{\chi} + m_A}$$

$$\Rightarrow \text{Recoil momentum (momentum transfer) } q_R = m_A v_R = 2\mu_{\chi A} v \cos \theta_R$$

$$\Rightarrow \text{Kinetic energy of the recoiled nucleus } E_R = \frac{q_R^2}{2m_A} = \frac{2\mu_{\chi A}^2}{m_A} v^2 \cos^2 \theta_R$$



As $v \sim 10^{-3}c$, for $m_{\chi} = m_A \simeq 100 \text{ GeV}$ and $\theta_R = 0$,

$$q_R = m_{\chi} v \sim 100 \text{ MeV}, \quad E_R = \frac{1}{2} m_{\chi} v^2 \sim 50 \text{ keV}$$

Event Rate

Event rate per unit time per unit energy interval:

$$\frac{dR}{dE_R} = N_T \frac{\rho_\oplus}{m_\chi} \int_{v_{\min}}^{v_{\max}} d^3v f(\mathbf{v}) v \frac{d\sigma_{\chi A}}{dE_R}$$

Astrophysics factors
Particle physics factors
Detector factors

N_T : **target nucleus number**

$\rho_\oplus \simeq 0.3 - 0.4 \text{ GeV/cm}^3$: DM **mass density** around the Earth

(ρ_\oplus/m_χ is the DM particle **number density** around the Earth)

$\sigma_{\chi A}$: DM-nucleus **scattering cross section**

Minimal velocity $v_{\min} = \left(\frac{m_A E_R^{\text{th}}}{2\mu_{\chi A}^2} \right)^{1/2}$: determined by the **detector threshold**
of nuclear recoil energy, E_R^{th}

Maximal velocity v_{\max} : determined by the DM **escape velocity** v_{esc}

($v_{\text{esc}} \simeq 544 \text{ km/s}$ [Smith *et al.*, MNRAS 379, 755])

Cross Section Dependence on Nucleus Spin

There are two kinds of DM-nucleus scattering

Spin-independent (SI) cross section: $\sigma_{\chi A}^{\text{SI}} \propto \mu_{\chi A}^2 [Z G_p + (A-Z) G_n]^2$

Spin-dependent (SD) cross section: $\sigma_{\chi A}^{\text{SD}} \propto \mu_{\chi A}^2 \frac{J_A + 1}{J_A} (S_p^A G_p' + S_n^A G_n')^2$

Nucleus properties: mass number A , atomic number Z , spin J_A ,

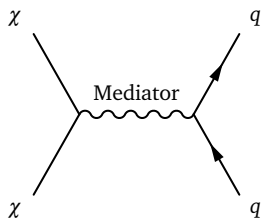
expectation value of the **proton (neutron) spin content** in the nucleus S_p^A (S_n^A)

$G_p^{(\prime)}$ and $G_n^{(\prime)}$: **DM effective couplings** to the proton and the neutron

- $Z \simeq A/2 \Rightarrow \sigma_{\chi A}^{\text{SI}} \propto A^2 [(G_p + G_n)/2]^2$
Strong **coherent enhancement** for **heavy** nuclei
- Spins of nucleons tend to **cancel out** among themselves:
 - $S_N^A \simeq 1/2$ ($N = p$ or n) for a nucleus with an **odd** number of N
 - $S_N^A \simeq 0$ for a nucleus with an **even** number of N

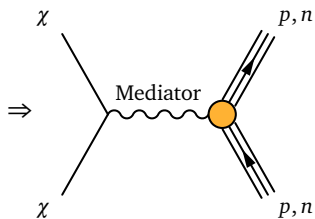
Three Levels of Interaction

DM-parton interaction



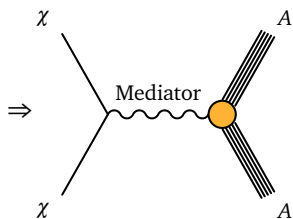
$$\mathcal{M}(\chi q \rightarrow \chi q)$$

DM-nucleon interaction



$$\mathcal{M}(\chi N \rightarrow \chi N)$$

DM-nucleus interaction

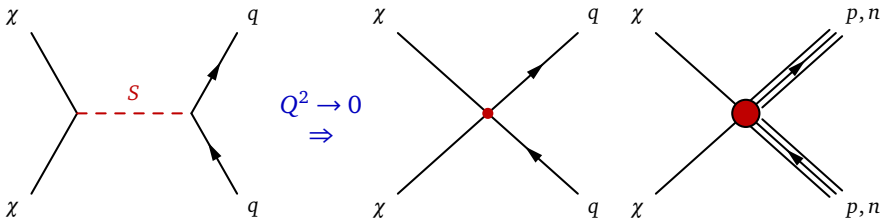


$$\mathcal{M}(\chi A \rightarrow \chi A)$$

- As a variety of target nuclei are used in direct detection experiments, results are usually compared with each other at the **DM-nucleon level**
- The DM-nucleon level is related to the DM-parton level via **form factors**, which describe the probabilities of finding partons inside nucleons
- Relevant partons involve not only valence quarks, but also **sea quarks** and **gluons**

Zero Momentum Transfer Limit

- As the momentum transfer is typically much smaller than the underlying energy scale (e.g., mediator mass), the **zero momentum transfer limit** is a good approximation for calculation
- In this limit, the mediator field can be integrated out, and the interaction can be described by **effective operators** in **effective field theory**



$$Q^2 \rightarrow 0$$

$$\Rightarrow$$

Scalar mediator propagator: $\frac{i}{Q^2 - m_S^2} \Rightarrow -\frac{i}{m_S^2}$

Lagrangian: $\mathcal{L}_{\text{int}} = g_\chi S \bar{\chi} \chi + g_q S \bar{q} q \Rightarrow \mathcal{L}_{\text{eff}} = G_{\text{eff}} \bar{\chi} \chi \bar{q} q, \quad G_{\text{eff}} = \frac{g_\chi g_q}{m_S^2}$

Effective Operators for DM-nucleon interactions

Assuming the DM particle is a **Dirac fermion** χ and using **Dirac fields** p and n to describe the proton and the neutron, the effective Lagrangian reads

$$\mathcal{L}_{\text{eff},N} = \sum_{N=p,n} \sum_{ij} G_{N,ij} \bar{\chi} \Gamma^i \chi \bar{N} \Gamma_j N, \quad \Gamma^i, \Gamma_j \in \{1, i\gamma_5, \gamma^\mu, \gamma^\mu \gamma_5, \sigma^{\mu\nu}\}$$

[Bélanger *et al.*, arXiv:0803.2360, Comput.Phys.Commun.]

- **Lorentz indices** in Γ^i and Γ_j should be contracted in pair
- Effective couplings $G_{N,ij}$ have a mass dimension of -2 : $[G_{N,ij}] = [\text{Mass}]^{-2}$
- $\bar{\chi} \chi \bar{N} N$ and $\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu N$ lead to **SI** DM-nucleon scattering
- $\bar{\chi} \gamma^\mu \gamma_5 \chi \bar{N} \gamma_\mu \gamma_5 N$ and $\bar{\chi} \sigma^{\mu\nu} \chi \bar{N} \sigma_{\mu\nu} N$ lead to **SD** DM-nucleon scattering
- The following operators lead to scattering cross sections $\sigma_{\chi N} \propto |Q^2|$:
 $\bar{\chi} i\gamma_5 \chi \bar{N} i\gamma_5 N$, $\bar{\chi} \chi \bar{N} i\gamma_5 N$, $\bar{\chi} i\gamma_5 \chi \bar{N} N$, $\bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu \gamma_5 N$, $\bar{\chi} \gamma^\mu \gamma_5 \chi \bar{N} \gamma_\mu N$
- For a **Majorana fermion** χ instead, we have $\bar{\chi} \gamma^\mu \chi = 0$ and $\bar{\chi} \sigma^{\mu\nu} \chi = 0$, and hence the related operators vanish

Higgs Portal for Majorana Fermionic DM

Interactions for a **Majorana fermion** χ , the **SM Higgs boson** h , and quarks q :

$$\mathcal{L}_{\text{DM}} \supset \frac{1}{2} g_\chi h \bar{\chi} \chi$$

$$\mathcal{L}_{\text{SM}} \supset - \sum_q \frac{m_q}{v} h \bar{q} q, \quad q = d, u, s, c, b, t$$

The amplitude for $\chi(p_1) + q(k_1) \rightarrow \chi(p_2) + q(k_2)$:

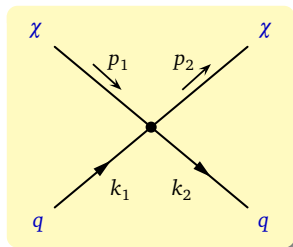
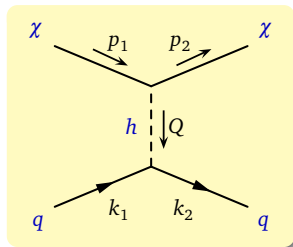
$$i\mathcal{M} = i g_\chi \bar{u}(p_2) u(p_1) \frac{i}{Q^2 - m_h^2} \left(-i \frac{m_q}{v} \right) \bar{u}(k_2) u(k_1)$$

Zero momentum transfer $\Downarrow Q^2 = (k_2 - k_1)^2 \rightarrow 0$

$$i\mathcal{M} = -i \frac{g_\chi m_q}{v m_h^2} \bar{u}(p_2) u(p_1) \bar{u}(k_2) u(k_1)$$

\Downarrow

$$\mathcal{L}_{\text{eff},q} = \sum_q G_{S,q} \bar{\chi} \chi \bar{q} q, \quad G_{S,q} = -\frac{g_\chi m_q}{2v m_h^2}$$



Effective Lagrangian: Scalar Type

Scalar-type effective Lagrangian for a **spin-1/2 fermion** χ :

$$\mathcal{L}_{S,q} = \sum_q G_{S,q} \bar{\chi} \chi \bar{q} q \quad \Rightarrow \quad \mathcal{L}_{S,N} = \sum_{N=p,n} G_{S,N} \bar{\chi} \chi \bar{N} N$$

$$G_{S,N} = m_N \left(\sum_{q=u,d,s} \frac{G_{S,q}}{m_q} f_q^N + \sum_{q=c,b,t} \frac{G_{S,q}}{m_q} f_q^N \right)$$

The second term accounts for DM interactions with gluons through loops of heavy quarks (c , b , and t): $f_Q^N = \frac{2}{27} \left(1 - \sum_{q=u,d,s} f_q^N \right)$

Form factor f_q^N is the contribution of q to m_N : $\langle N | m_q \bar{q} q | N \rangle = f_q^N m_N$

$$f_u^p \simeq 0.020, \quad f_d^p \simeq 0.026, \quad f_u^n \simeq 0.014, \quad f_d^n \simeq 0.036, \quad f_s^p = f_s^n \simeq 0.118$$

[Ellis *et al.*, arXiv:hep-ph/0001005, PLB]

The scalar type induces **SI** DM-nucleon scattering with a cross section of

$$\sigma_{\chi N}^{\text{SI}} = \frac{n_\chi}{\pi} \mu_{\chi N}^2 G_{S,N}^2, \quad \mu_{\chi N} \equiv \frac{m_\chi m_N}{m_\chi + m_N}, \quad n_\chi = \begin{cases} 1, & \text{for Dirac fermion } \chi \\ 4, & \text{for Majorana fermion } \chi \end{cases}$$

Z Portal for Majorana Fermionic DM

Interactions for a **Majorana fermion** χ , the **Z boson**, and quarks q :

$$\mathcal{L}_{\text{DM}} \supset \frac{1}{2} g_\chi Z_\mu \bar{\chi} \gamma^\mu \gamma_5 \chi, \quad \mathcal{L}_{\text{SM}} \supset \frac{g}{2c_W} Z_\mu \sum_q \bar{q} \gamma^\mu (g_V^q - g_A^q \gamma_5) q$$

$$g_V^{u_i} = \frac{1}{2} - \frac{4}{3} s_W^2, \quad g_V^{d_i} = -\frac{1}{2} + \frac{2}{3} s_W^2, \quad g_A^{u_i} = \frac{1}{2} = -g_A^{d_i}, \quad c_W \equiv \cos \theta_W, \quad s_W \equiv \sin \theta_W$$

$$\text{Z boson propagator} \quad \frac{-i}{Q^2 - m_Z^2} \left(g_{\mu\nu} - \frac{Q_\mu Q_\nu}{m_Z^2} \right) \xrightarrow{Q^2 \rightarrow 0} \frac{i}{m_Z^2} g_{\mu\nu}$$

Effective Lagrangian in the zero momentum transfer limit:

$$\mathcal{L}_{\text{eff},q} = \sum_q \bar{\chi} \gamma^\mu \gamma_5 \chi (G_{A,q} \bar{q} \gamma_\mu \gamma_5 q + G_{AV,q} \bar{q} \gamma_\mu q), \quad G_{A,q} = \frac{g_\chi g g_A^q}{4c_W m_Z^2}$$

$$G_{AV,q} = -\frac{g_\chi g g_V^q}{4c_W m_Z^2} \text{ leads to } \sigma_{\chi N} \propto |Q^2| \text{ and can be neglected for direct detection}$$

Effective Lagrangian: Axial Vector Type

Axial-vector-type effective Lagrangian for a **spin-1/2 fermion** χ :

$$\mathcal{L}_{A,q} = \sum_q G_{A,q} \bar{\chi} \gamma^\mu \gamma_5 \chi \bar{q} \gamma_\mu \gamma_5 q \quad \Rightarrow \quad \mathcal{L}_{A,N} = \sum_{N=p,n} G_{A,N} \bar{\chi} \gamma^\mu \gamma_5 \chi \bar{N} \gamma_\mu \gamma_5 N$$

$$G_{A,N} = \sum_{q=u,d,s} G_{A,q} \Delta_q^N, \quad 2\Delta_q^N s_\mu \equiv \langle N | \bar{q} \gamma_\mu \gamma_5 q | N \rangle$$

Form factors Δ_q^N account the contributions of quarks and anti-quarks to the nucleon spin vector s_μ , and can be extracted from lepton-proton scattering data:

$$\Delta_u^p = \Delta_d^n \simeq 0.842, \quad \Delta_d^p = \Delta_u^n \simeq -0.427, \quad \Delta_s^p = \Delta_s^n \simeq -0.085$$

[HERMES coll., arXiv:hep-ex/0609039, PRD]

Neutron form factors are related to proton form factors by **isospin symmetry**

The axial vector type induces **SD** DM-nucleon scattering:

$$\sigma_{\chi N}^{\text{SD}} = \frac{3n_\chi}{\pi} \mu_{\chi N}^2 G_{A,N}^2, \quad n_\chi = \begin{cases} 1, & \text{for Dirac fermion } \chi \\ 4, & \text{for Majorana fermion } \chi \end{cases}$$

Z Portal for Complex Scalar DM

Interactions for a **complex scalar** χ , the **Z boson**, and quarks q :

$$\mathcal{L}_{\text{DM}} \supset g_\chi Z_\mu (\chi^* i \overleftrightarrow{\partial}^\mu \chi)$$

$$\mathcal{L}_{\text{SM}} \supset \frac{g}{2c_W} Z_\mu \sum_q \bar{q} \gamma^\mu (g_V^q - g_A^q \gamma_5) q$$

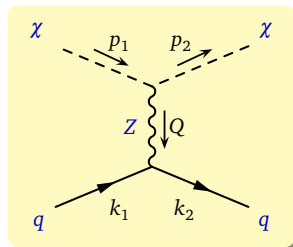
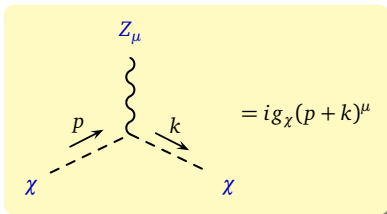
$$i\mathcal{M} = i g_\chi (p_1 + p_2)^\mu \frac{-i(g_{\mu\nu} - Q_\mu Q_\nu / m_Z^2)}{Q^2 - m_Z^2}$$

$$\times i \frac{g}{2c_W} \bar{u}(k_2) \gamma^\nu (g_V^q - g_A^q \gamma_5) u(k_1)$$

$$\xrightarrow{Q^2 \rightarrow 0} -i \frac{g_\chi g}{2c_W m_Z^2} (p_1 + p_2)^\mu \bar{u}(k_2) \gamma_\mu (g_V^q - g_A^q \gamma_5) u(k_1)$$

$$\mathcal{L}_{\text{eff},q} = \sum_q (\chi^* i \overleftrightarrow{\partial}^\mu \chi) (F_{V,q} \bar{q} \gamma_\mu q + F_{VA,q} \bar{q} \gamma_\mu \gamma_5 q)$$

$$F_{V,q} = -\frac{g_\chi g g_V^q}{2c_W m_Z^2}, \quad F_{VA,q} = \frac{g_\chi g g_A^q}{2c_W m_Z^2} (\Rightarrow \sigma_{\chi N} \propto |Q^2|)$$



Effective Lagrangian: Vector Type

 Vector-type effective Lagrangian for a **complex scalar** χ :

$$\mathcal{L}_{V,q} = \sum_q F_{V,q} (\chi^* i \overleftrightarrow{\partial}^\mu \chi) \bar{q} \gamma_\mu q \quad \Rightarrow \quad \mathcal{L}_{A,N} = \sum_{N=p,n} F_{V,N} (\chi^* i \overleftrightarrow{\partial}^\mu \chi) \bar{N} \gamma_\mu N$$

The relation between $F_{V,N}$ and $F_{V,q}$ reflects the valence quark numbers in N :

$$F_{V,p} = 2F_{V,u} + F_{V,d}, \quad F_{V,n} = F_{V,u} + 2F_{V,d}$$

The vector type induces **SI** DM-nucleon scattering: $\sigma_{\chi N}^{\text{SI}} = \frac{1}{\pi} \mu_{\chi N}^2 F_{V,N}^2$

 Vector-type effective Lagrangian for a **Dirac fermion** χ :

$$\mathcal{L}_{V,q} = \sum_q G_{V,q} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q \quad \Rightarrow \quad \mathcal{L}_{A,N} = \sum_{N=p,n} G_{V,N} \bar{\chi} \gamma^\mu \chi \bar{N} \gamma_\mu N$$

It also induces **SI** DM-nucleon scattering:

$$\sigma_{\chi N}^{\text{SI}} = \frac{1}{\pi} \mu_{\chi N}^2 G_{V,N}^2, \quad G_{V,p} = 2G_{V,u} + G_{V,d}, \quad G_{V,n} = G_{V,u} + 2G_{V,d}$$

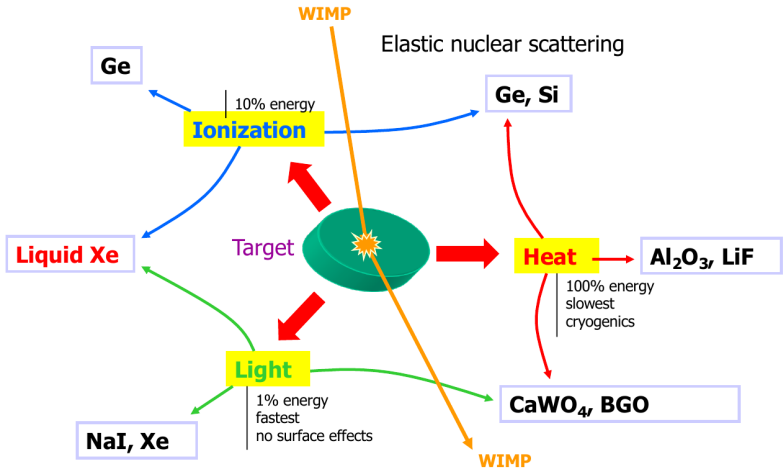
Effective Operators for DM-quark Interactions

	Spin-1/2 DM	Spin-0 DM
SI	$\bar{\chi}\chi\bar{q}q, \bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu q$	$\chi^*\chi\bar{q}q, (\chi^*i\overleftrightarrow{\partial}^\mu\chi)\bar{q}\gamma_\mu q$
SD	$\bar{\chi}\gamma^\mu\gamma_5\chi\bar{q}\gamma_\mu\gamma_5 q, \bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\mu\nu}q$	
$\sigma_{\chi N} \propto Q^2 $	$\bar{\chi}i\gamma_5\chi\bar{q}i\gamma_5 q, \bar{\chi}\chi\bar{q}i\gamma_5 q$ $\bar{\chi}i\gamma_5\chi\bar{q}q, \bar{\chi}\gamma^\mu\chi\bar{q}\gamma_\mu\gamma_5 q$ $\bar{\chi}\gamma^\mu\gamma_5\chi\bar{q}\gamma_\mu q, \epsilon^{\mu\nu\rho\sigma}\bar{\chi}\sigma^{\mu\nu}\chi\bar{q}\sigma_{\rho\sigma}q$	$\chi^*\chi\bar{q}i\gamma_5 q$ $(\chi^*i\overleftrightarrow{\partial}^\mu\chi)\bar{q}\gamma_\mu\gamma_5 q$
	Spin-3/2 DM	Spin-1 DM
SI	$\bar{\chi}^\mu\chi_\mu\bar{q}q, \bar{\chi}^\nu\gamma^\mu\chi_\nu\bar{q}\gamma_\mu q$	$\chi_\mu^*\chi^\mu\bar{q}q, (\chi_\nu^*i\overleftrightarrow{\partial}^\mu\chi^\nu)\bar{q}\gamma_\mu q$
SD	$\bar{\chi}^\nu\gamma^\mu\gamma_5\chi_\nu\bar{q}\gamma_\mu\gamma_5 q, \bar{\chi}^\rho\sigma^{\mu\nu}\chi_\rho\bar{q}\sigma_{\mu\nu}q$ $i(\bar{\chi}^\mu\chi^\nu - \bar{\chi}^\nu\chi^\mu)\bar{q}\sigma_{\mu\nu}q$	$i(\chi_\mu^*\chi_\nu - \chi_\nu^*\chi_\mu)\bar{q}\sigma^{\mu\nu}q$ $\epsilon^{\mu\nu\rho\sigma}(\chi_\mu^*\overleftrightarrow{\partial}_\nu\chi_\rho)\bar{q}\gamma_\sigma\gamma_5 q$
$\sigma_{\chi N} \propto Q^2 $	$\bar{\chi}^\mu i\gamma_5\chi_\mu\bar{q}i\gamma_5 q, \bar{\chi}^\mu\chi_\mu\bar{q}i\gamma_5 q$ $\bar{\chi}^\mu i\gamma_5\chi_\mu\bar{q}q, \bar{\chi}^\nu\gamma^\mu\chi_\nu\bar{q}\gamma_\mu\gamma_5 q$ $\bar{\chi}^\mu\gamma^\mu\gamma_5\chi_\nu\bar{q}\gamma_\mu q, \epsilon^{\mu\nu\rho\sigma}i(\bar{\chi}_\mu\chi_\nu - \bar{\chi}_\nu\chi_\mu)\bar{q}\sigma_{\rho\sigma}q$ $\epsilon^{\mu\nu\rho\sigma}\bar{\chi}^\alpha\sigma_{\mu\nu}\chi_\alpha\bar{q}\sigma_{\rho\sigma}q, (\bar{\chi}^\mu\gamma_5\chi^\nu - \bar{\chi}^\nu\gamma_5\chi^\mu)\bar{q}\sigma_{\mu\nu}q$ $\epsilon^{\mu\nu\rho\sigma}(\bar{\chi}_\mu\gamma_5\chi_\nu - \bar{\chi}_\nu\gamma_5\chi_\mu)\bar{q}\sigma_{\rho\sigma}q$	$\chi_\mu^*\chi^\mu\bar{q}i\gamma_5 q$ $(\chi_\nu^*i\overleftrightarrow{\partial}^\mu\chi^\nu)\bar{q}\gamma_\mu\gamma_5 q$ $\epsilon^{\mu\nu\rho\sigma}(\chi_\mu^*\overleftrightarrow{\partial}_\nu\chi_\rho)\bar{q}\gamma_\sigma q$ $\epsilon^{\mu\nu\rho\sigma}i(\chi_\mu^*\chi_\nu - \chi_\nu^*\chi_\mu)\bar{q}\sigma_{\rho\sigma}q$

[Zheng, **ZHY**, Shao, Bi, Li, Zhang, arXiv:1012.2022, NPB;

ZHY, Zheng, Bi, Li, Yao, Zhang, arXiv:1112.6052, NPB]

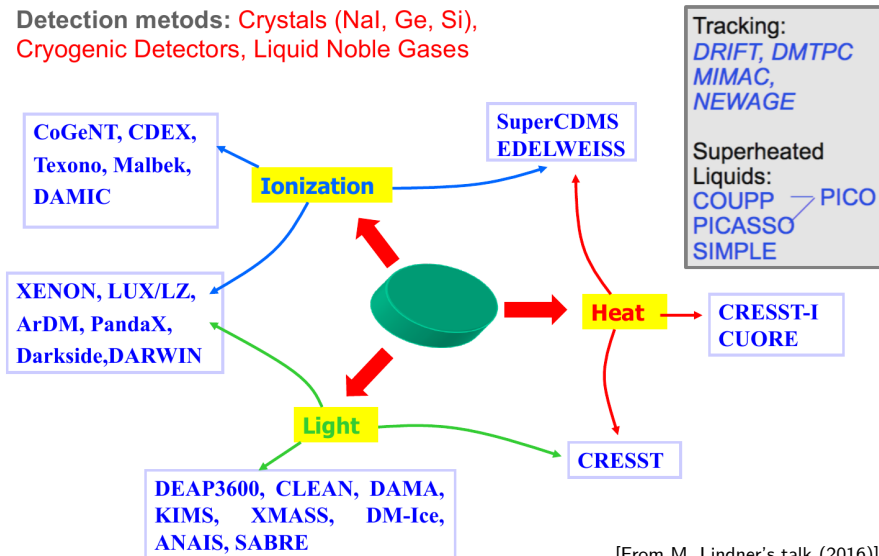
Technologies and Detector Material



[From M. Lindner's talk (2016)]

Technologies and Detector Material

Detection methods: Crystals (NaI, Ge, Si),
Cryogenic Detectors, Liquid Noble Gases



[From M. Lindner's talk (2016)]

Example: Dual-phase Xenon Time Projection Chamber

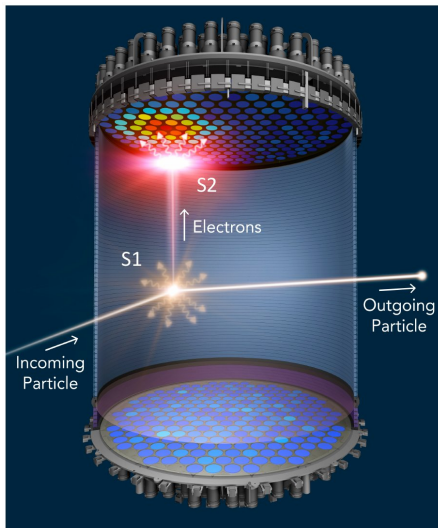
Upper: **Xenon gas**

Lower: **Liquid Xenon**

UV scintillation photons recorded by photomultiplier tube (PMT) arrays on top and bottom

- **Primary scintillation (S1):**
Scintillation light promptly emitted from the interaction vertex
- **Secondary scintillation (S2):**
Ionization electrons emitted from the interaction are drifted to the surface and into the gas, where they emit proportional scintillation light

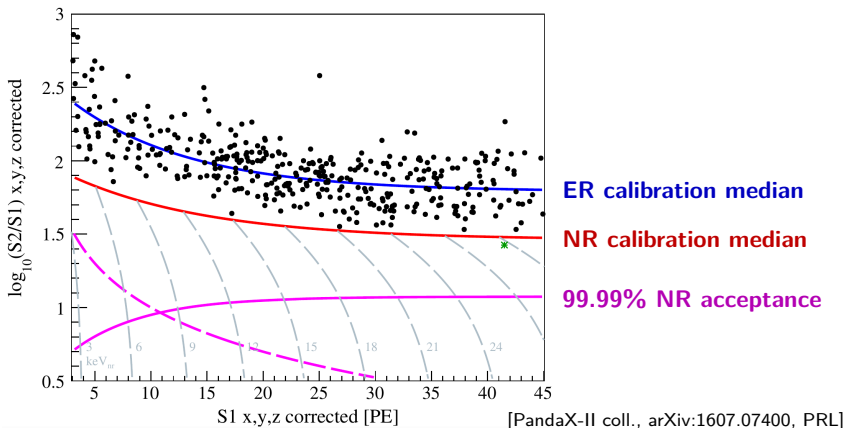
Experiments: XENON, LUX, PandaX



[From A. Cottle's talk (2017)]

PandaX-II Real Data: S1 versus S2

- S1 and S2: characterized by numbers of **photoelectrons (PEs)** in PMTs
- The γ **background**, which produces **electron recoil (ER)** events, can be distinguished from **nuclear recoil (NR)** events using the S2-to-S1 ratio



Backgrounds

Background suppression:

Deep underground

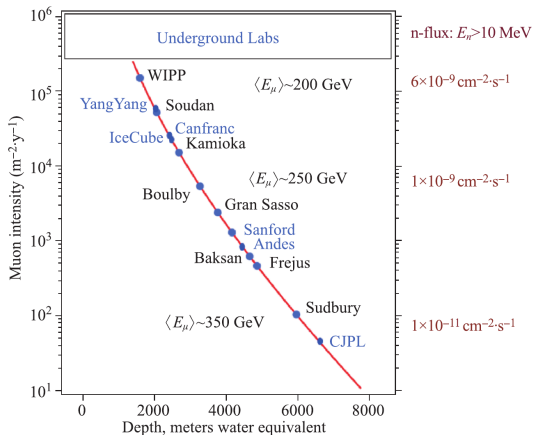
Shielded environments

● Cosmogenic backgrounds:

- Cosmic rays and secondary reactions
- Activation products in shields and detectors

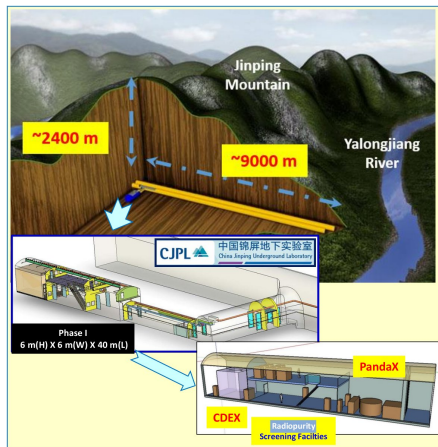
● Radiogenic backgrounds:

- External natural radioactivity: walls, structures of site, radon
- Internal radioactivity: shield and construction materials, detector contamination in manufacture, naturally occurring radio-isotopes in target material



[From P. Cushman's talk (2014)]

China JinPing Underground Laboratory (CJPL)

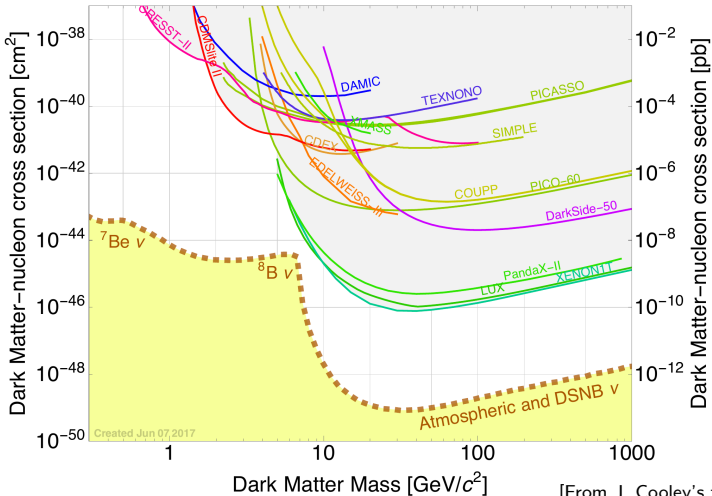


[Yue et al., arXiv:1602.02462]

Experiments: CDEX, PandaX

Exclusion Limits for SI Scattering

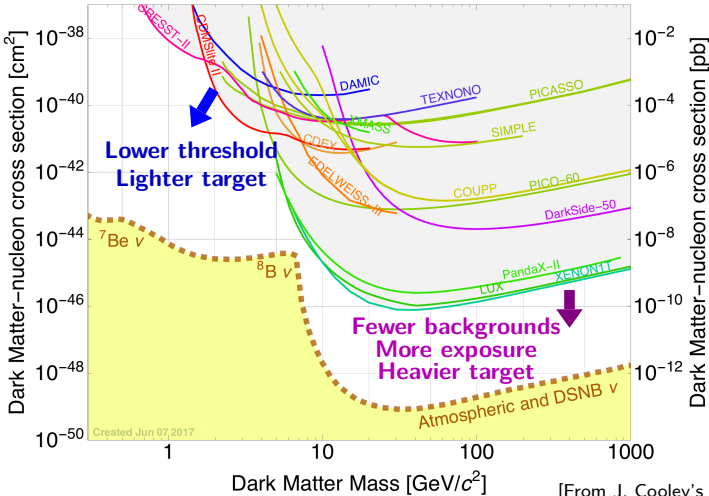
💡 Assuming **isospin conservation** ($G_p = G_n$) for **SI scattering**, we can treat protons and neutrons as the same species, **“nucleons”**



[From J. Cooley's talk (2017)]

Exclusion Limits for SI Scattering

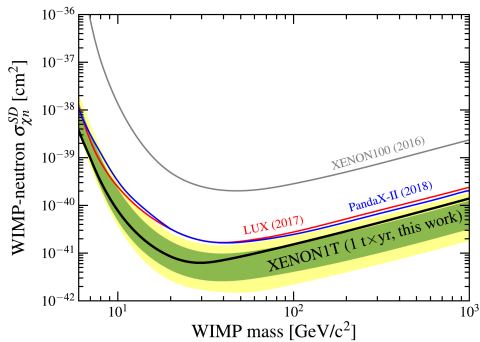
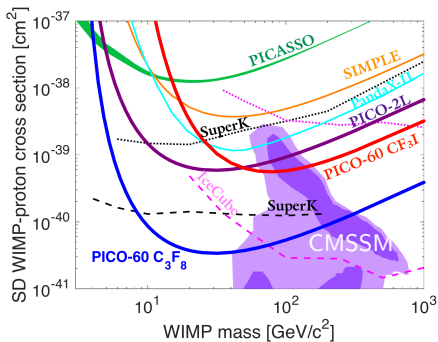
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[From J. Cooley's talk (2017)]

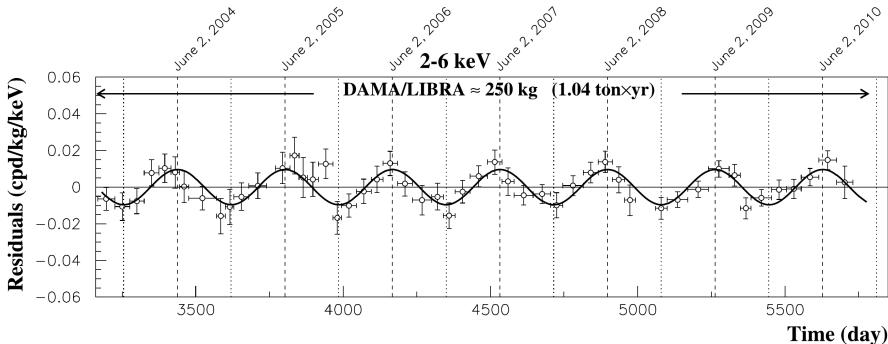
Exclusion Limits for SD Scattering

- For **SD scattering**, specific detection material usually has **very different** sensitivities to WIMP-**proton** and WIMP-**neutron** cross sections
- As there is no coherent enhancement for SD scattering, the sensitivity is **lower** than the SI case by **several orders of magnitude**



DAMA/LIBRA Annual Modulation “Signal”

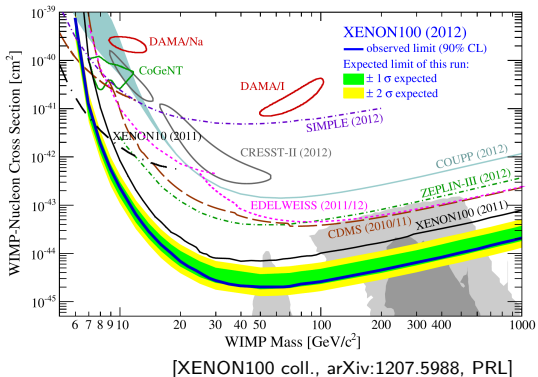
- 😄 Highly radio-pure scintillating **Nal(Tl) crystals** at Gran Sasso, Italy
- 😊 **Annual modulation signal** observed over 14 cycles at **9.3σ significance**
- 😞 **No background/signal discrimination**



[Bernabei *et al.*, arXiv:1308.5109, EPJC]

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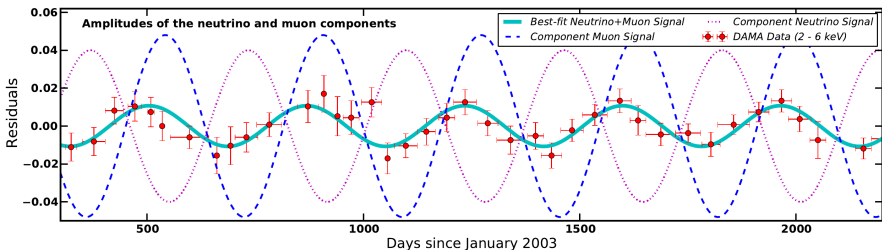


😞 **Favored regions excluded by other direct detection experiments**

Other Sources for DAMA/LIBRA Signal

🤩 The DAMA/LIBRA signal might be composed of **neutrons** liberated in the material surrounding the detector by **two sources** [Davis, arXiv:1407.1052, PRL]

- **Atmospheric muons:** flux depends on the **temperature of the atmosphere**, peaked on **June 21st**
- **Solar neutrinos:** flux depends on the **distance between the Earth and the Sun**, peaked on **January 4th**

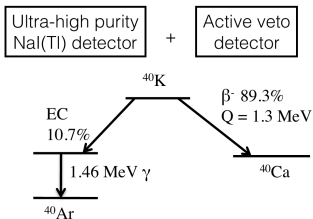


😬 **Objection:** Klinger & Kudryavtsev, “muon-induced neutrons do not explain the DAMA data,” arXiv:1503.07225, PRL

Further Test: SABRE Project

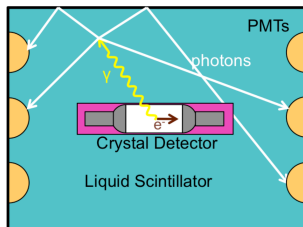
SABRE: Sodium iodide with Active Background REjection

- Complementary tests in **both hemispheres**: one part in Gran Sasso (Italy) and one part in Stawell (Australia)
- Developing **low background** scintillating NaI(Tl) crystals that exceed the radio-purity of DAMA/LIBRA
- A well-shielded **active veto** to reduce internal and external backgrounds



$^{40}\text{K} \rightarrow ^{40}\text{Ar}$, $\sim 11\%$ branch ratio

- 3 keV K shell X-ray, Auger e^-
- Background at ~ 3 keV if γ escapes

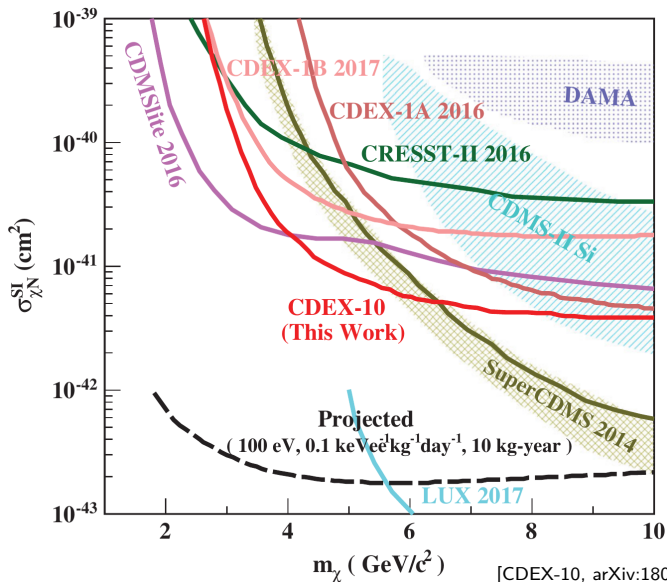


1.46 MeV γ can be detected by a veto.

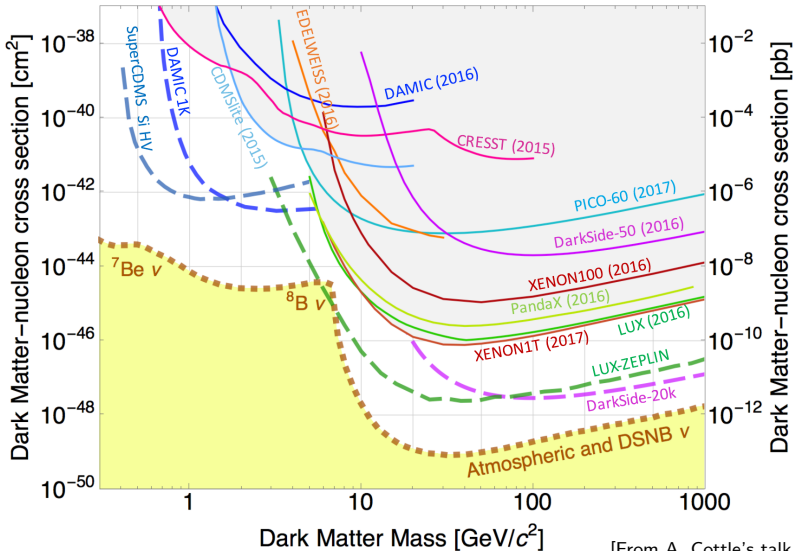
^{40}K background can be rejected.

[From E. Barberio's talk]

Low Mass Region



Near Future Prospect



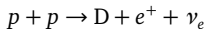
[From A. Cottle's talk (2017)]

Neutrino Backgrounds

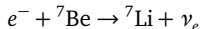
Direct detection experiments will be sensitive to **coherent neutrino-nucleus scattering (CNS)** due to astrophysical neutrinos [Billard *et al.*, arXiv:1307.5458, PRD]

• Solar neutrinos

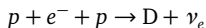
• pp neutrinos:



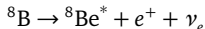
• ${}^7\text{Be}$ neutrinos:



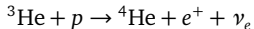
• pep neutrinos:



• ${}^8\text{B}$ neutrinos:



• Hep neutrinos:

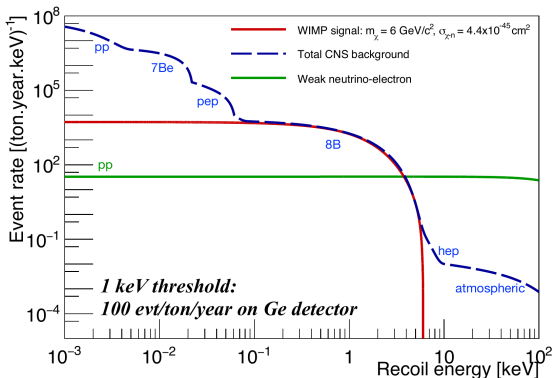


• Atmospheric neutrinos

Cosmic-ray collisions in the atmosphere

• Diffuse supernova neutrino background (DSNB)

All supernova explosions in the past history of the Universe

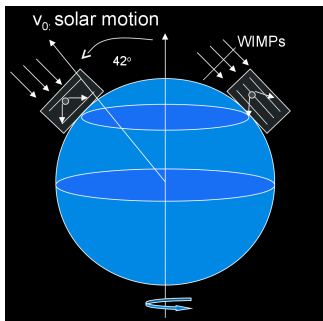


[From J. Billard's talk (2016)]

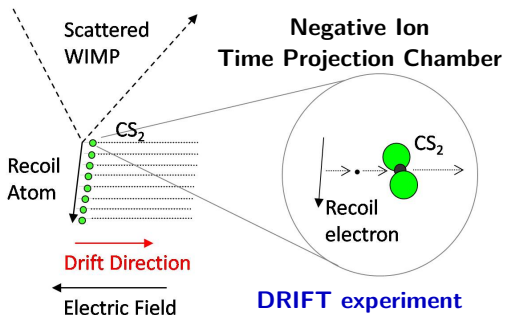
Going beyond the Neutrino Floor

Possible ways to reduce the impact of neutrino backgrounds:

- Reduction of **systematic uncertainties** on neutrino fluxes
- Utilization of **different target nuclei** [Ruppin *et al.*, arXiv:1408.3581, PRD]
- Measurement of **annual modulation** [Davis, arXiv:1412.1475, JCAP]
- Measurement of **nuclear recoil direction** [O'Hare, *et al.*, arXiv:1505.08061, PRD]



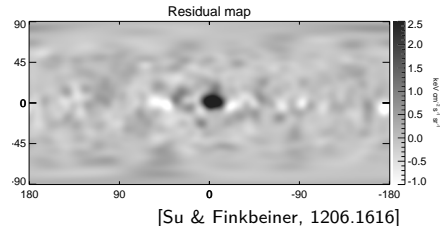
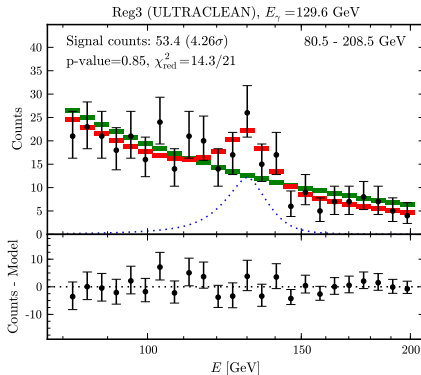
Diurnal modulation



[From J. Spooner's talk (2010)]

A γ -ray Line Signal at the Galactic Center?

- Using the 3.7-year Fermi-LAT γ -ray data, several analyses showed that there might be evidence of a **monochromatic γ -ray line at energy ~ 130 GeV**, originating from the Galactic center region (about $3 - 4\sigma$)
- It may be explained by **DM annihilation with $\langle \sigma_{\text{ann}} v \rangle \sim 10^{-27} \text{ cm}^3 \text{ s}^{-1}$**

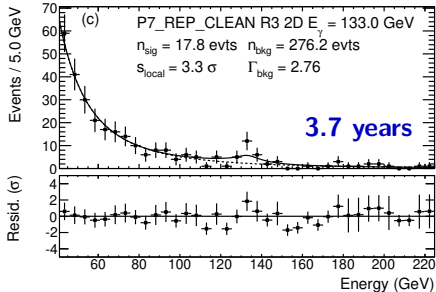


[Weniger, 1204.2797, JCAP]

Fermi-LAT Official Results: Not Confirmed with More Data

• 3.7-year data

The most significant fit occurred at $E_\gamma = 133$ GeV and had a **local significance** of 3.3σ , translating to a global significance of 1.6σ



[Fermi-LAT Coll., 1305.5597, PRD]

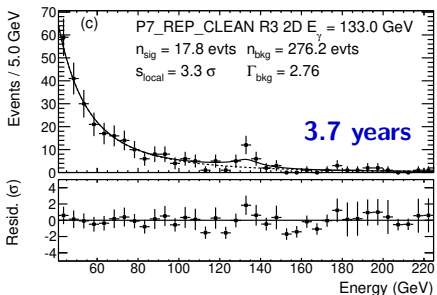
Fermi-LAT Official Results: Not Confirmed with More Data

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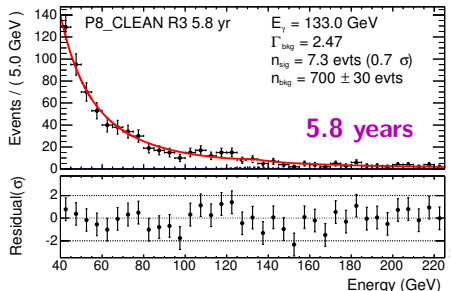
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- 5.8-year data**

The **local significance** has dropped to 0.72σ



[Fermi-LAT Coll., 1305.5597, PRD]



[Fermi-LAT Coll., 1506.00013, PRD]

Cosmic Ray Propagation Equation

The **propagation equation** for Galactic cosmic rays is

$$\frac{\partial \psi}{\partial t} = Q(\mathbf{x}, p) + \nabla \cdot (D_{xx} \nabla \psi - \mathbf{V}_c \psi) + \frac{\partial}{\partial p} \left[p^2 D_{pp} \frac{\partial}{\partial p} \left(\frac{\psi}{p^2} \right) \right] - \frac{\partial}{\partial p} \left[\dot{p} \psi - \frac{p}{3} (\nabla \cdot \mathbf{V}_c) \psi \right] - \frac{\psi}{\tau_f} - \frac{\psi}{\tau_r}$$

$\psi = \psi(\mathbf{x}, p, t)$: cosmic ray density per momentum interval

$Q(\mathbf{x}, p)$: cosmic ray source term

D_{xx} : spatial diffusion coefficient

D_{pp} : diffusion coefficient in the momentum space for reacceleration

\mathbf{V}_c : convection velocity

$\dot{p} \equiv dp/dt$: momentum loss rate

τ_f : fragmentation time scale

τ_r : radioactive decay time scale

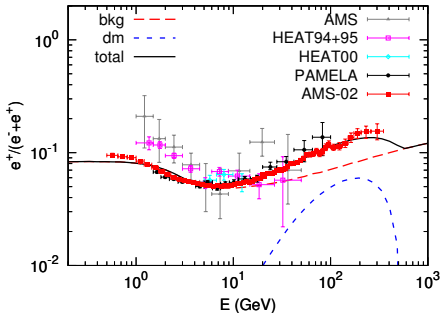
Numerical tools

- **GALPROP**: <https://galprop.stanford.edu>
- **DRAGON**: <https://github.com/cosmicrays/DRAGON>

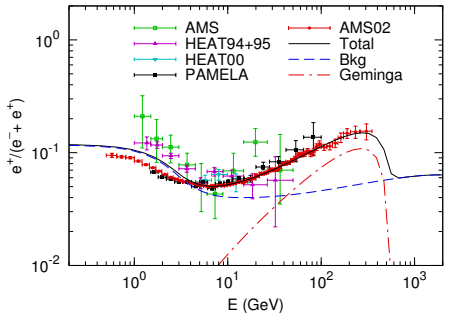
Interpretation: Dark Matter vs Pulsar

Interpretation with Galactic
DM annihilation into $\tau^+ \tau^-$

Interpretation with the
nearby pulsar Geminga



[Yuan, Bi, et al., 1304.1482, APP]



[Yin, ZHY, Yuan, Bi, 1304.4128, PRD]

Summary

- **Dark matter** connects our knowledge of the Universe from the **largest** to the **smallest** scales
- Although several anomalous observations have been found in direct and indirect searches, there is **no absolutely solid DM detection signal so far**
- **DM detection sensitivities are being improved quickly**; it is very promising to detect robust DM signals in the near future

