

# Current and Future Collider Searches for Electroweak Dark Matter Models

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Based on Tait, ZHY, arXiv:1601.01354, JHEP

CF Cai, ZHY, HH Zhang, arXiv:1611.02186, NPB

CF Cai, ZHY, HH Zhang, arXiv:1705.07921, NPB

QF Xiang, XJ Bi, PF Yin, ZHY, arXiv:1707.03094, PRD

JW Wang, XJ Bi, QF Xiang, PF Yin, ZHY, arXiv:1711.05622, PRD



10th National High Energy Physics  
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of Chinese Physical Society

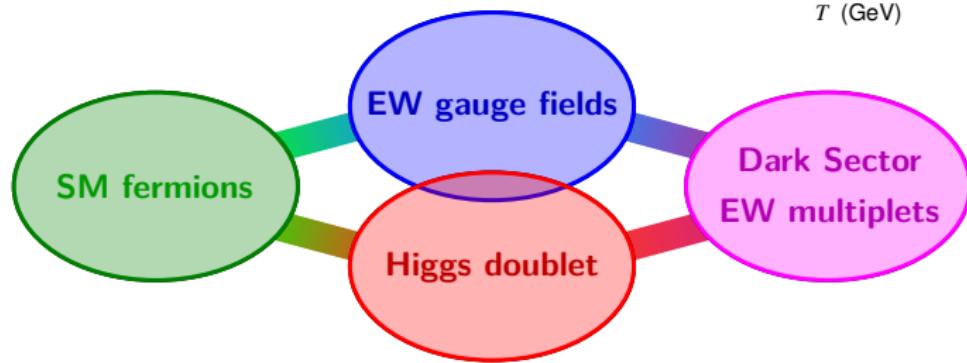
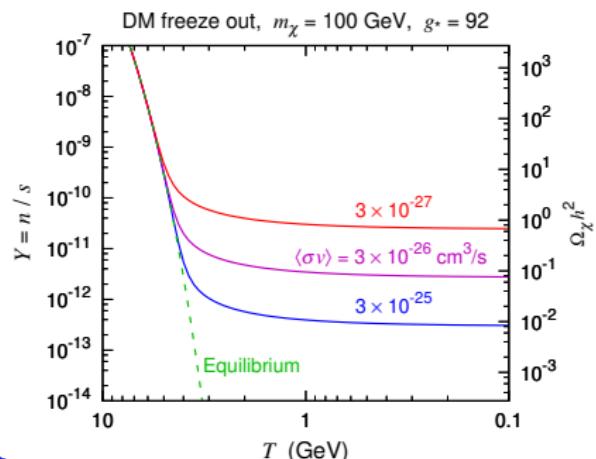
Shanghai, June 22, 2018



# Electroweak Dark Matter Models

🔥 An attractive class of **dark matter** (DM) candidates is **weakly interacting massive particles** (WIMPs), as they can explain the observed DM relic abundance via thermal production mechanism

💡 It is natural to construct WIMP models by extending the Standard Model (SM) with a **dark sector** consisting of electroweak (EW)  $SU(2)_L$  **multiplets**, whose **neutral** components could provide a viable DM candidate



# Fermionic Models

- ① **SDFDM: Singlet + Doublets** [Mahbubani, Senatore, hep-ph/0510064, PRD; D'Eramo, 0705.4493, PRD; Cohen *et al.*, 1109.2604, PRD]

$$S \in (\mathbf{1}, 0), \quad D_1 = \begin{pmatrix} D_1^0 \\ D_1^+ \\ D_1^- \end{pmatrix} \in (\mathbf{2}, -1/2), \quad D_2 = \begin{pmatrix} D_2^+ \\ D_2^0 \\ D_2^- \end{pmatrix} \in (\mathbf{2}, +1/2)$$

$$\mathcal{L} \supset -\frac{1}{2} \mathbf{m}_S S S - \mathbf{m}_D \epsilon_{ij} D_1^i D_2^j + \mathbf{y}_1 H_i S D_1^i - \mathbf{y}_2 H_i^\dagger S D_2^i + \text{h.c.}$$

- ② **DTFDM: Doublets + Triplet** [Dedes, Karamitros, 1403.7744, PRD]

$$D_1 = \begin{pmatrix} D_1^0 \\ D_1^+ \\ D_1^- \end{pmatrix} \in (\mathbf{2}, -1/2), \quad D_2 = \begin{pmatrix} D_2^+ \\ D_2^0 \\ D_2^- \end{pmatrix} \in (\mathbf{2}, +1/2), \quad T = \begin{pmatrix} T^+ \\ T^0 \\ T^- \end{pmatrix} \in (\mathbf{3}, 0)$$

$$\mathcal{L} \supset \mathbf{m}_D \epsilon_{ij} D_1^i D_2^j - \frac{1}{2} \mathbf{m}_T T^a T^a + \mathbf{y}_1 H_i T^a (\sigma^a)_j^i D_1^j - \mathbf{y}_2 H_i^\dagger T^a (\sigma^a)_j^i D_2^j + \text{h.c.}$$

- ③ **TQFDM: Triplet + Quadruplets** [Tait, ZHY, 1601.01354, JHEP]

$$T = \begin{pmatrix} T^+ \\ T^0 \\ T^- \end{pmatrix} \in (\mathbf{3}, 0), \quad Q_1 = \begin{pmatrix} Q_1^+ \\ Q_1^0 \\ Q_1^- \\ Q_1^- \end{pmatrix} \in (\mathbf{4}, -1/2), \quad Q_2 = \begin{pmatrix} Q_2^{++} \\ Q_2^+ \\ Q_2^0 \\ Q_2^- \end{pmatrix} \in (\mathbf{4}, +1/2)$$

$$\mathcal{L} \supset -\frac{1}{2} \mathbf{m}_T T T - \mathbf{m}_Q Q_1 Q_2 + \mathbf{y}_1 \epsilon_{jl} (Q_1)_i^{jk} T_k^i H^l - \mathbf{y}_2 (Q_2)_i^{jk} T_k^i H_j^\dagger + \text{h.c.}$$

# Mass Eigenstates

Take the **TQFDM** model as an example [Tait, **ZHY**, 1601.01354, JHEP]

$$\begin{aligned}\mathcal{L}_{\text{mass}} &= -\frac{1}{2}(T^0, Q_1^0, Q_2^0) \mathcal{M}_N \begin{pmatrix} T^0 \\ Q_1^0 \\ Q_2^0 \end{pmatrix} - (T^-, Q_1^-, Q_2^-) \mathcal{M}_C \begin{pmatrix} T^+ \\ Q_1^+ \\ Q_2^+ \end{pmatrix} - m_Q Q_1^{--} Q_2^{++} + \text{h.c.} \\ &= -\frac{1}{2} \sum_{i=1}^3 m_{\chi_i^0} \chi_i^0 \chi_i^0 - \sum_{i=1}^3 m_{\chi_i^\pm} \chi_i^- \chi_i^+ + \text{h.c.} - m_Q \chi^{--} \chi^{++}\end{aligned}$$

$$\mathcal{M}_N = \begin{pmatrix} m_T & \frac{1}{\sqrt{3}}y_1v & -\frac{1}{\sqrt{3}}y_2v \\ \frac{1}{\sqrt{3}}y_1v & 0 & m_Q \\ -\frac{1}{\sqrt{3}}y_2v & m_Q & 0 \end{pmatrix}, \quad \mathcal{M}_C = \begin{pmatrix} m_T & \frac{1}{\sqrt{2}}y_1v & -\frac{1}{\sqrt{6}}y_2v \\ -\frac{1}{\sqrt{6}}y_1v & 0 & -m_Q \\ \frac{1}{\sqrt{2}}y_2v & -m_Q & 0 \end{pmatrix}$$

$$\begin{pmatrix} T^0 \\ Q_1^0 \\ Q_2^0 \end{pmatrix} = \mathcal{N} \begin{pmatrix} \chi_1^0 \\ \chi_2^0 \\ \chi_3^0 \end{pmatrix}, \quad \begin{pmatrix} T^+ \\ Q_1^+ \\ Q_2^+ \end{pmatrix} = \mathcal{C}_L \begin{pmatrix} \chi_1^+ \\ \chi_2^+ \\ \chi_3^+ \end{pmatrix}, \quad \begin{pmatrix} T^- \\ Q_1^- \\ Q_2^- \end{pmatrix} = \mathcal{C}_R \begin{pmatrix} \chi_1^- \\ \chi_2^- \\ \chi_3^- \end{pmatrix}, \quad \chi^{--} \equiv Q_1^{--}, \quad \chi^{++} \equiv Q_2^{++}$$

👉 3 Majorana fermions, 3 singly charged fermions, 1 doubly charged fermion

✨  $\chi_1^0$  would be an excellent **DM candidate** if it is the lightest among them

# Monojet + $\cancel{E}_T$ Channel at $pp$ Colliders (TQFDM)

💥 Pair production of dark sector fermions:

$$pp \rightarrow \chi\chi + \text{jets}, \quad \chi = \chi_i^0, \chi_i^\pm, \chi^{\pm\pm}$$

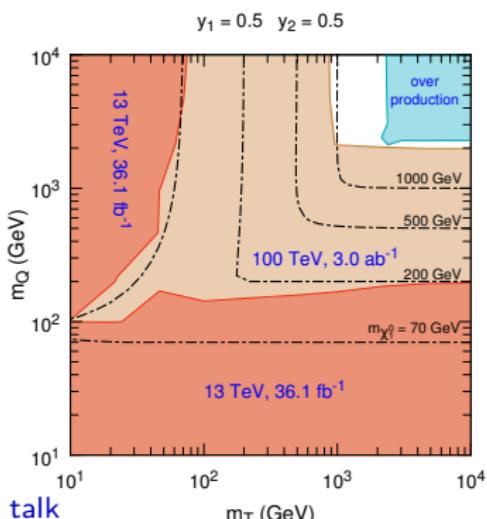
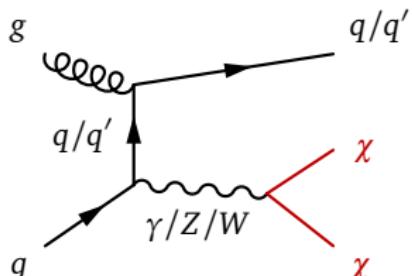
Associated with  $\geq 1$  hard jet from initial state radiation  $\Rightarrow$  monojet +  $\cancel{E}_T$  final state

🔍 Current constraints: ATLAS searches at the 13 TeV LHC with  $36.1 \text{ fb}^{-1}$  data [ATLAS-CONF-2017-060] excluded parameter regions up to  $m_{\chi_1^0} \sim 70 - 200 \text{ GeV}$

🎯 Future prospect: SPPC at 100 TeV collecting with  $3 \text{ ab}^{-1}$  data would be able to explore up to  $m_{\chi_1^0} \sim 1 - 2 \text{ TeV}$

[JW Wang, XJ Bi, QF Xiang, PF Yin, ZHY, 1711.05622, PRD]

More details will be given by Jin-Wei Wang in a following talk



# Multilepton + $\cancel{E}_T$ Channel at $pp$ Colliders (TQFDM)

💥 Signals in the  $2\ell + \cancel{E}_T$  channel:

$$\chi_i^+ \chi_j^- \rightarrow W^+ (\rightarrow \ell^+ \nu) W^- (\rightarrow \ell^- \bar{\nu}) \chi_1^0 \chi_1^0$$

💥 Signals in the  $2\ell + \text{jets} + \cancel{E}_T$  channel:

$$\chi_i^0 \chi_j^\pm \rightarrow Z (\rightarrow \ell^+ \ell^-) W^\pm (\rightarrow jj) \chi_1^0 \chi_1^0$$

💥 Signals in the  $3\ell + \cancel{E}_T$  channel:

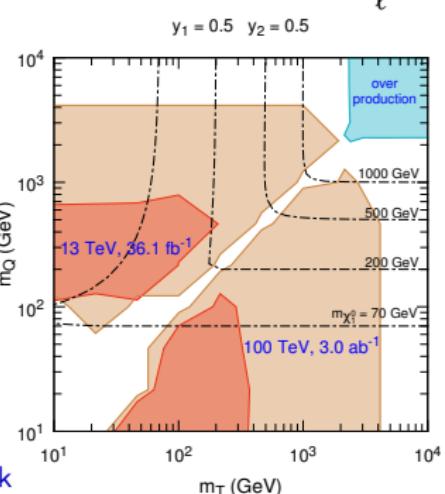
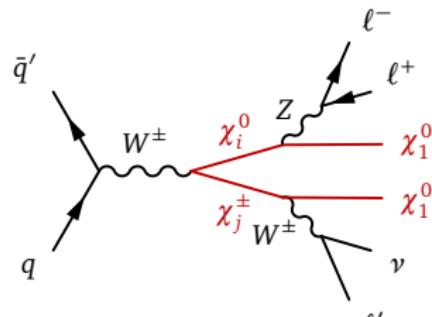
$$\chi_i^0 \chi_j^\pm \rightarrow Z (\rightarrow \ell^+ \ell^-) W^\pm (\rightarrow \ell' \nu) \chi_1^0 \chi_1^0$$

🔍 Current constraints: ATLAS searches at the 13 TeV LHC with  $36.1 \text{ fb}^{-1}$  data [ATLAS-CONF-2017-039]

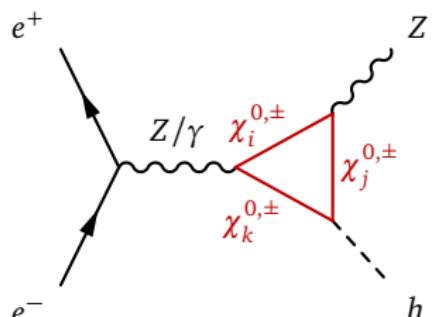
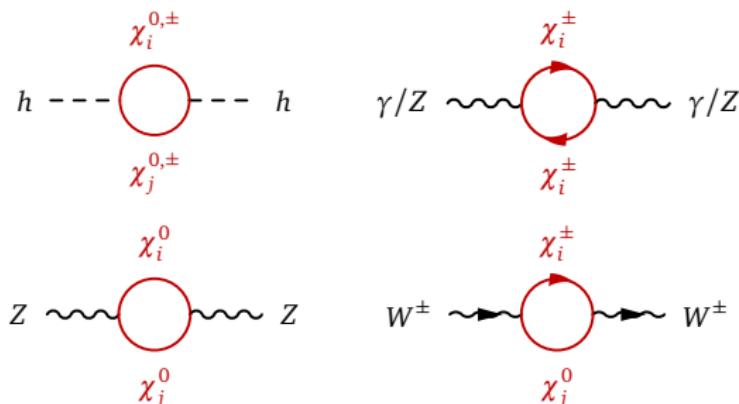
⌚ Future prospect: SPPC experiments at  $\sqrt{s} = 100 \text{ TeV}$  with  $3 \text{ ab}^{-1}$  data

[JW Wang, XJ Bi, QF Xiang, PF Yin, **ZHY**, 1711.05622, PRD]

More details will be given by Jin-Wei Wang in a following talk



# Correction to $e^+e^- \rightarrow Zh$ (DTFDM)

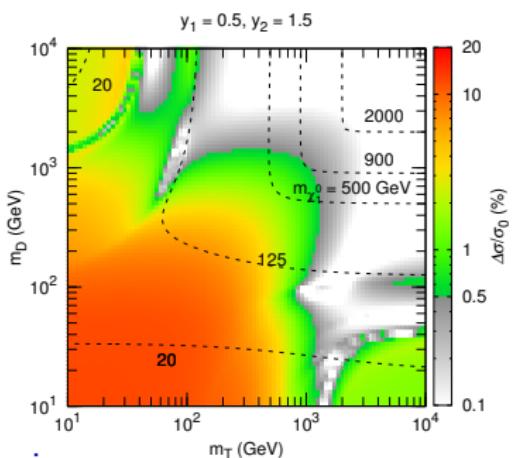


💥  $e^+e^- \rightarrow Zh$  cross section could be modified by dark sector fermions via **loop effects**

🌀 **CEPC** experiments with  $5 \text{ ab}^{-1}$  data can measure the relative deviation from SM down to  $\Delta\sigma/\sigma_0 \simeq 0.51\%$  [CEPC-SPPC pre-CDR, Vol. II]

[QF Xiang, XJ Bi, PF Yin, **ZHY**, 1707.03094, PRD]

Details have been given in **Qian-Fei Xiang's talk in this morning**

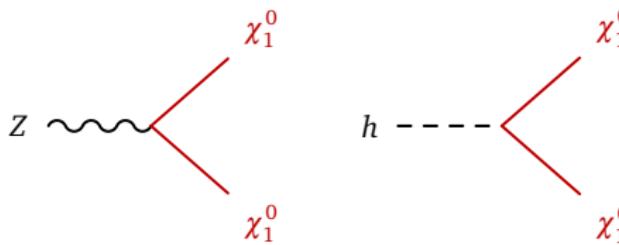


# Higgs Boson Invisible and Diphoton Decays (DTFDM)

The LEP bound on the  $Z$  invisible width is

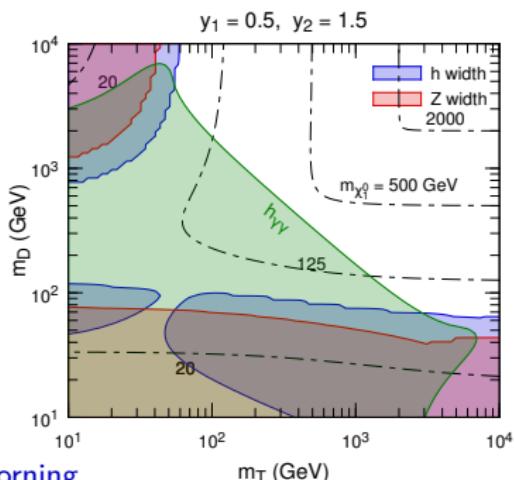
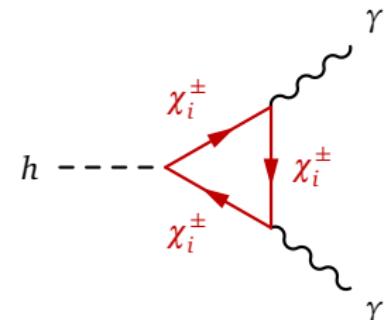
$$\Gamma_{Z,\text{inv}}^{\text{BSM}} < 2 \text{ MeV} \text{ at 95% CL}$$

For CEPC experiments collecting  $5 \text{ ab}^{-1}$  data, the 95% CL expected constraint on the  $h$  invisible width would be  $\Gamma_{h,\text{inv}} < 11.4 \text{ keV}$ , while the relative precision of the  $h \rightarrow \gamma\gamma$  decay width could be measured to 9.4% [CEPC-SPPC pre-CDR, Vol. II]



[QF Xiang, XJ Bi, PF Yin, **ZHY**, 1707.03094, PRD]

Details have been given in Qian-Fei Xiang's talk in this morning



# Electroweak Oblique Parameters

 EW oblique parameters  $S$ ,  $T$ , and  $U$  are introduced to describe new physics corrections to gauge boson propagators [Peskin, Takeuchi, PRL, '90; PRD '92]

$$S = 16\pi[\Pi'_{33}(0) - \Pi'_{3Q}(0)]$$

$$T = \frac{4\pi}{s_W^2 c_W^2 m_Z^2} [\Pi_{11}(0) - \Pi_{33}(0)], \quad U = 16\pi[\Pi'_{11}(0) - \Pi'_{33}(0)]$$

Here  $\Pi'_{IJ}(0) \equiv \partial \Pi_{IJ}(p^2)/\partial p^2|_{p^2=0}$ ,  $s_W \equiv \sin \theta_W$ ,  $c_W \equiv \cos \theta_W$

$$\gamma \sim \text{wavy line} \text{ (yellow circle)} \gamma = ie^2 \Pi_{QQ}(p^2) g^{\mu\nu} + (p^\mu p^\nu \text{ terms})$$

$$Z \sim \text{wavy line} \text{ (yellow circle)} \gamma = \frac{ie^2}{s_W c_W} [\Pi_{3Q}(p^2) - s_W^2 \Pi_{QQ}(p^2)] g^{\mu\nu} + (p^\mu p^\nu \text{ terms})$$

$$Z \sim \text{wavy line} \text{ (yellow circle)} Z = \frac{ie^2}{s_W^2 c_W^2} [\Pi_{33}(p^2) - 2s_W^2 \Pi_{3Q}(p^2) + s_W^4 \Pi_{QQ}(p^2)] g^{\mu\nu} + (p^\mu p^\nu \text{ terms})$$

$$W \sim \text{wavy line} \text{ (yellow circle)} W = \frac{ie^2}{s_W^2} \Pi_{11}(p^2) g^{\mu\nu} + (p^\mu p^\nu \text{ terms})$$

# CEPC Precision of Electroweak Observables

	Current data	CEPC-B precision	CEPC-I precision
$\alpha_s(m_Z^2)$	$0.1185 \pm 0.0006$	$\pm 1 \times 10^{-4}$	
$\Delta\alpha_{\text{had}}^{(5)}(m_Z^2)$	$0.02765 \pm 0.00008$	$\pm 4.7 \times 10^{-5}$	
$m_Z$ [GeV]	$91.1875 \pm 0.0021$	$\pm 5 \times 10^{-4}$	$\pm 1 \times 10^{-4}$
$m_t$ [GeV]	$173.34 \pm 0.76_{\text{ex}} \pm 0.5_{\text{th}}$	$\pm 0.2_{\text{ex}} \pm 0.5_{\text{th}}$	$\pm 0.03_{\text{ex}} \pm 0.1_{\text{th}}$
$m_h$ [GeV]	$125.09 \pm 0.24$	$\pm 5.9 \times 10^{-3}$	
$m_W$ [GeV]	$80.385 \pm 0.015_{\text{ex}} \pm 0.004_{\text{th}}$	$(\pm 3_{\text{ex}} \pm 1_{\text{th}}) \times 10^{-3}$	
$\sin^2\theta_{\text{eff}}^\ell$	$0.23153 \pm 0.00016$	$(\pm 2.3_{\text{ex}} \pm 1.5_{\text{th}}) \times 10^{-5}$	
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	$(\pm 5_{\text{ex}} \pm 0.8_{\text{th}}) \times 10^{-4}$	$(\pm 1_{\text{ex}} \pm 0.8_{\text{th}}) \times 10^{-4}$

For **CEPC baseline (CEPC-B) precisions**, experimental uncertainties will be mostly reduced by CEPC measurements; theoretical uncertainties of  $m_W$ ,  $\sin^2\theta_{\text{eff}}^\ell$ , and  $\Gamma_Z$  can be reduced by fully calculating 3-loop corrections in the future

CEPC improved (CEPC-I) precisions need

- A high-precision beam energy calibration for improving  $m_Z$  and  $\Gamma_Z$  measurements
- A  $t\bar{t}$  threshold scan for the  $m_t$  measurement at other  $e^+e^-$  colliders, like ILC

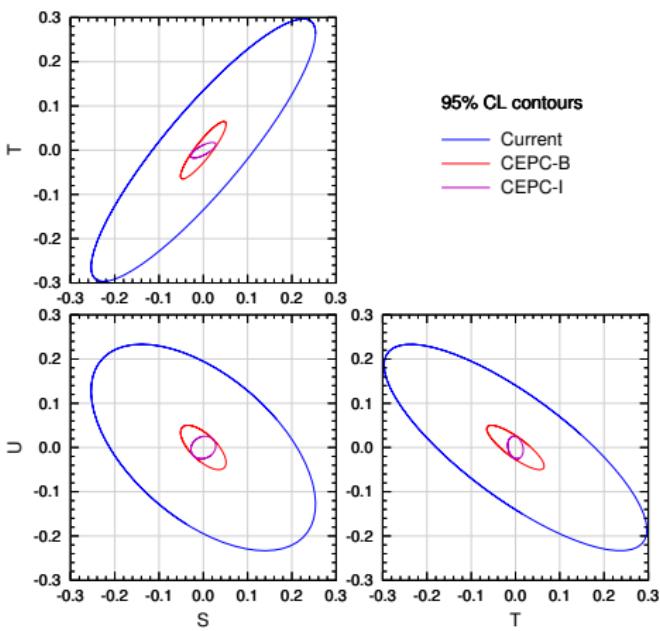
# Global Fit

**Modified  $\chi^2$  function** [JJ Fan, Reece, LT Wang, 1411.1054, JHEP]:

$$\sum_i \left( \frac{O_i^{\text{meas}} - O_i^{\text{pred}}}{\sigma_i} \right)^2 + \sum_j \left\{ -2 \ln \left[ \operatorname{erf} \left( \frac{O_j^{\text{meas}} - O_j^{\text{pred}} + \delta_j}{\sqrt{2}\sigma_j} \right) \right] - \operatorname{erf} \left( \frac{O_j^{\text{meas}} - O_j^{\text{pred}} - \delta_j}{\sqrt{2}\sigma_j} \right) \right] \right\}$$

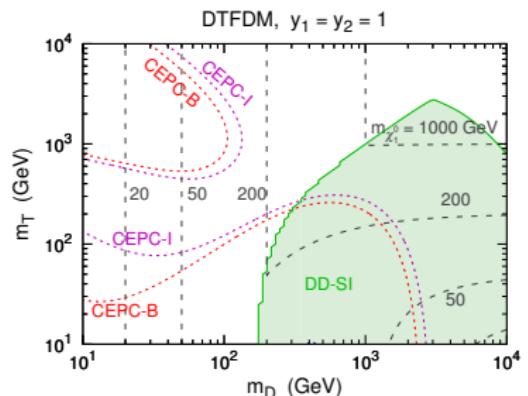
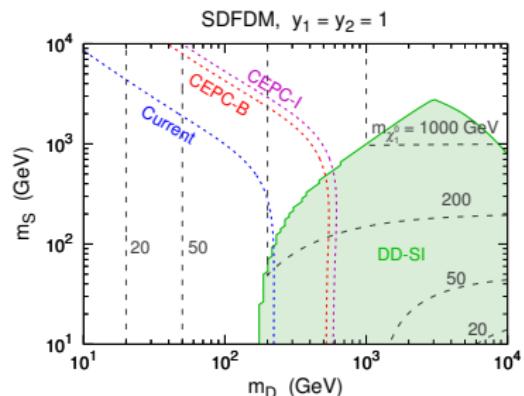
The **experimental uncertainty**  $\sigma_j$  and the **theoretical uncertainty**  $\delta_j$  of an observable  $O_j$  are treated as **Gaussian** and **flat** errors

	Current	CEPC-B	CEPC-I
$\sigma_S$	0.10	0.021	0.011
$\sigma_T$	0.12	0.026	0.0071
$\sigma_U$	0.094	0.020	0.010
$\rho_{ST}$	+0.89	+0.90	+0.74
$\rho_{SU}$	-0.55	-0.68	+0.15
$\rho_{TU}$	-0.80	-0.84	-0.21



[CF Cai, ZHY, HH Zhang, 1611.02186, NPB]

# CEPC Sensitivity to Fermionic Models

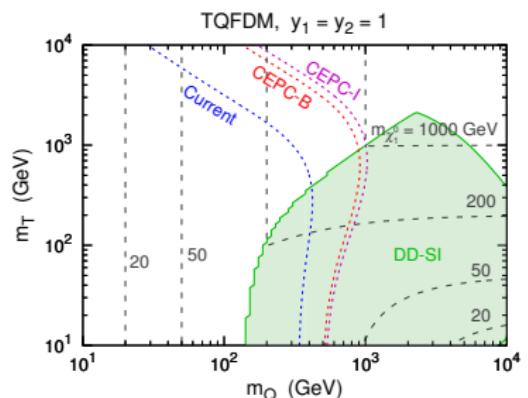


🎯 **Dotted lines:** expected 95% CL constraints from **current**, **CEPC-B**, and **CEPC-I** precisions of EW oblique parameters assuming  $T = U = 0$

🔍 **DD-SI:** excluded by spin-independent direct detection experiments at 90% CL

✍ **Dashed lines:** DM particle mass

[CF Cai, ZHY, HH Zhang, 1611.02186, NPB]

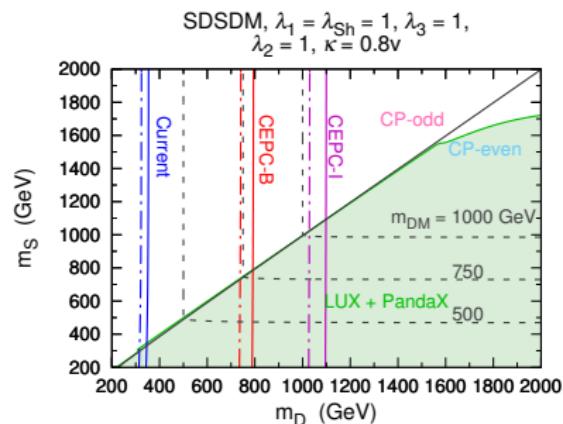
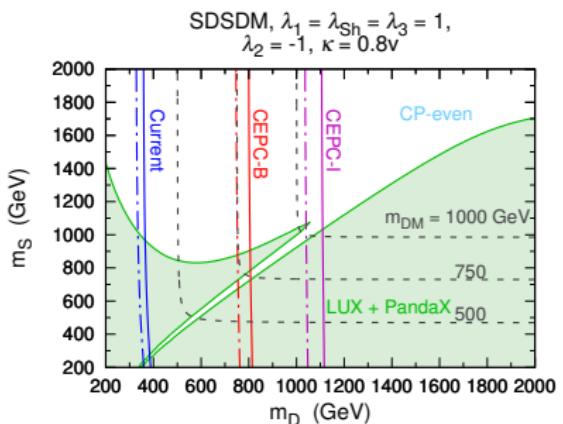


# Singlet-Doublet Scalar Dark Matter (SDSDM)

 A **real singlet scalar**  $S \in (1, 0)$  and a **complex doublet scalar**  $\Phi \in (2, 1/2)$ :

$$\mathcal{L} \supset \frac{1}{2}(\partial_\mu S)^2 - \frac{1}{2}m_S^2 S^2 + (D_\mu \Phi)^\dagger D^\mu \Phi - m_D^2 |\Phi|^2 - (\kappa S \Phi^\dagger H + \text{h.c.}) - \frac{1}{2}\lambda_{Sh} S^2 |H|^2 \\ - \lambda_1 |H|^2 |\Phi|^2 - [\lambda_2 (\Phi^\dagger H)^2 + \text{h.c.}] - \lambda_3 |\Phi^\dagger H|^2$$

 The DM candidate can be either a **CP-even** or **CP-odd** scalar



**Dot-dashed lines:** free  $S$ ,  $T$ , and  $U$

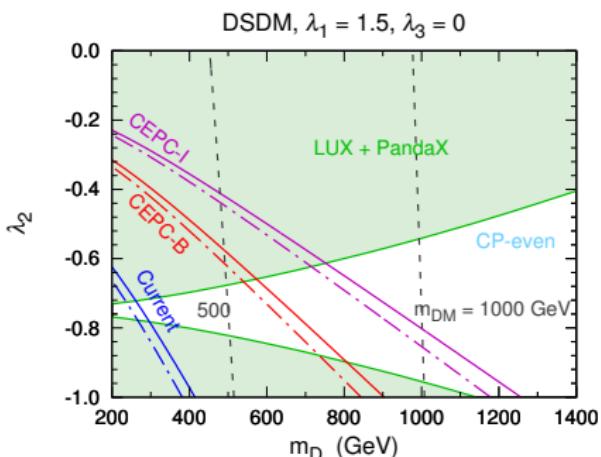
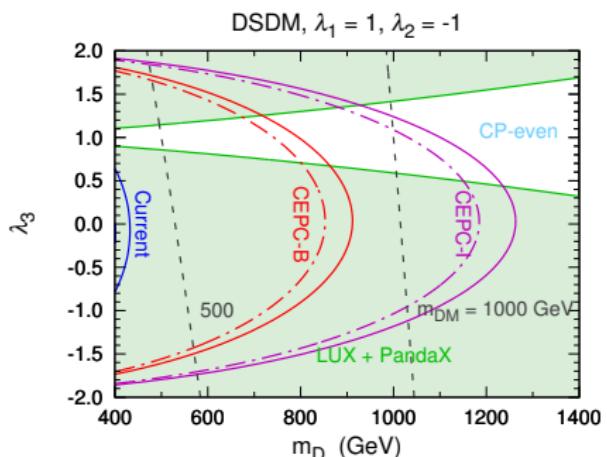
**Solid lines:** assuming  $U = 0$

[CF Cai, ZHY, HH Zhang, 1705.07921, NPB]

# Reduction to the Inert Higgs Doublet Model

 In the limit  $\kappa = 0$  and  $m_S \rightarrow \infty$ , the singlet decouples the SDSDM model reduces to the **inert Higgs doublet model** [Deshpande, Ma, PRD 18, 2574 (1978)]

- $\lambda_2 < 0$ : **CP-even** DM candidate, coupling to the Higgs  $\propto \lambda_1 + 2\lambda_2 + \lambda_3$
- $\lambda_2 > 0$ : **CP-odd** DM candidate, coupling to the Higgs  $\propto \lambda_1 - 2\lambda_2 + \lambda_3$



**Dot-dashed lines:** free  $S$ ,  $T$ , and  $U$

**Solid lines:** assuming  $U = 0$

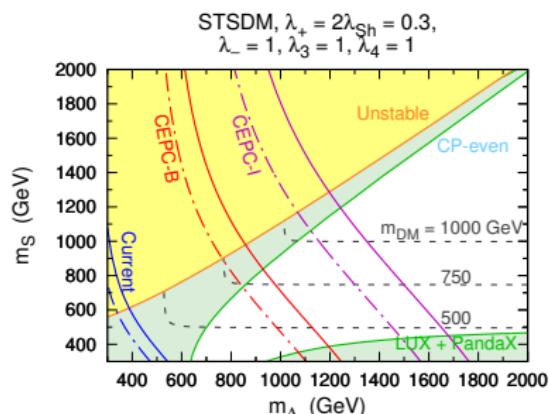
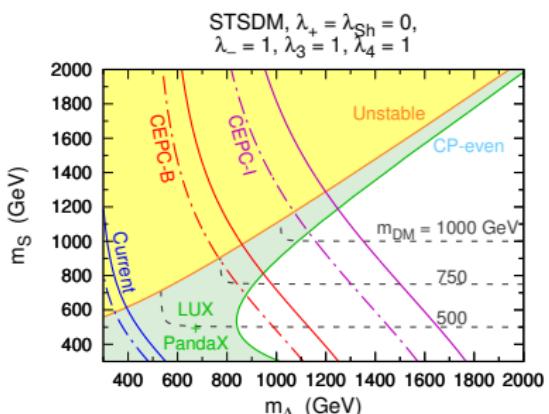
[CF Cai, ZHY, HH Zhang, 1705.07921, NPB]

# Singlet-Triplet Scalar Dark Matter (STSDM)

 A **real singlet scalar**  $S \in (1, 0)$  and a **complex triplet scalar**  $\Delta \in (3, 0)$ :

$$\begin{aligned} -\mathcal{L} \supset & \frac{1}{2} m_S^2 S^2 + m_\Delta^2 |\Delta|^2 + \frac{1}{2} \lambda_{Sh} S^2 |H|^2 + \lambda_0 |H|^2 |\Delta|^2 + \lambda_1 H_i^\dagger \Delta_j^i (\Delta^\dagger)_k^j H^k \\ & + \lambda_2 H_i^\dagger (\Delta^\dagger)_j^i \Delta_k^j H^k - (\lambda_3 H_i^\dagger \Delta_j^i \Delta_k^j H^k + \lambda'_3 |H|^2 \Delta_j^i \Delta_i^j + \lambda_4 S H_i^\dagger \Delta_j^i H^j + \text{h.c.}) \end{aligned}$$

 Define  $\lambda_{\pm} \equiv \lambda_1 \pm \lambda_2$ , and  $\lambda'_3$  and  $\lambda_0$  can be absorbed into  $\lambda_3$  and  $\lambda_+$



**Dot-dashed lines:** assuming  $S = 0$

**Solid lines:** assuming  $S = U = 0$

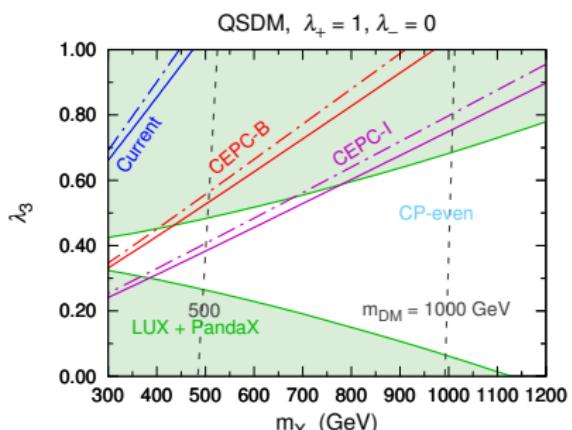
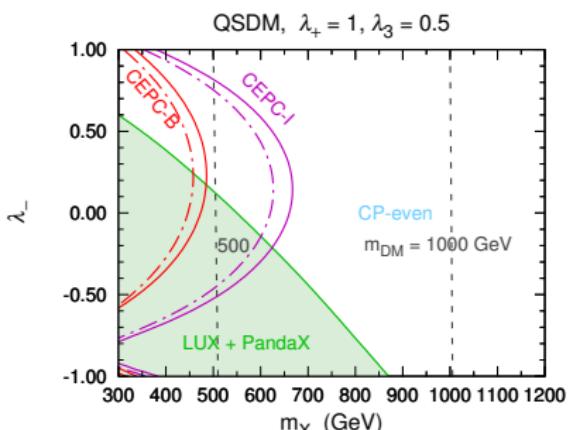
[CF Cai, ZHY, HH Zhang, 1705.07921, NPB]

# Quadruplet Scalar Dark Matter (QSDM)

 A **complex quadruplet scalar**  $X \in (4, 1/2)$ :

$$\begin{aligned} -\mathcal{L} \supset & m_X^2 |X|^2 + \lambda_0 |H|^2 |X|^2 + \lambda_1 H_i^\dagger X_k^{ij} (X^\dagger)_{jl}^k H^l + \lambda_2 H_i^\dagger (X^\dagger)_{jk}^i X_l^{jk} H^l \\ & - (\lambda_3 H_i^\dagger H_j^\dagger X_l^{ik} X_k^{jl} + \text{h.c.}) \end{aligned}$$

 Define  $\lambda_{\pm} \equiv \lambda_1 \pm \lambda_2$ , and  $\lambda_0$  can be absorbed into  $\lambda_+$



**Dot-dashed lines:** free  $S, T$ , and  $U$

**Solid lines:** assuming  $U = 0$

[CF Cai, ZHY, HH Zhang, 1705.07921, NPB]

# Conclusions

- ① WIMP models can be naturally constructed by extending the Standard Model with a dark sector consisting of **electroweak multiplets**, whose electrically neutral components provide a DM candidate.
- ② Such models typically introduce several **new electroweak particles** that could lead to remarkable signatures at  $pp$  and  $e^+e^-$  colliders.
- ③ We have studied the corresponding **direct production signals** at the **LHC** and at the future **SPPC**, as well as the indirect searches via **Higgs and electroweak precision measurements** at the future **CEPC**.

# Conclusions

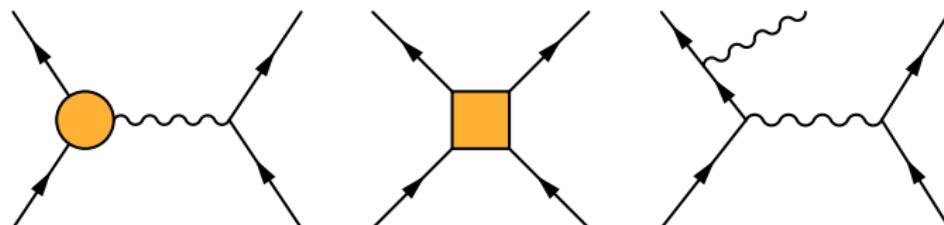
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- ➌ We have studied the corresponding **direct production signals** at the **LHC** and at the future **SPPC**, as well as the indirect searches via **Higgs and electroweak precision measurements** at the future **CEPC**.

**Thanks for your attention!**

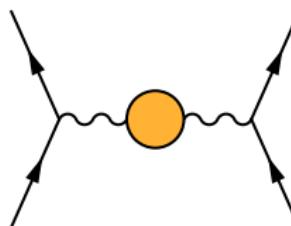
# Electroweak Radiative Corrections

## Two classes of EW radiative corrections

- **Direct Corrections:** vertex, box, and bremsstrahlung corrections



- **Oblique Corrections:** gauge boson propagator corrections



Oblique corrections can be treated in a self-consistent and model-independent way through an effective lagrangian to incorporate a large class of Feynman diagrams into a few **running couplings** [Kennedy & Lynn, NPB 322, 1 (1989)]

# Custodial Symmetry

Standard model (SM) scalar potential  $V = -\mu^2 H^\dagger H + \lambda(H^\dagger H)^2$  is a function of  $H^\dagger H$ , which respects an  $SU(2)_L \times SU(2)_R$  **global symmetry**:

$$H^\dagger H = -\frac{1}{2} \epsilon_{AB} \epsilon^{ij} (\mathcal{H}^A)_i (\mathcal{H}^B)_j, \quad (\mathcal{H}^A)_i \equiv \begin{pmatrix} H_i^\dagger \\ H_i \end{pmatrix} \text{ is an } SU(2)_R \text{ doublet}$$

$$H \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix} \Rightarrow SU(2)_L \times SU(2)_R \rightarrow \textcolor{red}{SU(2)_{L+R} \text{ custodial symmetry}}$$



$SU(2)_L$  gauge bosons  $W_\mu^a$  transform as an  $SU(2)_{L+R}$  triplet and acquire the same mass from EW symmetry breaking



The custodial symmetry protects the tree-level relation  $\rho \equiv m_W^2 / (m_Z^2 c_W^2) = 1$  up to EW radiative corrections [Sikivie et al., NPB 173, 189 (1980)], and leads to  $T = U = 0$  (note that  $\rho - 1 = \alpha T$ )

The custodial symmetry is **approximate** in the SM, explicitly broken by the Yukawa couplings of fermions and the  $U(1)_Y$  gauge interaction

Electroweak Precision Observables

For evaluating CEPC precision of oblique parameters, we use a simplified set of EW precision observables in the **global fit**:

$$\alpha_s(m_Z^2), \Delta\alpha_{\text{had}}^{(5)}(m_Z^2), m_Z, m_t, m_h, m_W, \sin^2\theta_{\text{eff}}^\ell, \Gamma_Z$$

**Free parameters:** the former 5 observables,  $S$ ,  $T$ , and  $U$

The remaining 3 observables are determined by the free parameters:

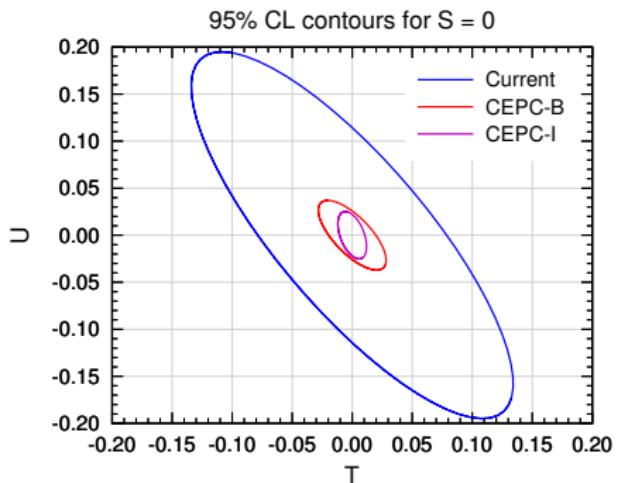
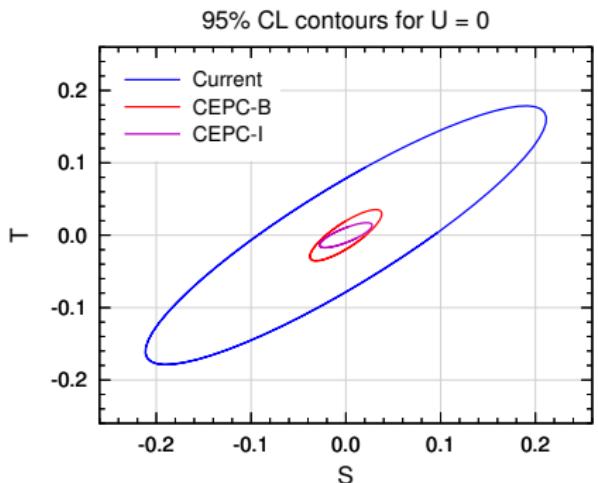
$$m_W = m_W^{\text{SM}} \left[ 1 - \frac{\alpha}{4(c_W^2 - s_W^2)} (S - 1.55T - 1.24U) \right]$$

$$\sin^2 \theta_{\text{eff}}^\ell = (\sin^2 \theta_{\text{eff}}^\ell)^{\text{SM}} + \frac{\alpha}{4(c_w^2 - s_w^2)}(S - 0.69T)$$

$$\Gamma_Z = \Gamma_Z^{\text{SM}} - \frac{\alpha^2 m_Z}{72 s_W^2 c_W^2 (c_W^2 - s_W^2)} (12.2\mathcal{S} - 32.9\mathcal{T})$$

The calculation of **SM predictions** is based on 2-loop radiative corrections

# Fit Results for Some Parameters Fixed to 0



$T = U = 0$  fixed

	Current	CEPC-B	CEPC-I
$\sigma_S$	0.037	0.0085	0.0068

$S = U = 0$  fixed

	Current	CEPC-B	CEPC-I
$\sigma_T$	0.032	0.0079	0.0042

# DM Models with Electroweak Multiplets

We study the CEPC sensitivity to WIMP models with a dark sector consisting of **EW multiplets**. By imposing a  $Z_2$  symmetry, the DM candidate would be the lightest mass eigenstate of the neutral components.

- ➊ EW oblique parameters  $S$ ,  $T$ , and  $U$  respond to **EW symmetry breaking**
  - **Mass splittings** among the multiplet components induced by the nonzero Higgs VEV would break the EW symmetry  
⇒ **Nonzero oblique parameters**
  - If the Higgs VEV just gives a **common mass shift** to every components in a multiplet, the effect can be absorbed into the gauge-invariant mass term  
⇒ No EW symmetry breaking effect manifests  
⇒ **Vanishing  $S$ ,  $T$ , and  $U$**
- ➋  $S$  relates to the  $U(1)_Y$  gauge field  
⇒ A multiplet with **zero hypercharge cannot contribute to  $S$**
- ➌ Multiplet couplings to the Higgs respect a **custodial symmetry**  
⇒ **Vanishing  $T$  and  $U$**

# Fermionic and Scalar Multiplets

In order to have nonzero contributions to EW oblique parameters, **dark sector multiplets should couple to the SM Higgs doublet**

## ① Fermionic multiplets

- **1 vector-like fermionic  $SU(2)_L$  multiplet:** the  $Z_2$  symmetry for stabilizing DM forbids the multiplet coupling to the Higgs  $\Rightarrow S = T = U = 0$
- **2 types of vector-like  $SU(2)_L$  multiplets whose dimensions differ by one:**  
Yukawa couplings split the components  $\Rightarrow$  Nonzero oblique parameters

## ② Scalar multiplets

- **1 real scalar multiplet  $\Phi$ :** the quartic coupling  $\lambda' \Phi^\dagger \Phi H^\dagger H$  can only induce a common mass shift  $\Rightarrow S = T = U = 0$
- **1 complex scalar multiplet  $\Phi$ :** the quartic coupling  $\lambda'' \Phi^\dagger \tau^a \Phi H^\dagger \sigma^a H$  can induce mass splittings  $\Rightarrow$  Nonzero oblique parameters
- **$\geq 2$  scalar multiplets:** various trilinear and quartic couplings could break the mass degeneracy  $\Rightarrow$  Nonzero oblique parameters

# Direct Detection

For a **Majorana DM candidate**  $\chi$ , the couplings to the Higgs and Z bosons

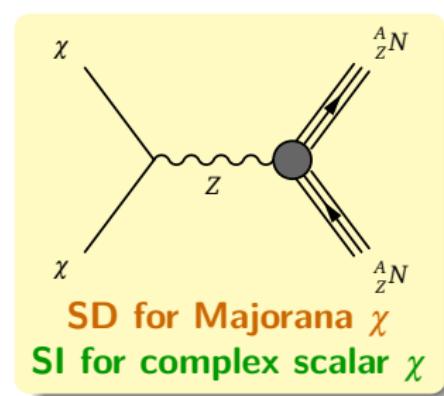
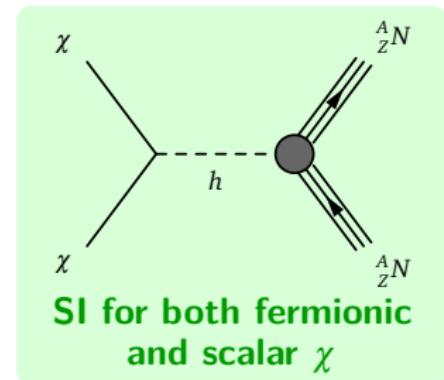
$$\mathcal{L} \supset \frac{1}{2} g_{h\chi\bar{\chi}} h \bar{\chi} \chi + \frac{1}{2} g_{Z\chi\bar{\chi}} Z_\mu \bar{\chi} \gamma^\mu \gamma_5 \chi$$

would induce **spin-independent (SI)** and **spin-dependent (SD)** DM-nucleus scatterings.

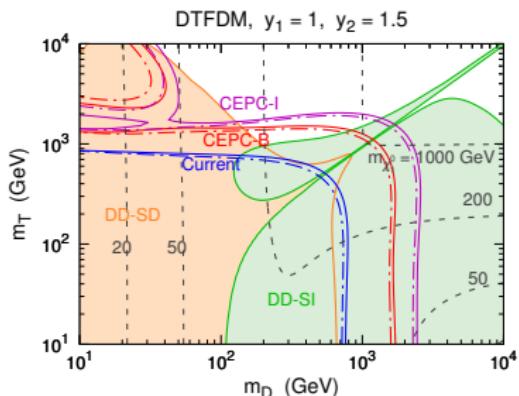
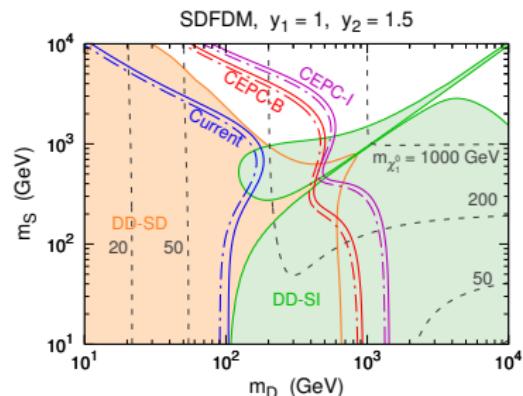
For scalar multiplets, interactions with the Higgs doublet could split the real and imaginary parts of neutral components, leading to a **CP-even or CP-odd real scalar DM candidate**. Its coupling to the Higgs boson would induce **SI scatterings**.

**Most stringent constraints from current direct detection experiments:**

- **SI:** PandaX-II [1607.07400], LUX [1608.07648]
- **SD:** PICO (proton) [1503.00008, 1510.07754], LUX (neutron) [1602.03489]



# Fermionic Models with $y_1 = 1$ and $y_2 = 1.5$

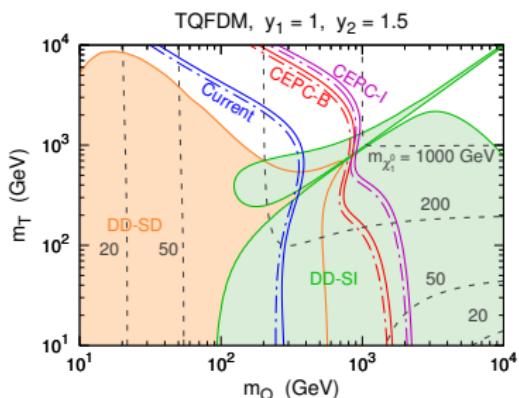


Expected 95% CL constraints from **current**, **CEPC-B**, and **CEPC-I** precisions of EW oblique parameters

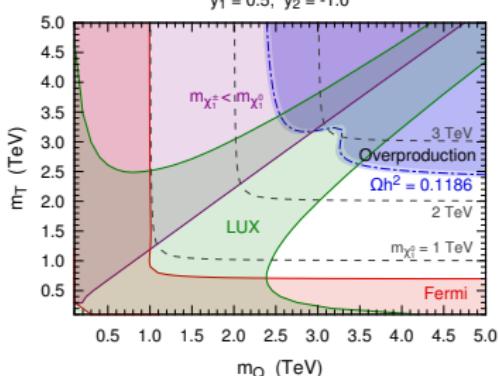
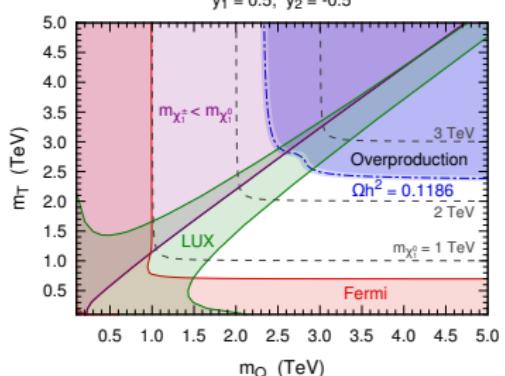
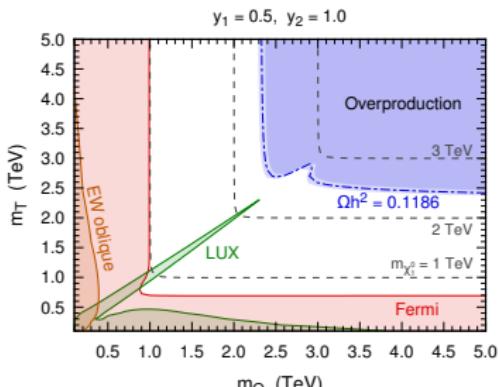
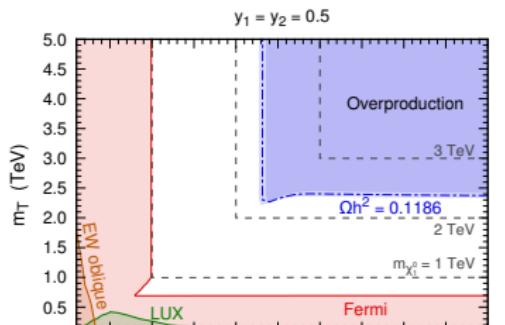
**Dot-dashed lines:** free  $S$ ,  $T$ , and  $U$   
**Solid lines:** assuming  $U = 0$

**DD-SI:** excluded by SI direct detection

**DD-SD:** excluded by SD direct detection



# Constraints on the TQFDM model



[Tait, ZHY, 1601.01354, JHEP]