

Triplet-Quadruplet Fermionic Dark Matter

Zhao-Huan Yu (余钊焕)

ARC Centre of Excellence for Particle Physics at the Terascale,
School of Physics, the University of Melbourne

Based on **Tim Tait and ZHY, arXiv:1601.01354, JHEP**



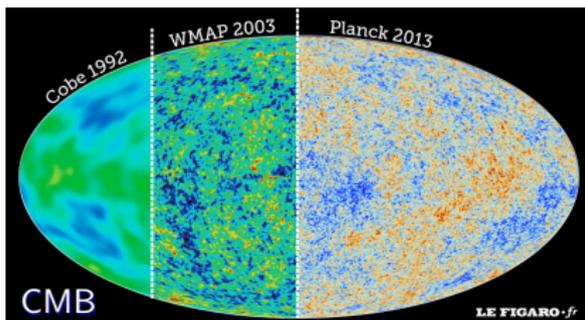
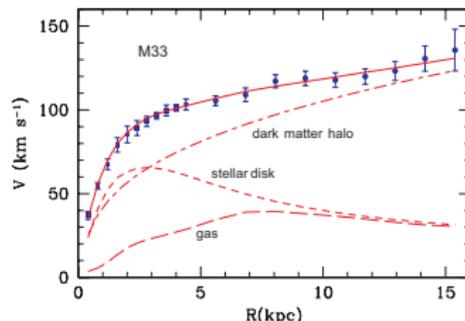
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Dark Matter in the Universe

Dark matter (DM) makes up most of the matter component in the Universe, as suggested by astrophysical and cosmological observations



Planck 2015
[1502.01589]

Cold DM (25.8%)

$$\Omega_c h^2 = 0.1186 \pm 0.0020$$

Baryons (4.8%)

$$\Omega_b h^2 = 0.02226 \pm 0.00023$$

Dark energy (69.3%)

$$\Omega_\Lambda = 0.692 \pm 0.012$$

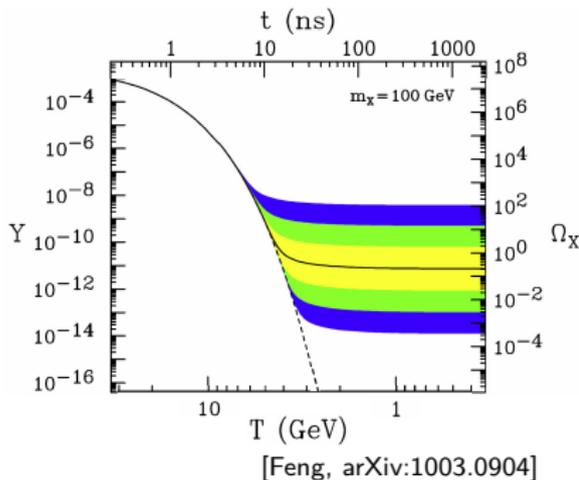
DM Relic Abundance

If DM particles (χ) were thermally produced in the early Universe, their **relic abundance** would be determined by the annihilation cross section $\langle\sigma_{\text{ann}}v\rangle$:

$$\Omega_\chi h^2 \simeq \frac{3 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}}{\langle\sigma_{\text{ann}}v\rangle}$$

Observation value $\Omega_\chi h^2 \simeq 0.1$

$$\Rightarrow \langle\sigma_{\text{ann}}v\rangle \simeq 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$



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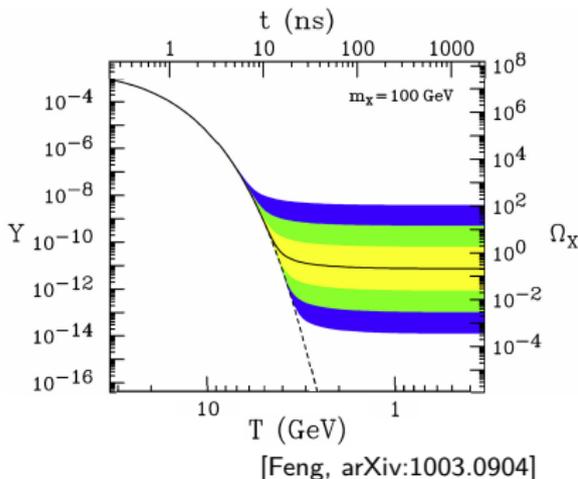
$$\Rightarrow \langle\sigma_{\text{ann}}v\rangle \simeq 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$$

Assuming the annihilation process consists of two weak interaction vertices with the $SU(2)_L$ gauge coupling $g \simeq 0.64$, for $m_\chi \sim \mathcal{O}(\text{TeV})$ we have

$$\langle\sigma_{\text{ann}}v\rangle \sim \frac{g^4}{16\pi^2 m_\chi^2} \sim \mathcal{O}(10^{-26}) \text{ cm}^3 \text{ s}^{-1}$$

\Rightarrow A very attractive class of DM candidates:

Weakly interacting massive particles (WIMPs)



WIMP Models

WIMPs are typically introduced in the extensions of the Standard Model (SM) aiming at solving the **gauge hierarchy problem**

- **Supersymmetry (SUSY):** the lightest neutralino ($\tilde{\chi}_1^0$)
- **Universal extra dimensions:** the lightest KK particle ($B^{(1)}$, $W^{3(1)}$, or $\nu^{(1)}$)

WIMP Models

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For DM phenomenology, it is quite natural to construct WIMP models by extending the SM with a dark sector consisting of **$SU(2)_L$ multiplets**, whose neutral components could provide a viable DM candidate

- 1 multiplet in a high-dimensional representation:
 - **minimal DM model** [Cirelli *et al.*, hep-ph/0512090]
(DM stability is explained by an accidental symmetry)
- 2 types of multiplets: **an artificial Z_2 symmetry is usually needed**
 - **Singlet-doublet DM model** [Mahbubani & Senatore, hep-ph/0510064; D'Eramo, 0705.4493; Cohen *et al.*, 1109.2604]
 - **Doublet-triplet DM model** [Dedes & Karamitros, 1403.7744]
 -

Connection to SUSY models

The above models with $SU(2)_L$ multiplets can be understood as **simplifications** of more complete models, but the model parameters are much more **free**

Singlet-doublet fermionic DM model:

- **Bino-higgsino** sector in the MSSM

$$\mathcal{L}_{\text{mass}} \supset -\frac{1}{2}M_1\tilde{B}\tilde{B} - \mu(\tilde{H}_u^+\tilde{H}_d^- - \tilde{H}_u^0\tilde{H}_d^0) + \frac{g'v_d}{\sqrt{2}}\tilde{B}\tilde{H}_d^0 - \frac{g'v_u}{\sqrt{2}}\tilde{B}\tilde{H}_u^0 + \text{h.c.}$$

- **Singlino-higgsino** sector in the NMSSM

$$\mathcal{L}_{\text{mass}} \supset -\kappa v_s\tilde{S}\tilde{S} - \lambda v_s(\tilde{H}_u^+\tilde{H}_d^- - \tilde{H}_u^0\tilde{H}_d^0) + \lambda v_u\tilde{S}\tilde{H}_d^0 + \lambda v_d\tilde{S}\tilde{H}_u^0 + \text{h.c.}$$

Doublet-triplet fermionic DM model: **higgsino-wino** sector in the MSSM

$$\begin{aligned} \mathcal{L}_{\text{mass}} \supset & -\frac{1}{2}M_2\tilde{W}^0\tilde{W}^0 - M_2\tilde{W}^+\tilde{W}^- - \mu(\tilde{H}_u^+\tilde{H}_d^- - \tilde{H}_u^0\tilde{H}_d^0) - \frac{g v_d}{\sqrt{2}}\tilde{W}^0\tilde{H}_d^0 \\ & + \frac{g v_u}{\sqrt{2}}\tilde{W}^0\tilde{H}_u^0 - g v_u\tilde{H}_u^+\tilde{W}^- - g v_d\tilde{W}^+\tilde{H}_d^- + \text{h.c.} \end{aligned}$$

Triplet-quadruplet fermionic DM model: **no analogue** in usual SUSY models

Triplet-Quadruplet Fermionic DM Model

Introduce left-handed Weyl fermions in the dark sector:

$$T = \begin{pmatrix} T^+ \\ T^0 \\ T^- \end{pmatrix} \in (\mathbf{3}, 0), \quad Q_1 = \begin{pmatrix} Q_1^+ \\ Q_1^0 \\ Q_1^- \\ Q_1^- \end{pmatrix} \in \left(\mathbf{4}, -\frac{1}{2} \right), \quad Q_2 = \begin{pmatrix} Q_2^{++} \\ Q_2^+ \\ Q_2^0 \\ Q_2^- \end{pmatrix} \in \left(\mathbf{4}, +\frac{1}{2} \right)$$

Covariant kinetic and mass terms:

$$\mathcal{L}_T = iT^\dagger \bar{\sigma}^\mu D_\mu T - \frac{1}{2}(m_T TT + \text{h.c.})$$

$$\mathcal{L}_Q = iQ_1^\dagger \bar{\sigma}^\mu D_\mu Q_1 + iQ_2^\dagger \bar{\sigma}^\mu D_\mu Q_2 - (m_Q Q_1 Q_2 + \text{h.c.})$$

Yukawa couplings: $\mathcal{L}_{\text{HTQ}} = y_1 \varepsilon_{jl} (Q_1)_i^{jk} T_k^i H^l - y_2 (Q_2)_i^{jk} T_k^i H_j^\dagger + \text{h.c.}$

Z₂ symmetry: odd for dark sector fermions, even for SM particles

⇒ forbids operators like TLH , $Te^c H^\dagger H^\dagger$, $Q_1 L^\dagger H H^\dagger$, $Q_2 L H H^\dagger$, ...

State Mixing

$$\begin{aligned}\mathcal{L}_{\text{mass}} &= -\frac{1}{2}(T^0, Q_1^0, Q_2^0)\mathcal{M}_N \begin{pmatrix} T^0 \\ Q_1^0 \\ Q_2^0 \end{pmatrix} - (T^-, Q_1^-, Q_2^-)\mathcal{M}_C \begin{pmatrix} T^+ \\ Q_1^+ \\ Q_2^+ \end{pmatrix} - m_Q Q_1^{--} Q_2^{++} + \text{h.c.} \\ &= -\frac{1}{2} \sum_{i=1}^3 m_{\chi_i^0} \chi_i^0 \chi_i^0 - \sum_{i=1}^3 m_{\chi_i^\pm} \chi_i^- \chi_i^+ + \text{h.c.} - m_Q \chi^- \chi^{++}\end{aligned}$$

$$\mathcal{M}_N = \begin{pmatrix} m_T & \frac{1}{\sqrt{3}}y_1 v & -\frac{1}{\sqrt{3}}y_2 v \\ \frac{1}{\sqrt{3}}y_1 v & 0 & m_Q \\ -\frac{1}{\sqrt{3}}y_2 v & m_Q & 0 \end{pmatrix}, \quad \mathcal{M}_C = \begin{pmatrix} m_T & \frac{1}{\sqrt{2}}y_1 v & -\frac{1}{\sqrt{6}}y_2 v \\ -\frac{1}{\sqrt{6}}y_1 v & 0 & -m_Q \\ \frac{1}{\sqrt{2}}y_2 v & -m_Q & 0 \end{pmatrix}$$

$$\begin{pmatrix} T^0 \\ Q_1^0 \\ Q_2^0 \end{pmatrix} = \mathcal{N} \begin{pmatrix} \chi_1^0 \\ \chi_2^0 \\ \chi_3^0 \end{pmatrix}, \quad \begin{pmatrix} T^+ \\ Q_1^+ \\ Q_2^+ \end{pmatrix} = \mathcal{C}_L \begin{pmatrix} \chi_1^+ \\ \chi_2^+ \\ \chi_3^+ \end{pmatrix}, \quad \begin{pmatrix} T^- \\ Q_1^- \\ Q_2^- \end{pmatrix} = \mathcal{C}_R \begin{pmatrix} \chi_1^- \\ \chi_2^- \\ \chi_3^- \end{pmatrix}$$

$$\chi^- \equiv Q_1^-, \quad \chi^{++} \equiv Q_2^{++}$$

3 Majorana fermions, 3 singly charged fermions, 1 doubly charged fermion
 χ_1^0 would be an excellent DM candidate if it is the lightest dark sector fermion

$y_1 = y_2$: Custodial Symmetry

When the two Yukawa couplings are **equal** ($y = y_1 = y_2$), the Lagrangian has an $SU(2)_L \times SU(2)_R$ **global symmetric form**:

$$\begin{aligned} \mathcal{L}_Q + \mathcal{L}_{\text{HTQ}} = & i(\mathbf{Q}^{\dagger A})_{ij}^k \bar{\sigma}^\mu D_\mu (\mathbf{Q}_A)^{ij}_k - \frac{1}{2} [m_Q \varepsilon^{AB} \varepsilon_{il} (\mathbf{Q}_A)^{ij}_k (\mathbf{Q}_B)^{lk}_j + \text{h.c.}] \\ & + [y \varepsilon^{AB} (\mathbf{Q}_A)^{jk}_i T_k^i (\mathbf{H}_B)_j + \text{h.c.}] \end{aligned}$$

$$SU(2)_R \text{ doublets: } (\mathbf{Q}_A)^{ij}_k = \begin{pmatrix} (Q_1)^{ij}_k \\ (Q_2)^{ij}_k \end{pmatrix}, \quad (\mathbf{H}_A)_i = \begin{pmatrix} H_i^\dagger \\ H_i \end{pmatrix}$$

This is a custodial symmetry, explicitly broken by $U(1)_Y$ **gauge interactions**

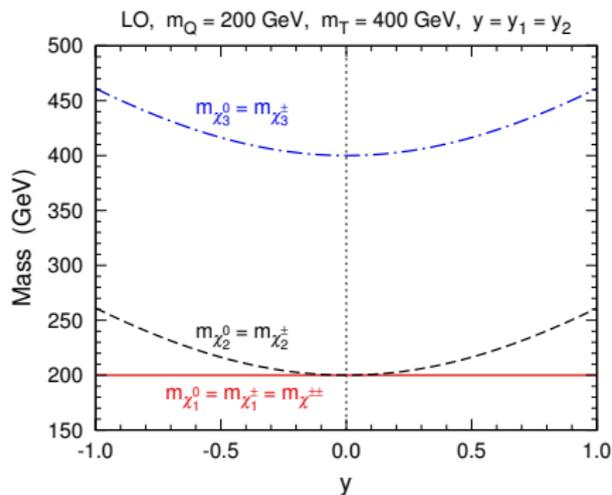
This approximate symmetry leads to **special mixing patterns**:

Identical magnitudes of Q_1 and Q_2 components in χ_i^0 and χ_i^\pm

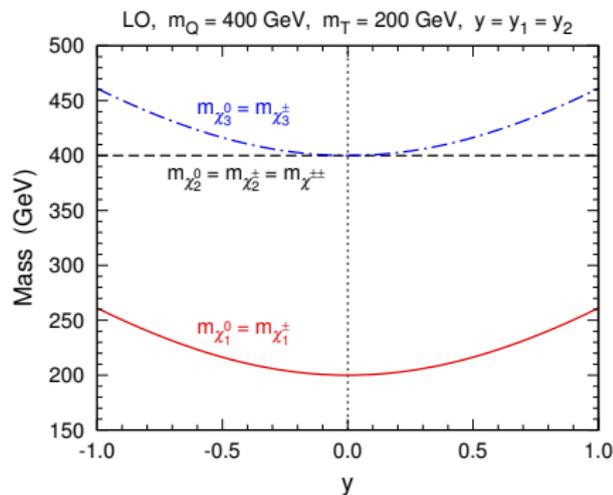
$y_1 = y_2$: Custodial Symmetry

In the custodial symmetry limit, each of the dark sector neutral fermions is **exactly degenerate in mass** with a singly charged fermion at the LO.

Mass corrections at the NLO are needed to check if $m_{\chi_1^0} < m_{\chi_1^\pm}, m_{\chi^{\pm\pm}}$.



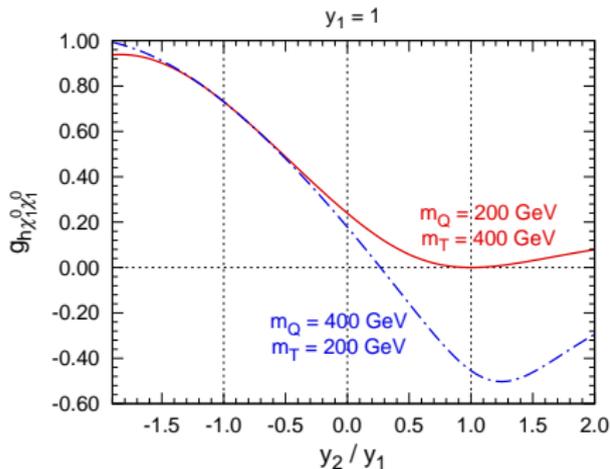
$m_Q < m_T$ case



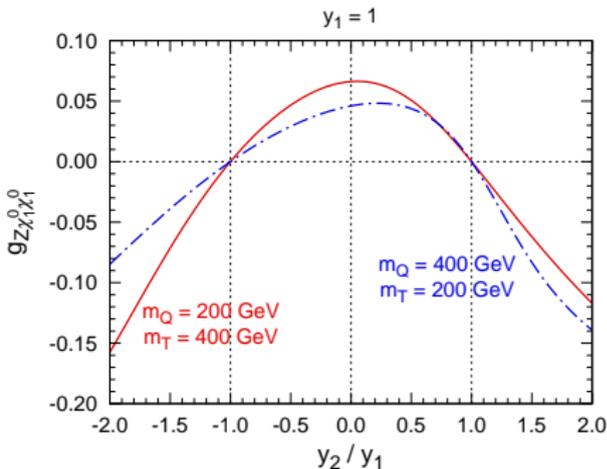
$m_T < m_Q$ case

$y_1 = y_2$: Custodial Symmetry

In the custodial symmetry limit, when $m_Q < m_T$, we have $\chi_1^0 = (Q_1^0 + Q_2^0)/\sqrt{2}$, which leads to **vanishing χ_1^0 couplings to h and Z** at the tree level. As a result, χ_1^0 cannot interact with nuclei at the LO and could easily escape from current DM direct detection bounds.

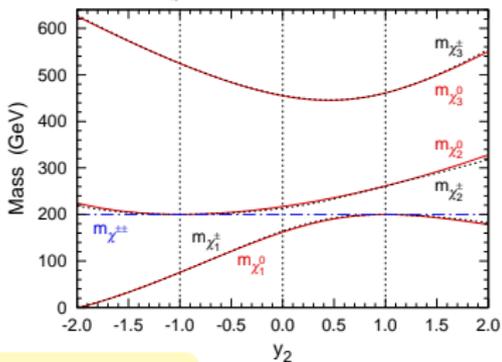
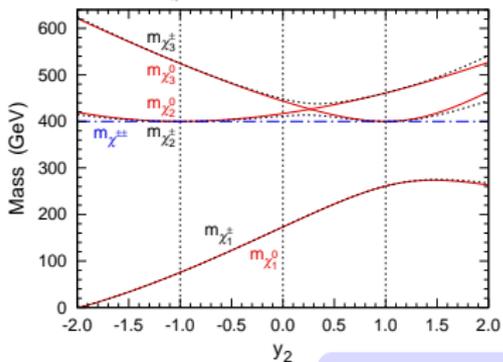
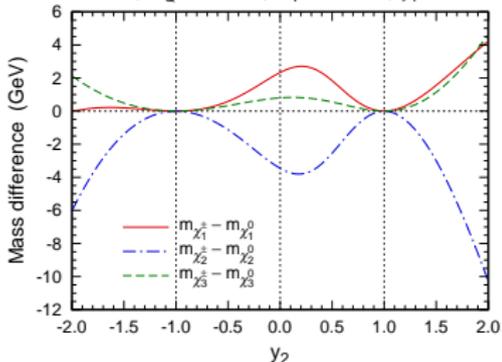
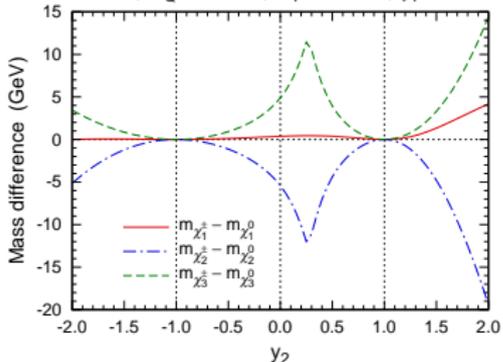


$h\chi_1^0\chi_1^0$ coupling



$Z\chi_1^0\chi_1^0$ coupling

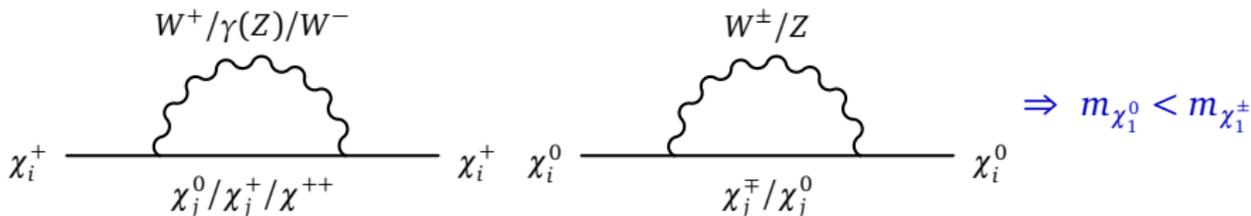
LO Mass Spectrum: Generally $m_{\chi_i^0} \simeq m_{\chi_i^\pm}$

LO, $m_Q = 200$ GeV, $m_T = 400$ GeV, $y_1 = 1$ LO, $m_Q = 400$ GeV, $m_T = 200$ GeV, $y_1 = 1$  $m_Q < m_T$ case $m_T < m_Q$ caseLO, $m_Q = 200$ GeV, $m_T = 400$ GeV, $y_1 = 1$ LO, $m_Q = 400$ GeV, $m_T = 200$ GeV, $y_1 = 1$ 

Mass Corrections at the NLO

One-loop corrections to an $SU(2)_L$ multiplet from **electroweak gauge boson loops** drive a charged component **heavier** than the neutral component (by $\sim Q^2 \cdot 170$ MeV for a multiplet much heavier than Z with $Y = 0$).

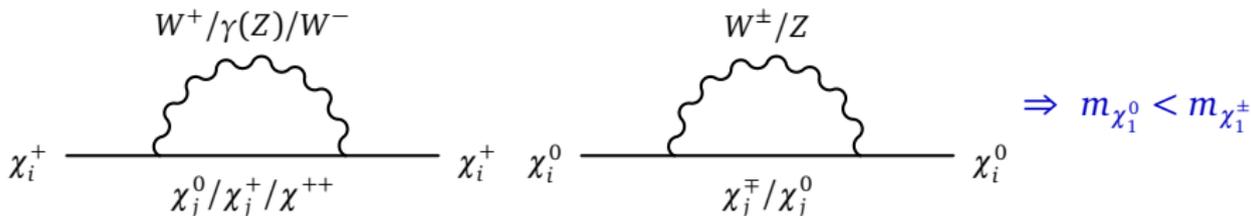
[Feng *et al.*, hep-ph/9904250; Cirelli *et al.*, hep-ph/0512090; Hill & Solon, 1111.0016]



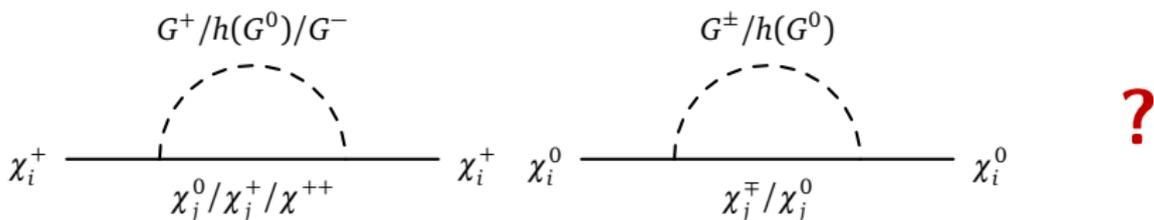
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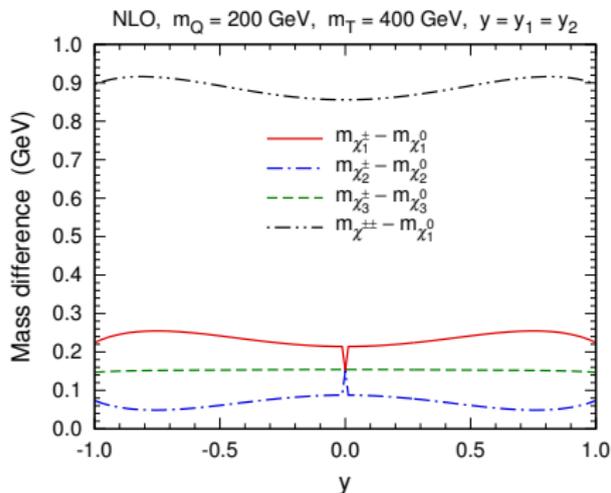


There are **mixings** among T , Q_1 , and Q_2 , and corrections from the Higgs sector due to the **HTQ Yukawa couplings**. The situation is more complicated.

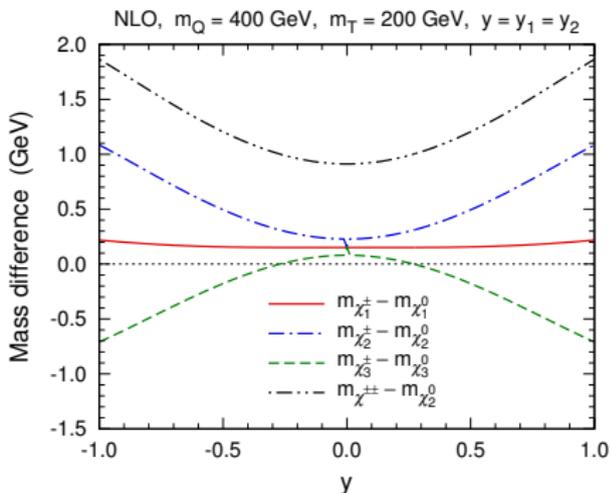


Mass Corrections at the NLO

In the **custodial symmetry limit**, we always have $m_{\chi_1^0} < m_{\chi_1^\pm}$ at the NLO and hence χ_1^0 is stable as required for a DM candidate.



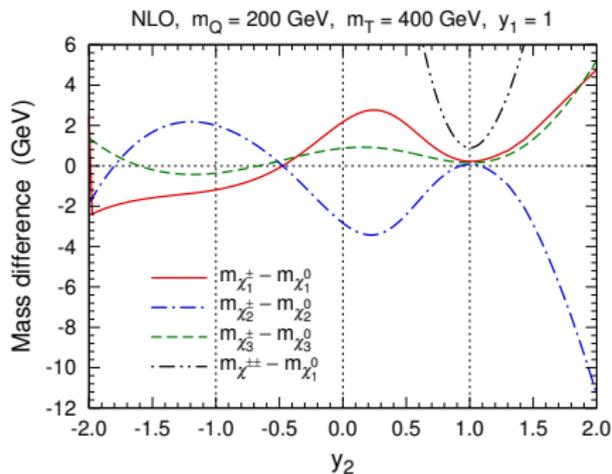
$m_Q < m_T$ case



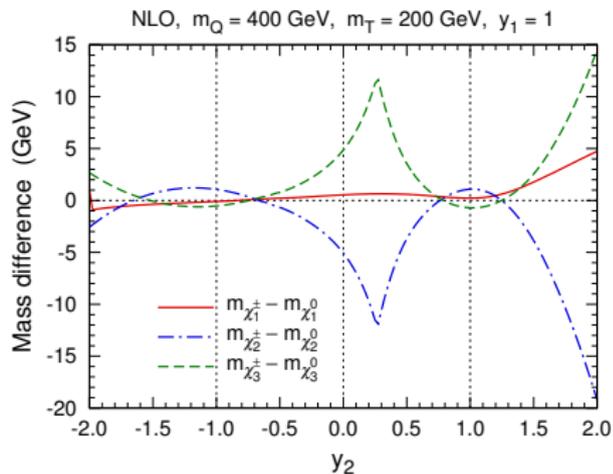
$m_T < m_Q$ case

Mass Corrections at the NLO

Beyond the custodial symmetry limit:



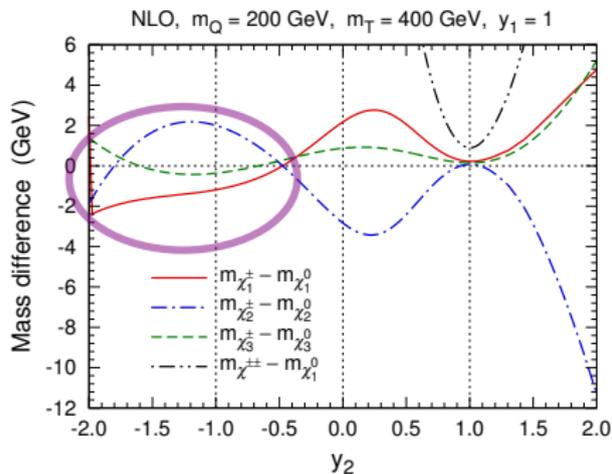
$m_Q < m_T$ case



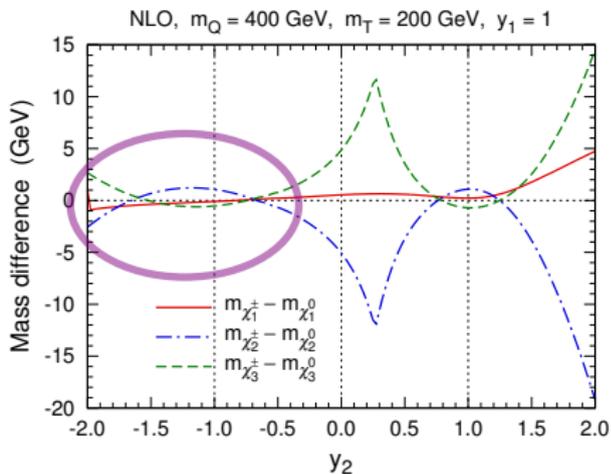
$m_T < m_Q$ case

Mass Corrections at the NLO

Beyond the custodial symmetry limit:



$m_Q < m_T$ case



$m_T < m_Q$ case

When y_1 and y_2 have opposite signs, we may have $m_{\chi_1^\pm} < m_{\chi_1^0}$ at the NLO and χ_1^0 is unstable and no longer a viable DM candidate.

Relic Abundance

In this model, we always have the mass degeneracy $m_{\chi_1^\pm} \simeq m_{\chi_1^0}$. Besides,

$$m_Q < m_T \quad \Rightarrow \quad \text{maybe } m_{\chi^{\pm\pm}} \simeq m_{\chi_1^0}$$

$$|y_{1,2\nu}| \ll m_Q < m_T \quad \Rightarrow \quad m_{\chi_2^0} \simeq m_{\chi_2^\pm} \simeq m_{\chi_1^0}$$

These dark sector fermions, with close masses and comparable interaction strengths, basically decoupled at the same time in the early Universe.

Coannihilation processes among them significantly affected their abundances.

After freeze-out, χ_1^\pm , $\chi^{\pm\pm}$, χ_2^0 , and χ_2^\pm decayed into χ_1^0 and contributed to the DM relic abundance.

FeynRules → **MadGraph** → **MadDM**:

includes all annihilation and coannihilation channels

$$\text{Observed DM abundance } \Omega h^2 = 0.1186 \quad \Leftrightarrow \quad m_{\chi_1^0} \sim 2.4 \text{ TeV}$$

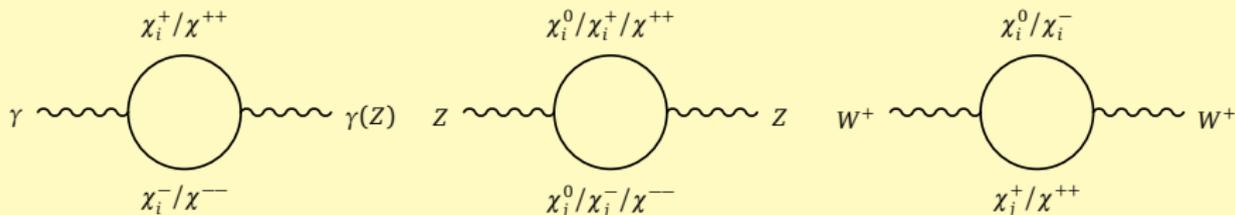
Electroweak Oblique Parameters

Electroweak oblique parameters S , T , and U describe new physics contributions through gauge boson propagator corrections [Peskin & Takeuchi, '90, '92]

$$S = \frac{16\pi c_W^2 s_W^2}{e^2} \left[\Pi'_{ZZ}(0) - \frac{c_W^2 - s_W^2}{c_W s_W} \Pi'_{ZA}(0) - \Pi'_{AA}(0) \right]$$

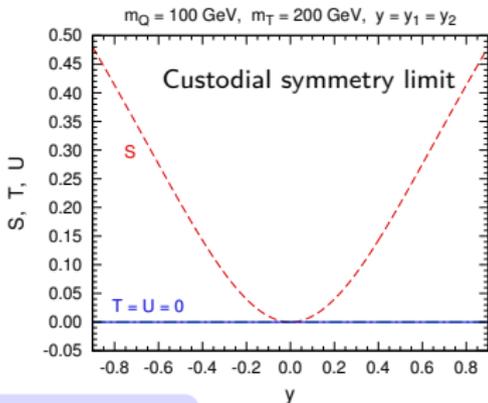
$$T = \frac{4\pi}{e^2} \left[\frac{\Pi_{WW}(0)}{m_W^2} - \frac{\Pi_{ZZ}(0)}{m_Z^2} \right]$$

$$U = \frac{16\pi s_W^2}{e^2} \left[\Pi'_{WW}(0) - c_W^2 \Pi'_{ZZ}(0) - 2c_W s_W \Pi'_{ZA}(0) - s_W^2 \Pi'_{AA}(0) \right]$$

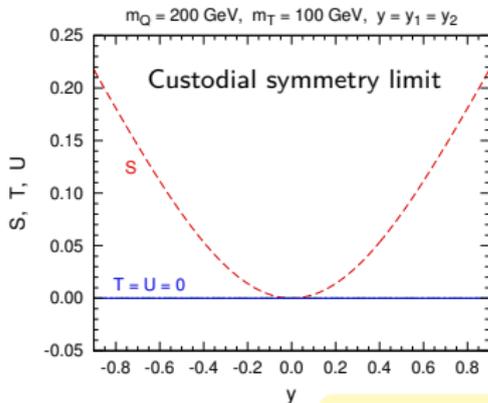


Gauge interactions of the triplet and quadruplets affect these parameters

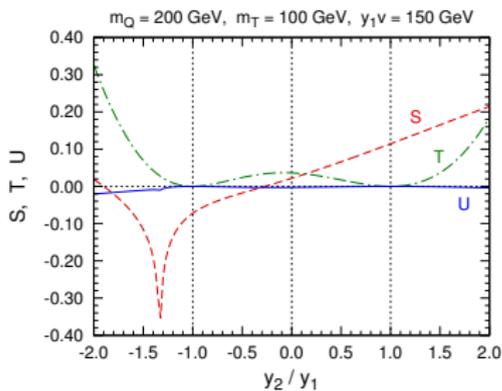
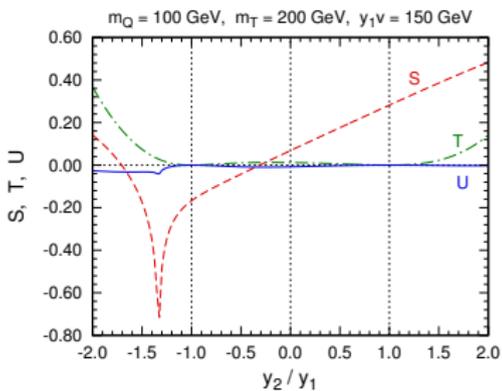
Prediction for Electroweak Oblique Parameters



$m_Q < m_T$ case



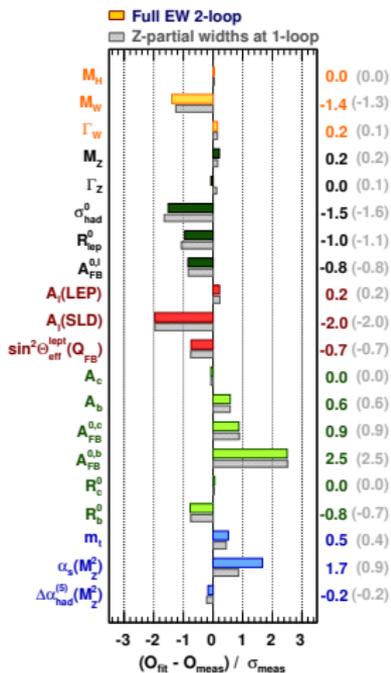
$m_T < m_Q$ case



Current Constraints on Electroweak Oblique Parameters

Global fit based on the measurements of **electroweak precision observables**:

[Gfitter Group, 1407.3792]



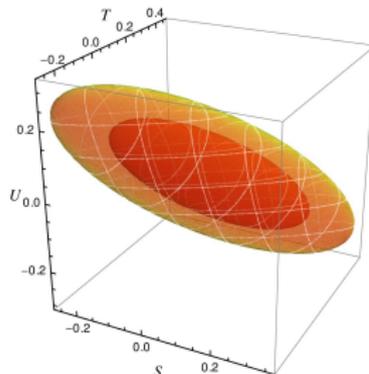
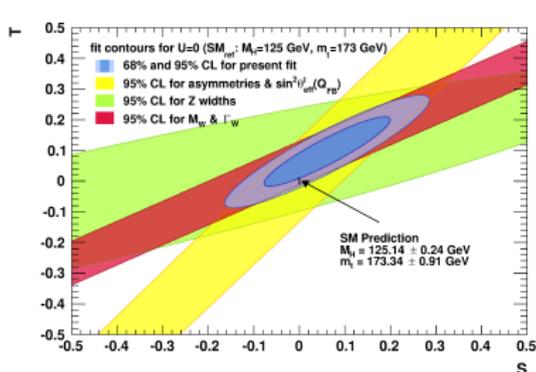
Fixed $U = 0 \rightarrow$

$$S = 0.06 \pm 0.09, T = 0.10 \pm 0.07, \rho_{ST} = +0.91$$

Free $U \rightarrow$

$$S = 0.05 \pm 0.11, T = 0.09 \pm 0.13, U = 0.01 \pm 0.11$$

$$\rho_{ST} = +0.90, \rho_{SU} = -0.59, \rho_{TU} = -0.83$$



Direct Detection

$$\mathcal{L} \supset \frac{1}{2} g_{h\chi_1^0\chi_1^0} h \bar{\chi}_1^0 \chi_1^0 + \frac{1}{2} g_{Z\chi_1^0\chi_1^0} Z_\mu \bar{\chi}_1^0 \gamma^\mu \gamma_5 \chi_1^0$$

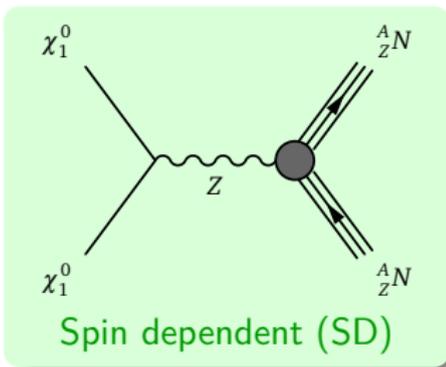
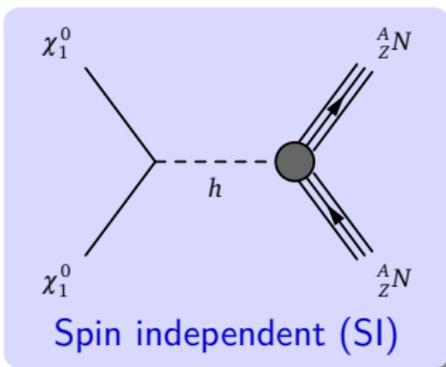
$$g_{h\chi_1^0\chi_1^0} = -\frac{2}{\sqrt{3}} (y_1 \mathcal{N}_{21} - y_2 \mathcal{N}_{31}) \mathcal{N}_{11}$$

$$g_{Z\chi_1^0\chi_1^0} = \frac{g}{2c_W} (|\mathcal{N}_{31}|^2 - |\mathcal{N}_{21}|^2)$$

For $m_Q < m_T$ in the **custodial symmetry limit**, we have $\mathcal{N}_{11} = 0$ and $|\mathcal{N}_{31}| = |\mathcal{N}_{21}|$, and both $g_{h\chi_1^0\chi_1^0}$ and $g_{Z\chi_1^0\chi_1^0}$ **vanish**

Current direct detection experiments are much more sensitive to the SI DM-nucleus scatterings than the SD scatterings

The exclusion limit on the SI cross section from the **LUX experiment** [1310.8214] is used to constrain the model



Indirect Detection

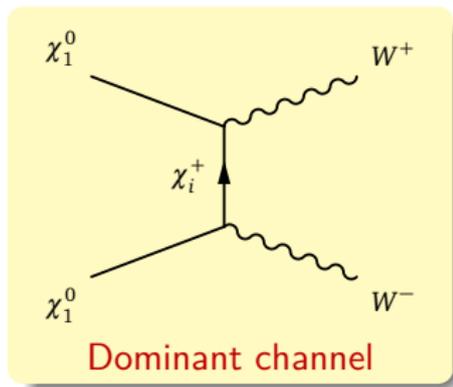
Indirect detection searches for products from **nonrelativistic DM annihilations**

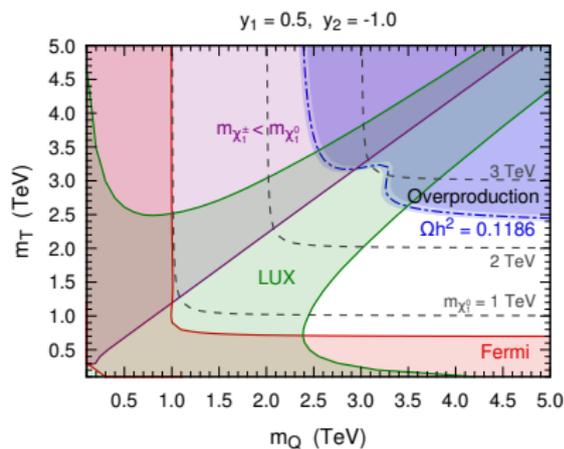
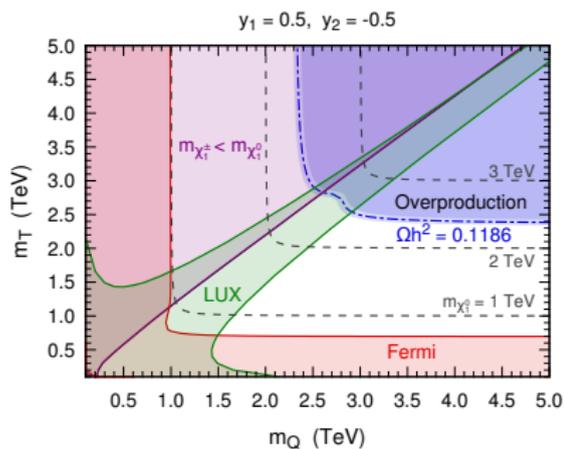
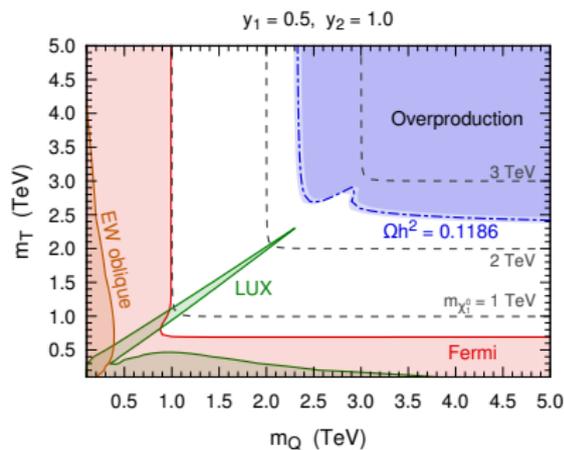
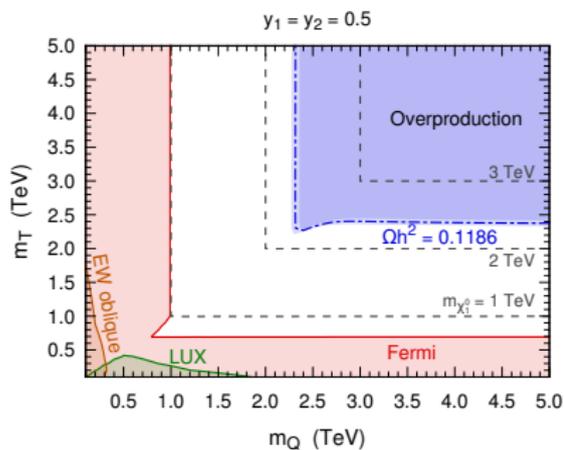
Suppressions on $\chi_1^0 \chi_1^0$ annihilations into SM particles

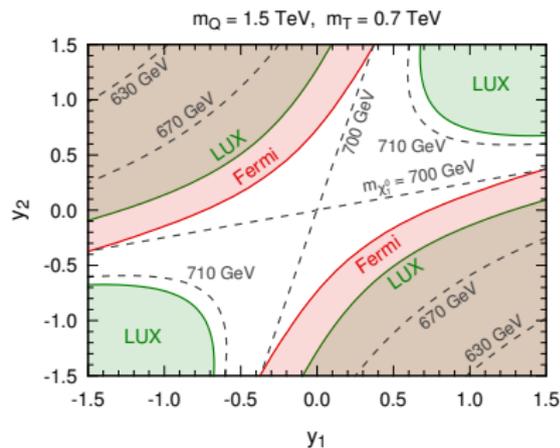
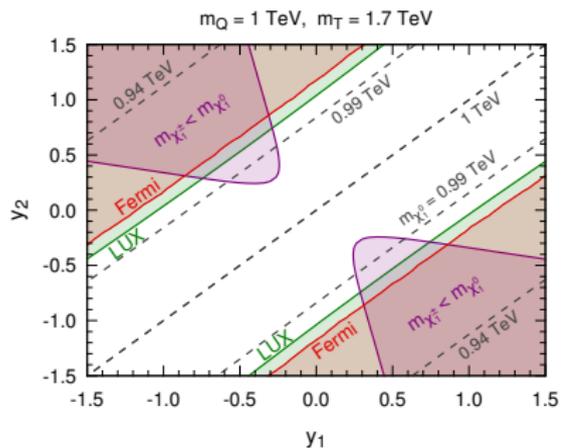
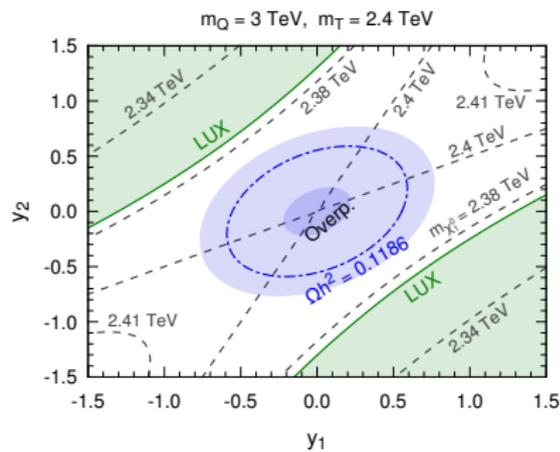
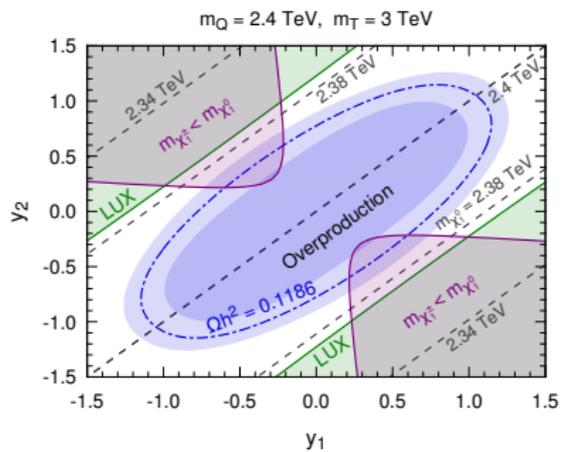
- $\chi_1^0 \chi_1^0 \rightarrow Z^* \rightarrow f \bar{f}$: helicity suppression in s wave ($\langle \sigma v \rangle \propto m_f^2 / m_{\chi_1^0}^2$)
- $\chi_1^0 \chi_1^0 \rightarrow h^* \rightarrow f \bar{f}$: p -wave suppression ($\langle \sigma v \rangle \propto v^2$)
- $\chi_1^0 \chi_1^0 \rightarrow hh$: p -wave suppression ($\langle \sigma v \rangle \propto v^2$)

The cross section of $\chi_1^0 \chi_1^0 \rightarrow W^+ W^-$ is typically larger than those of $\chi_1^0 \chi_1^0 \rightarrow ZZ, Zh, t\bar{t}$ by at least 1 to 2 orders of magnitude

The upper limit on the annihilation cross section into $W^+ W^-$ given by **Fermi-LAT** 6-year γ -ray observations of dwarf galaxies [1503.02641] is used to constrain the model







Conclusion

- 1 We investigate a **triplet-quadruplet WIMP model**, whose dark sector involves 3 Majorana fermions, 3 singly charged fermions, and 1 doubly charged fermion.
- 2 The triplet and quadruplets can interact with the SM Higgs doublet through two Yukawa couplings, whose equality leads to **an approximate custodial symmetry** that would make the DM candidate χ_1^0 easily escaping from direct searches.
- 3 There are mass degeneracies among dark sector fermions. **One-loop mass corrections** are calculated to check if χ_1^0 can be stable.
- 4 The observed relic abundance suggests $m_{\chi_1^0} \sim 2.4$ TeV. Phenomenological constraints from EW oblique parameters and direct and indirect detection experiments are also considered.

Thanks for your attention!

Outlook: Collider Signatures

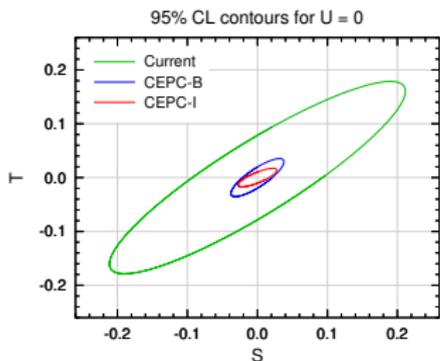
- **$h \rightarrow \gamma\gamma$ measurement:** contribution from χ_i^\pm loops
- **Monojet + \cancel{E}_T final state:** $pp \rightarrow \chi_1^0 \chi_1^0 + j$
- **Disappearing tracks:** $pp \rightarrow \chi_1^\pm \chi_1^\mp \rightarrow \pi^+ \pi^-$ (soft) + $\chi_1^0 \chi_1^0$
- **$2\ell + \cancel{E}_T$ final state:** $pp \rightarrow \chi_{2,3}^\pm \chi_{2,3}^\mp \rightarrow \ell^+ \ell^- + \nu\chi_1^0 \chi_1^0$
- **$3\ell + \cancel{E}_T$ final state with same-sign dilepton:**

$$pp \rightarrow \chi^{\pm\pm} \chi_{2,3}^\mp \rightarrow \ell^\pm \ell^+ \ell^- + \nu\nu\chi_1^0 \chi_1^0$$

$$pp \rightarrow \chi_{2,3}^\pm \chi_{2,3}^0 \rightarrow \ell^\pm \ell^+ \ell^- + \nu\chi_1^0 \chi_1^0$$
- **$4\ell + \cancel{E}_T$ final state:** $pp \rightarrow \chi^{\pm\pm} \chi^{\mp\mp} \rightarrow \ell^+ \ell^+ \ell^- \ell^- + \nu\nu\nu\chi_1^0 \chi_1^0$

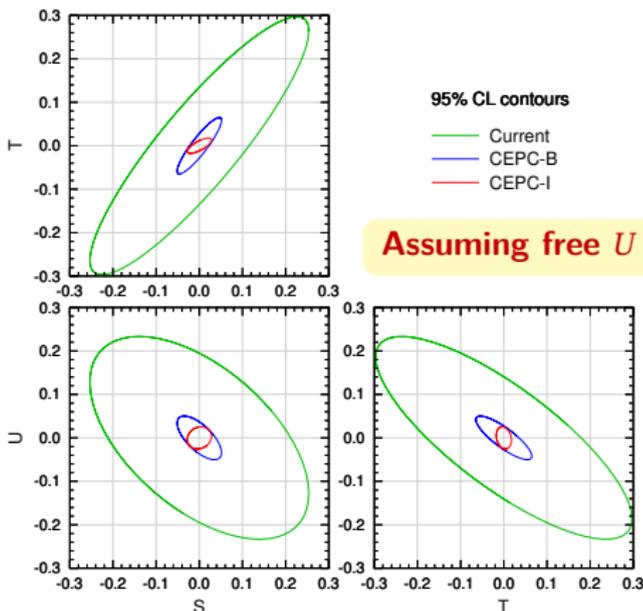
$$pp \rightarrow \chi_{2,3}^0 \chi_{2,3}^0 \rightarrow \ell^+ \ell^- \ell^+ \ell^- + \chi_1^0 \chi_1^0$$
-

Outlook: CEPC Precision for Electroweak Oblique Parameters



Assuming $U = 0$

[Cai, ZHY & Zhang, 1611.02186]

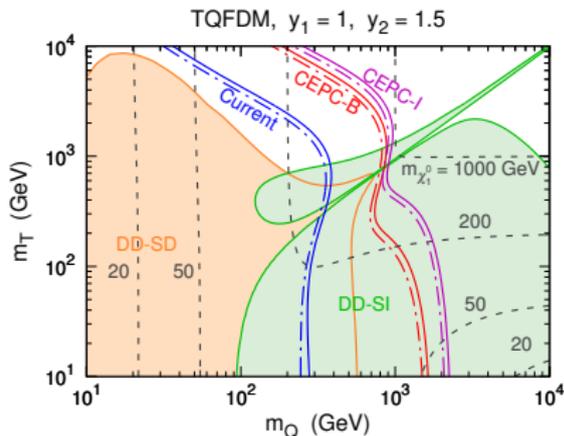
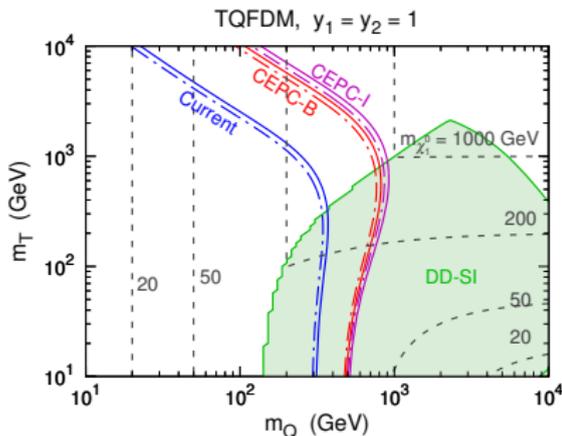


Current: current precision for EW oblique parameters [Gfitter Group, 1407.3792]

CEPC-B: CEPC baseline precision for EW oblique parameters

CEPC-I: CEPC precision with improvements of m_Z , Γ_Z , and m_t measurements

Outlook: CEPC Precision for Electroweak Oblique Parameters



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Solid lines: 95% CL constraints from the fitting results assuming $U = 0$

Dot-dashed lines: 95% CL constraints from the fitting results for free U

SI direct detection constraints: **PandaX-II** [1607.07400] and **LUX** [1608.07648]

SD direct detection constraints: **LUX** [1602.03489] and **PICO** [1503.00008, 1510.07754]

State Mixing in the Custodial Symmetry Limit

Mass spectrum for $y = y_1 = y_2$ and $m_Q < m_T$:

$$m_{\chi_1^0}^{\text{LO}} = m_{\chi_1^\pm}^{\text{LO}} = m_{\chi^{++}}^{\text{LO}} = m_Q$$

$$m_{\chi_2^0}^{\text{LO}} = m_{\chi_2^\pm}^{\text{LO}} = \frac{1}{2} \left[\sqrt{8y^2v^2/3 + (m_Q + m_T)^2} + m_Q - m_T \right]$$

$$m_{\chi_3^0}^{\text{LO}} = m_{\chi_3^\pm}^{\text{LO}} = \frac{1}{2} \left[\sqrt{8y^2v^2/3 + (m_Q + m_T)^2} - m_Q + m_T \right]$$

$$\mathcal{N} = \begin{pmatrix} 0 & \frac{ai}{b} & -\frac{\sqrt{2}}{b} \\ \frac{1}{\sqrt{2}} & -\frac{i}{b} & -\frac{a}{\sqrt{2}b} \\ \frac{1}{\sqrt{2}} & \frac{i}{b} & \frac{a}{\sqrt{2}b} \end{pmatrix}, \quad C_L = \begin{pmatrix} 0 & \frac{a}{b} & -\frac{\sqrt{2}i}{b} \\ \frac{i}{2} & -\frac{\sqrt{6}}{2b} & -\frac{\sqrt{3}ai}{2b} \\ \frac{\sqrt{3}i}{2} & \frac{\sqrt{2}}{2b} & \frac{ai}{2b} \end{pmatrix}, \quad C_R = \begin{pmatrix} 0 & -\frac{a}{b} & \frac{\sqrt{2}i}{b} \\ \frac{\sqrt{3}i}{2} & -\frac{\sqrt{2}}{2b} & -\frac{ai}{2b} \\ \frac{i}{2} & \frac{\sqrt{6}}{2b} & \frac{\sqrt{3}ai}{2b} \end{pmatrix}$$

Identical magnitudes of Q_1^0 and Q_2^0 components in χ_i^0
 Identical magnitudes of Q_1^+ (Q_2^+) and Q_2^- (Q_1^-) components in χ_i^\pm